

# LatentLLM: Activation-Aware Transform to Multi-Head Latent Attention

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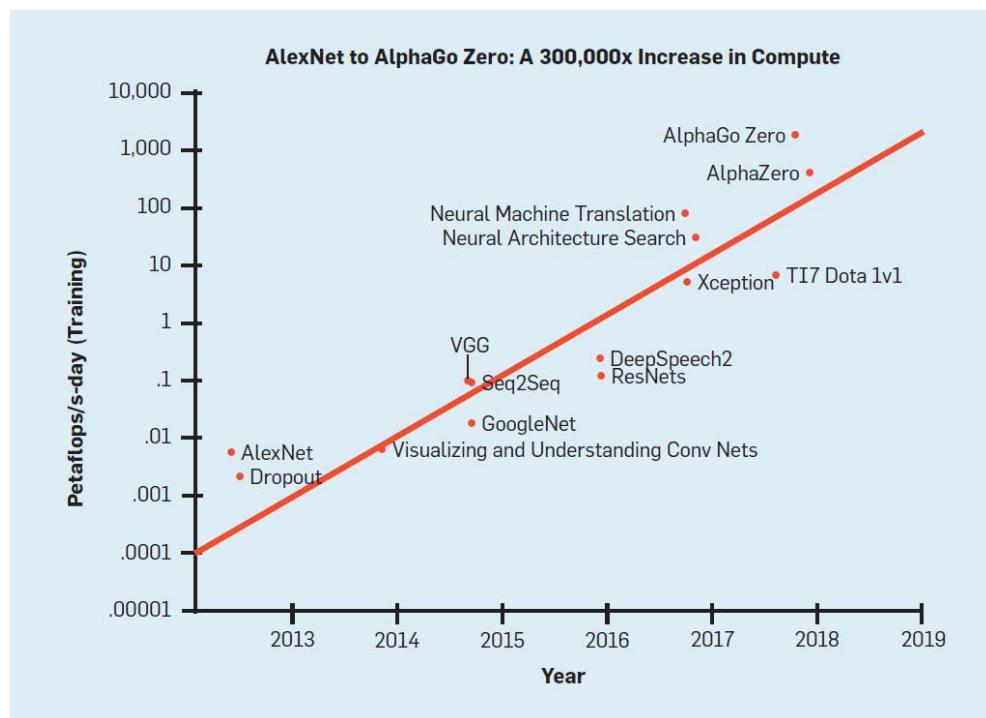
# Agenda

- Green AI overview
- Model compression: **LatentLLM**
  - Preconditioning matrix
  - Junction matrix
  - Attention-aware joint tensor decomposition
- Benchmark experiments
- Summary

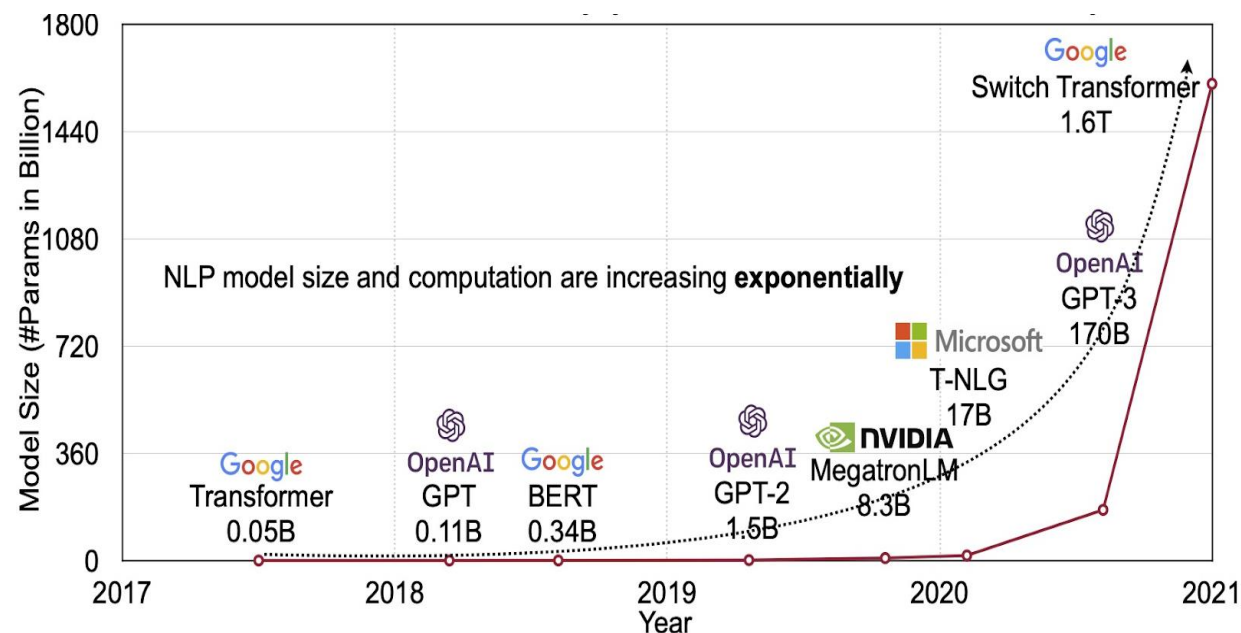


# Social Challenge: Red AI

- R. Schwartz et al., “Green AI” 2020.
  - Training compute has increased exponentially: **10-fold annually**.
- Strubell et al. “Energy and policy considerations for deep learning in NLP” 2019.
  - Training a single NLP model requires **5-fold higher** carbon emission of *single car lifetime*.



The computation used to train deep learning models has increased 300,000x in six years: nearly 10x annually



Language model increases exponentially over years

# Power Demand by AI Explosion

- High demand in electric power at data center driven by AI explosion, increasing bill
  - Electricity capacity prices jumped 833% in one regional auction
  - Some households saw \$27/month increases
  - All traced directly to data center electricity demand

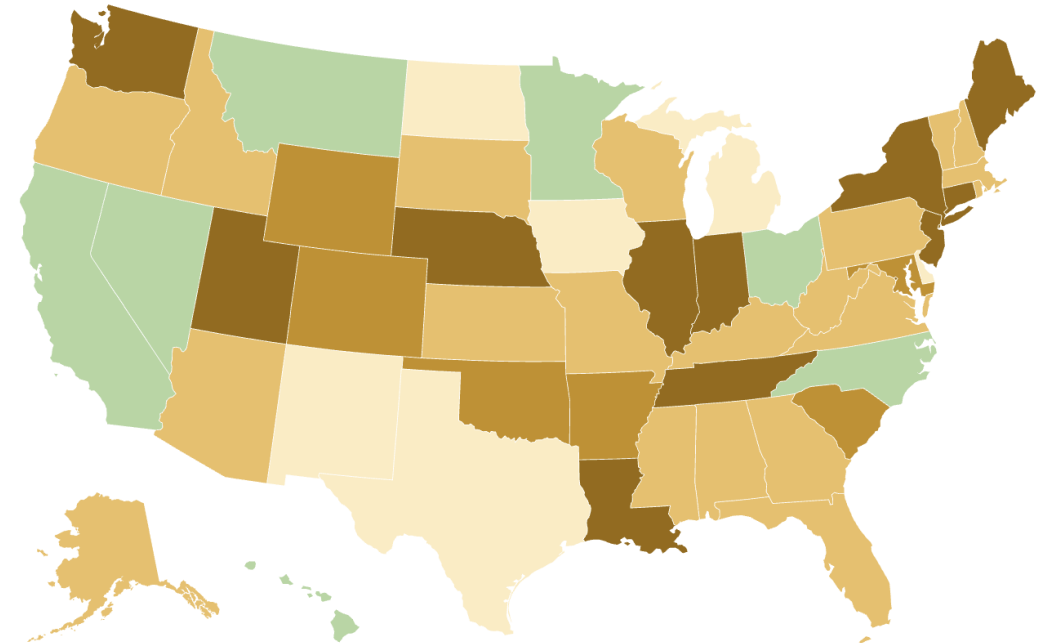
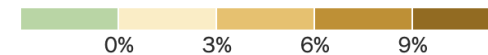
**The Washington Post**  
*Democracy Dies in Darkness*

## The AI explosion means millions are paying more for electricity

The data centers required for Big Tech are driving up electricity demand — and prices.

July 27, 2025

Percentage change in the cost of a kilowatt-hour



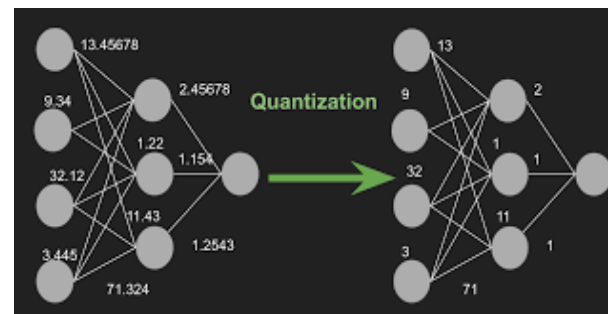
Change in price is from April 2024 to April 2025

Source: [Energy Information Administration](#)

PETER WHORISKEY / THE WASHINGTON POST

# Green AI Technologies

- **Data** efficiency:
  - Data distillation
  - Dimension reduction
  - Curriculum learning
- **Training** efficiency:
  - Few-shot learning
  - Parameter-efficient fine-tuning (PEFT)
- **Model** efficiency:
  - Quantization
  - Pruning
  - **Decomposition**



Quantization

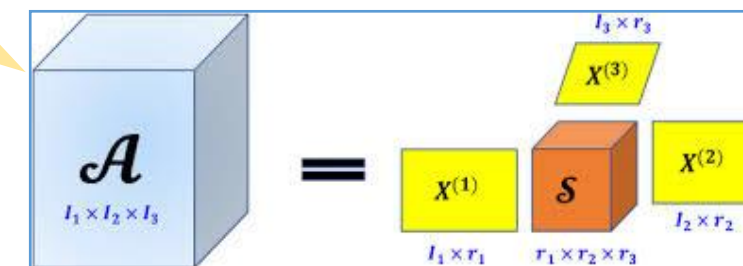


Green AI  
Efficient Model



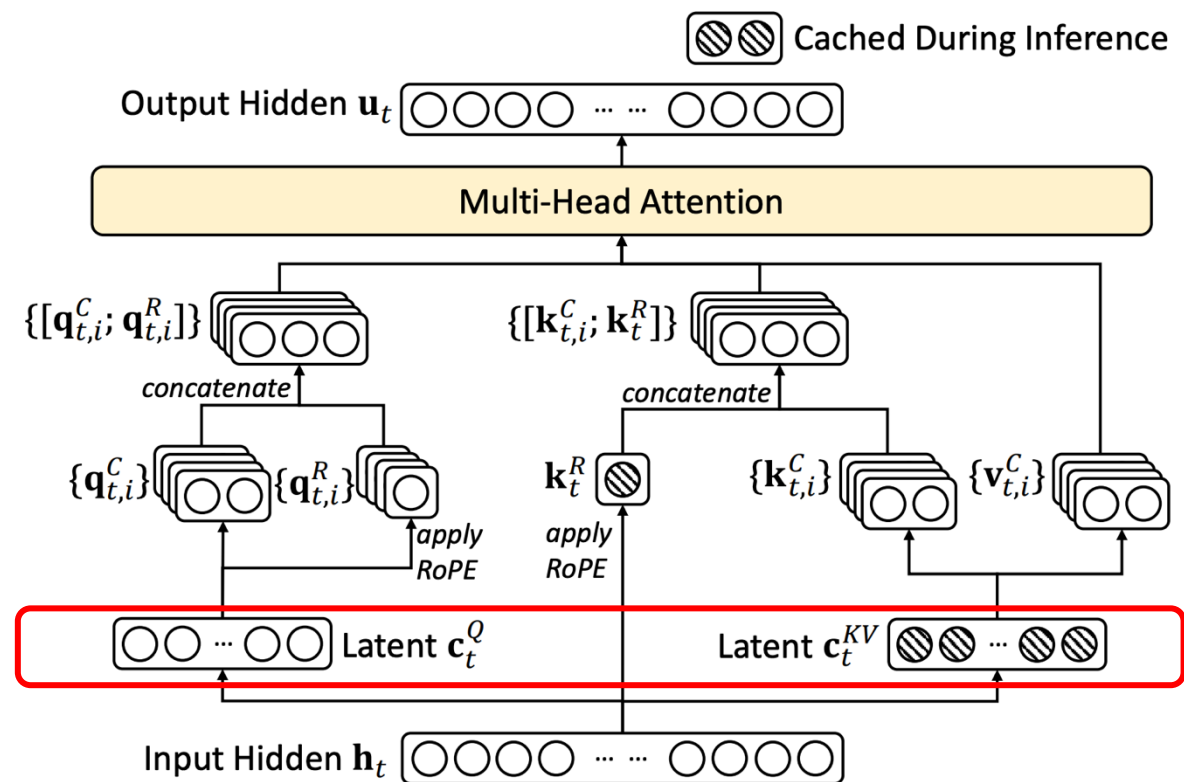
Pruning

Decomposition



- We developed a solution to globally compress multi-head attention (MHA) into multi-head latent attention (MLA)
- MLA was introduced in **DeepSeek-V3** to improve efficiency: KV cache
- How to convert any LLMs into DeepSeek-like LLMs efficiently?
  - 1) Preconditioner; 2) Junction; 3) Joint tensor decomposition

## MLA in DeepSeek-V3



**QKV Low-Dimensional Projection**

Q: 7168  $\rightarrow$  1536

KV: 7168  $\rightarrow$  512



# 1. Activation-Aware Rank Reduction

- How to compress pre-trained LLMs without fine-tuning?
- Adaptive SVD (ASVD) [Yuan24] compresses weights in a locally optimal manner
  - Activation statistics is compensated by preconditioning matrix
  - Calibration tokens are used to compute activation statistics (similar to AWQ/GPTQ)

Plain SVD:

$$\mathcal{L}_0 = \|W - \hat{W}\|^2 = \|W - BA\|^2$$



ASVD:

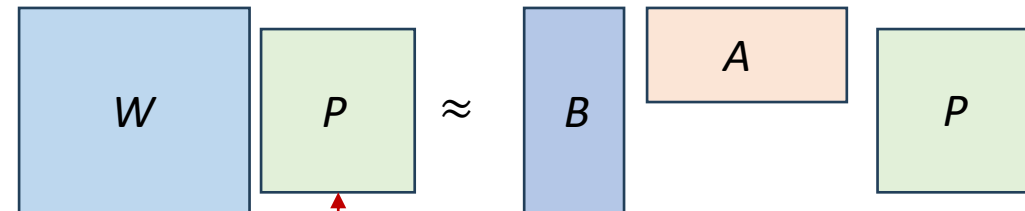
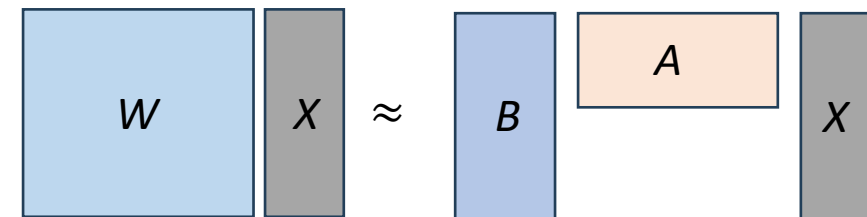
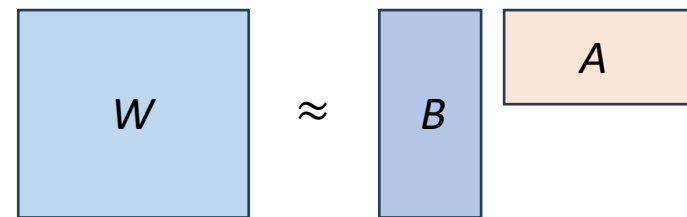
$$\mathcal{L}_1 = \mathbb{E}_X \|WX - \hat{W}X\|^2 = \mathbb{E}_X \|WX - BAX\|^2$$

$$= \text{tr}[(W - BA)\mathbb{E}_X[XX^\top](W - BA)^\top]$$

$$= \|(W - BA)C^{\frac{1}{2}}\|^2 = \|WC^{\frac{1}{2}} - BAC^{\frac{1}{2}}\|^2$$

$$BAP = \text{svd}_r[W \overset{\text{Preconditioner}}{P}]$$

Preconditioner



# Preconditioner

- Various preconditioners are introduced for model pruning, quantization, etc.
  - Original ASVD used diagonal L1-norm
  - We theoretically derived that root-covariance is optimal

| Preconditioner $P$      | Expression   | Reference            |
|-------------------------|--|----------------------|
| Identity                | $I$  | Plain SVD            |
| Diagonal Hessian        | $\text{diag}[(\mathbf{X}\mathbf{X}^\top + \lambda I)^{-1}]^{\frac{-1}{2}}$                   | OBS; GPTQ; SparseGPT |
| Diagonal $\ell_1$ -norm | $\text{diag}[\sum_j  \mathbf{X}_{1,j} , \dots, \sum_j  \mathbf{X}_{d,j} ]^\alpha / n^\alpha$ | ASVD; AWQ            |
| Diagonal $\ell_2$ -norm | $\text{diag}[\mathbf{X}\mathbf{X}^\top]^{\frac{1}{2}}$                                       | Wanda                |
| Covariance              | $\mathbf{X}\mathbf{X}^\top + \lambda I$  | CorDA                |
| Root-Covariance         | $(\mathbf{X}\mathbf{X}^\top + \lambda I)^{\frac{1}{2}}$                                      | LatentLLM (Ours)     |

**Table:** Variants of pre-conditioning matrices  $P$  for activation-aware distillation.



## 2. Junction Matrix

- There is no unique decomposition to minimize the error
  - Any arbitrary full-rank junction matrix has no impact in performance
  - There are infinite choices to map SVD towards B and A

$$USV = \text{svd}_r[WP]$$



$$BAP = \text{svd}_r[WP]$$

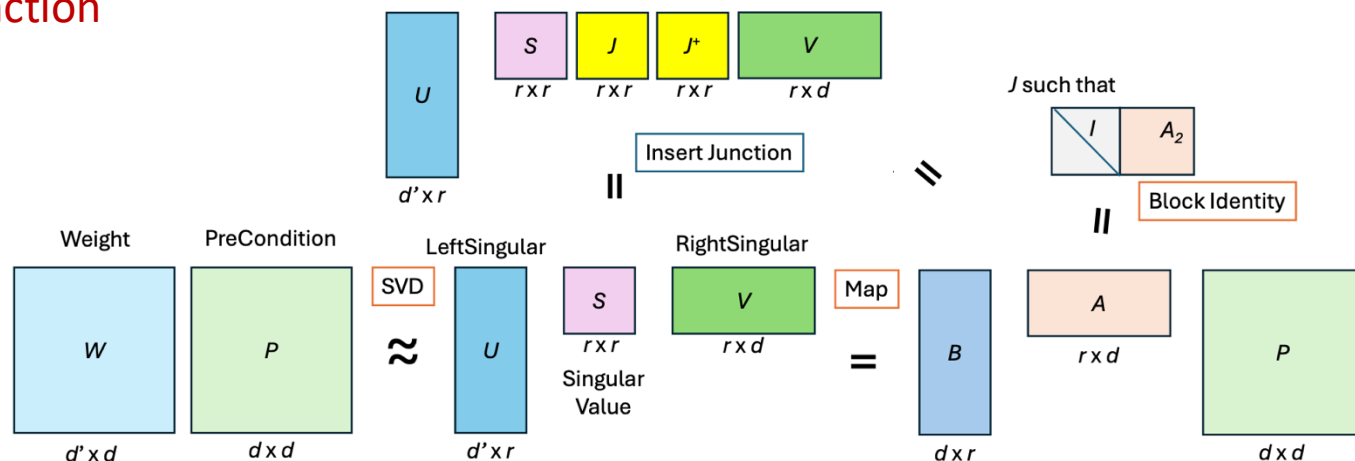
General solution:



$$B = USJ, \\ A = J^+VP^+,$$

Junction

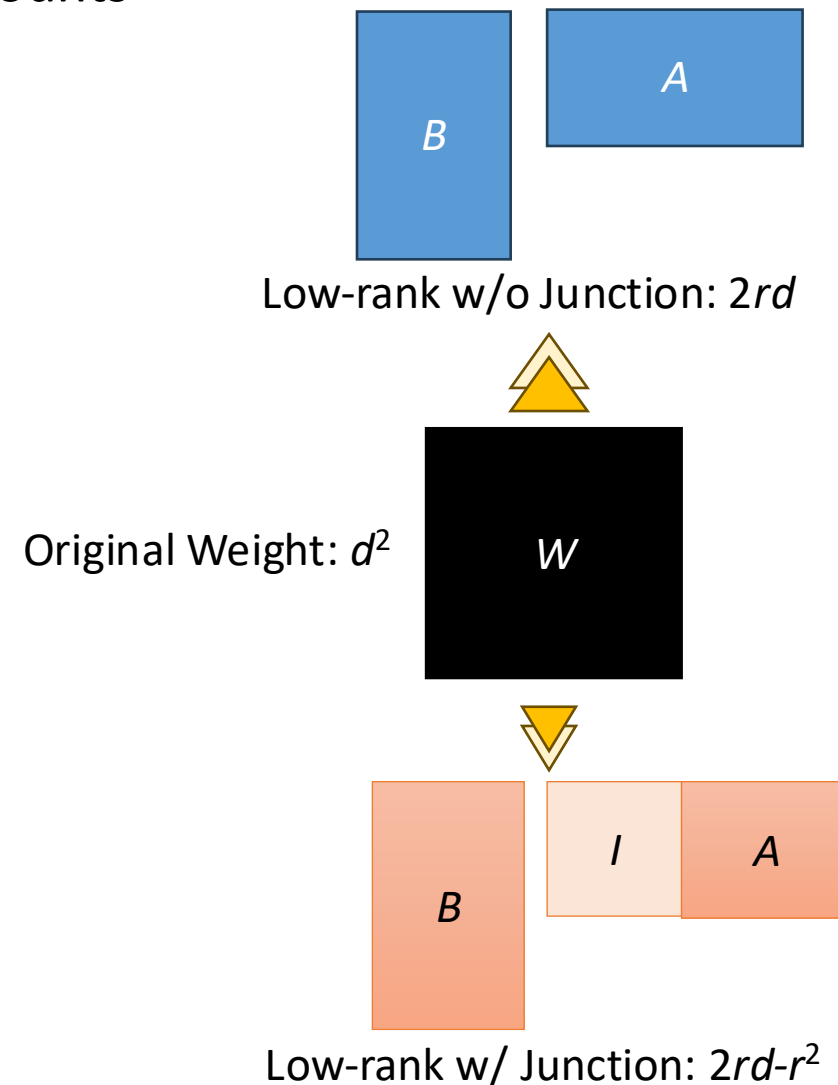
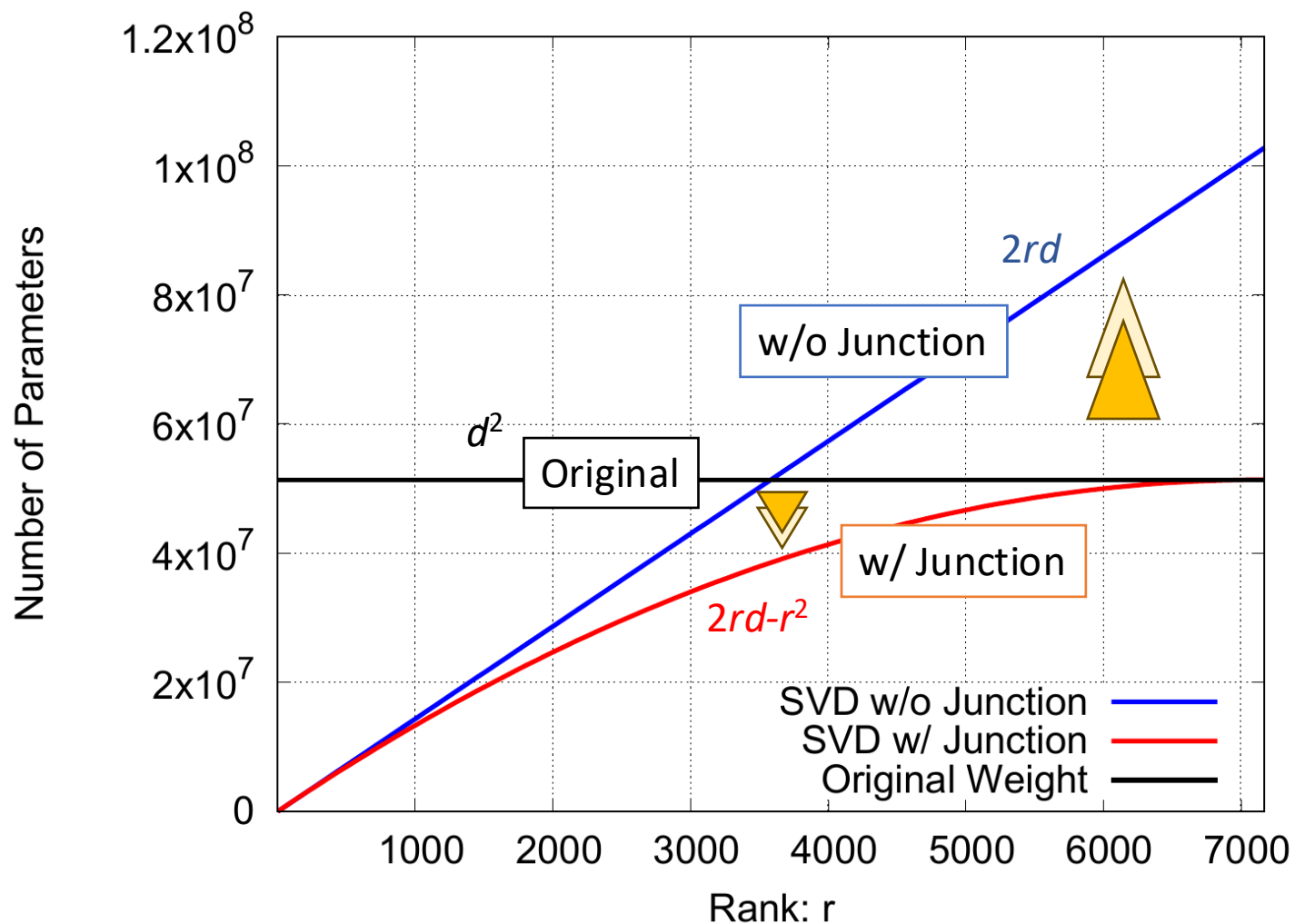
- Left singular:  $J = I$ ;
- Right singular:  $J = S^+$ ;
- Symmetry singular:  $J = [S^{\frac{1}{2}}]^+$ .
- Left block identity:  $J = [US]_{:r}^+$
- Right block identity:  $J = [V]_{:r}$



Total FLOPs/memory can be reduced

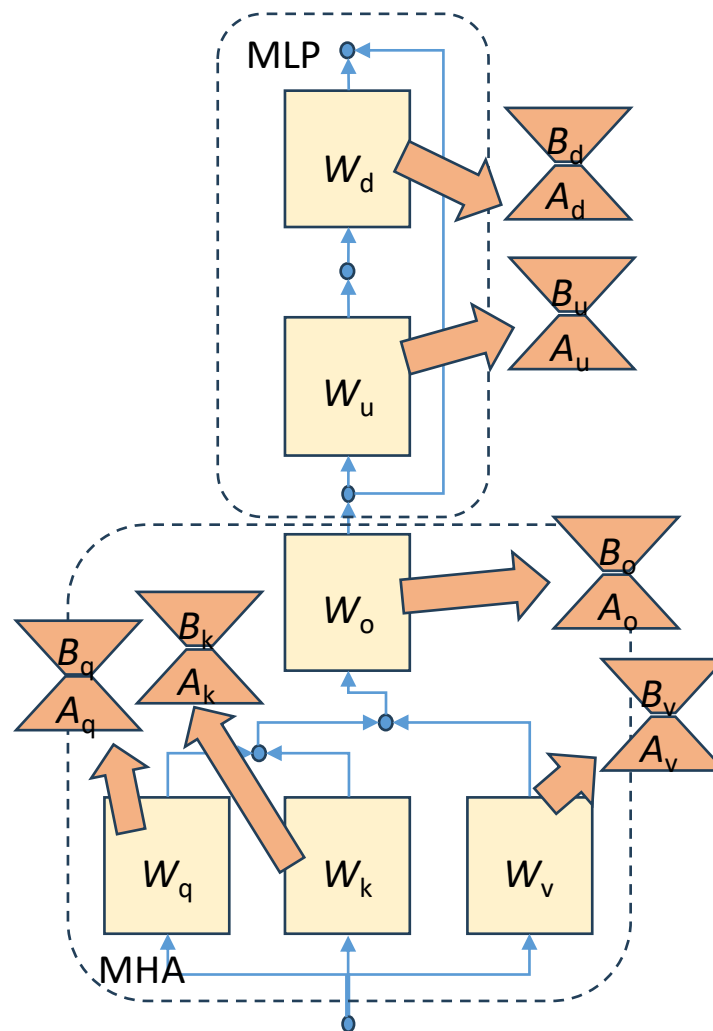
# Junction Matrix Impact

- SVD with block-identity junction can reduce the total number of parameters
  - SVD without junction can exceed the original parameter counts

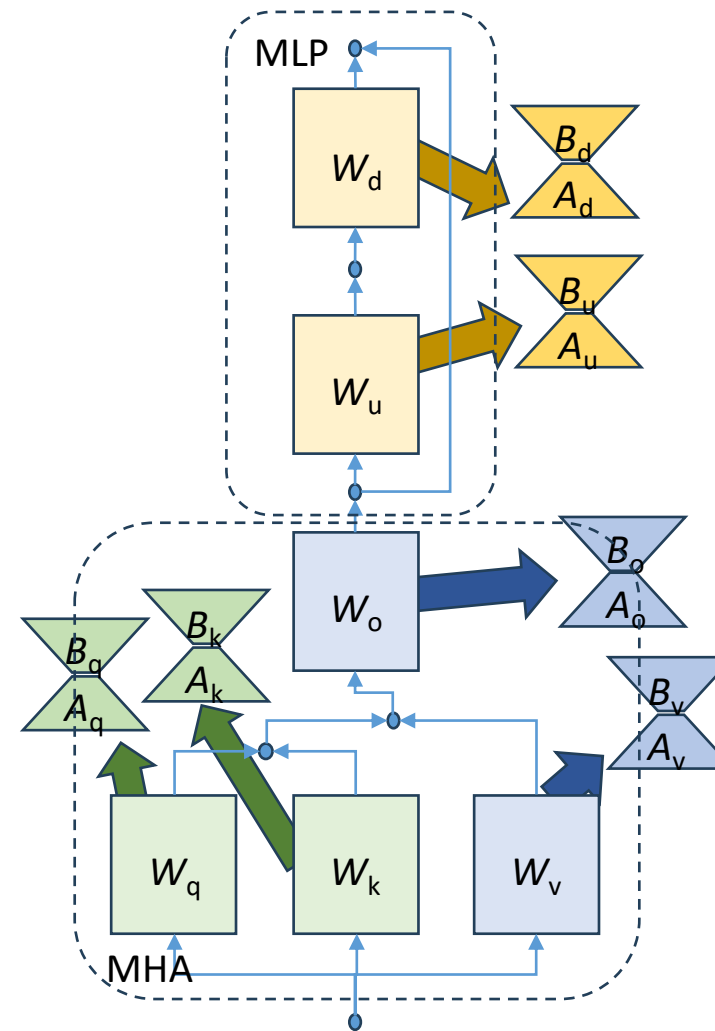


### 3. Attention-Aware Joint Rank Reduction

- We propose to compress multiple weights jointly
  - Joint QK compression
  - Joint VO compression
  - Joint UD compression



(a) LLM Local Tensor Compression



(b) LLM Joint Tensor Compression

# Joint QK Compression: High-Order Tensor Decomposition

- Attention map error minimization:

$$\mathcal{L}_2 = \sum_{i=1}^h \|M_i - \hat{M}_i\|^2,$$

$$= \sum_{i=1}^h \left\| \underbrace{C^{\frac{1}{2}} W_{q,i}^\top W_{k,i} C^{\frac{1}{2}}}_{G_i \in \mathbb{R}^{d \times d}} - \underbrace{C^{\frac{1}{2}} A_q^\top}_{A_q'^\top} \underbrace{B_{q,i}^\top B_{k,i}}_{H_i \in \mathbb{R}^{r_q \times r_k}} \underbrace{A_k C^{\frac{1}{2}}}_{A_k'} \right\|^2$$

$$= \sum_{i=1}^h \|G_i - A_q'^\top H_i A_k'\|^2.$$

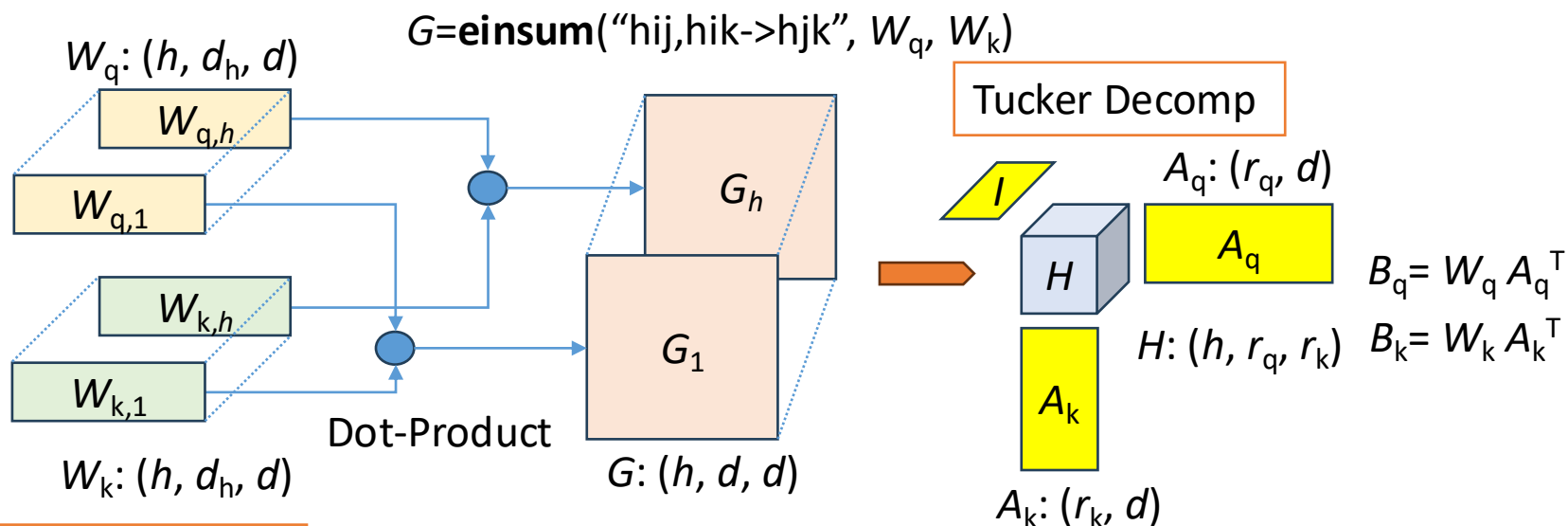
(14)

$$M_i = X^\top W_{q,i}^\top W_{k,i} X,$$

$$\hat{M}_i = X^\top A_q^\top B_{q,i}^\top B_{k,i} A_k X,$$



**Solution:**  
HO-SVD  
(Tucker Decomposition)



Joint VO compression has similar solution

# Joint UD Compression: Decoupled Loss Minimization

- We use decoupled loss minimization trick, similar to SparseLLM

$$\mathcal{L} = \|W_d Z' - \hat{W}_d \sigma(\hat{W}_u X)\|^2$$

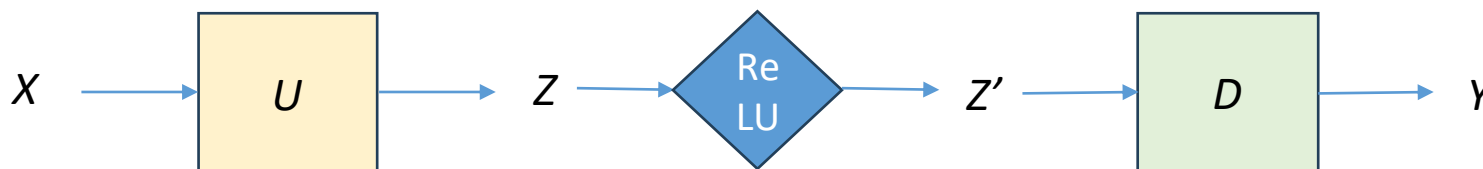


$$\mathcal{L}_4 = \alpha \|W_u X - Z\|^2 + \beta \|Z' - \sigma(Z)\|^2 + \gamma \|W_d Z' - Y\|^2,$$

$$\begin{aligned} Z_- &= W_u X, \\ Z_+ &= \frac{1}{\alpha + \beta} (\alpha Z_- + \beta Z'), \end{aligned}$$

$$Z' = (\gamma W_d^\top W_d + \beta I)^+ (\beta \sigma(Z) + \gamma W_d^\top Y)$$

$$\begin{aligned} Z &= W_u X, \\ Z' &= \sigma(Z), \\ Y &= W_d Z', \end{aligned}$$



Alternating optimization of auxiliary values  $Z/Z'$  and weight rank reduction

# Experiments: Complexity/Memory/Throughput Analysis

- FLOPs/MACs can decrease almost linearly
- Throughput improves almost quadratically
- KV cache reduces significantly

facebook  
/opt-6.7b

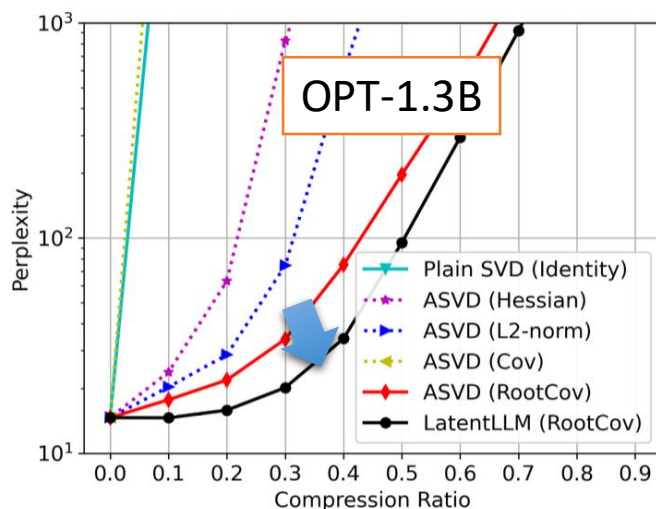
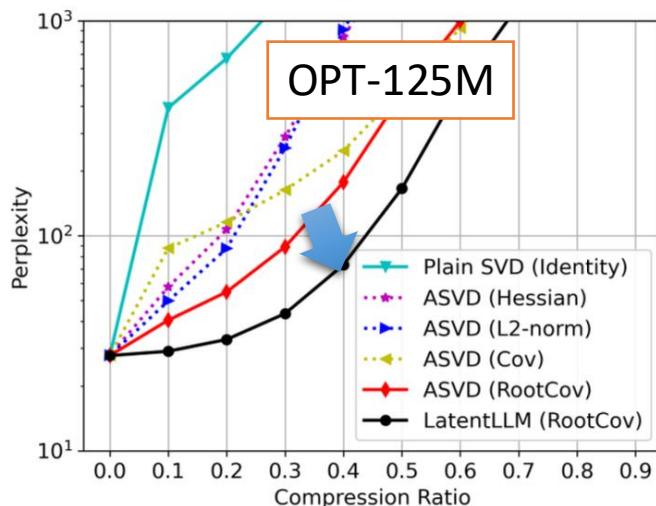
| Compression | FLOPs  |                        | MACs  |                        | Parameters (byte) |                        | Speed (token/sec) | KV Cache (byte)        |       |                        |
|-------------|--------|------------------------|-------|------------------------|-------------------|------------------------|-------------------|------------------------|-------|------------------------|
| 0%          | 109.0T | <div><div></div></div> | 54.5T | <div><div></div></div> | 13.32G            | <div><div></div></div> | 6.64k             | <div><div></div></div> | 5.37G | <div><div></div></div> |
| 10%         | 98.1T  | <div><div></div></div> | 49.1T | <div><div></div></div> | 12.40G            | <div><div></div></div> | 6.64k             | <div><div></div></div> | 3.67G | <div><div></div></div> |
| 20%         | 87.2T  | <div><div></div></div> | 43.6T | <div><div></div></div> | 11.06G            | <div><div></div></div> | 7.14k             | <div><div></div></div> | 2.97G | <div><div></div></div> |
| 30%         | 76.3T  | <div><div></div></div> | 38.2T | <div><div></div></div> | 9.74G             | <div><div></div></div> | 7.34k             | <div><div></div></div> | 2.43G | <div><div></div></div> |
| 40%         | 65.4T  | <div><div></div></div> | 32.7T | <div><div></div></div> | 8.40G             | <div><div></div></div> | 8.92k             | <div><div></div></div> | 1.98G | <div><div></div></div> |
| 50%         | 54.5T  | <div><div></div></div> | 27.3T | <div><div></div></div> | 7.08G             | <div><div></div></div> | 9.54k             | <div><div></div></div> | 1.57G | <div><div></div></div> |
| 60%         | 43.6T  | <div><div></div></div> | 21.8T | <div><div></div></div> | 5.74G             | <div><div></div></div> | 11.55k            | <div><div></div></div> | 1.21G | <div><div></div></div> |
| 70%         | 32.7T  | <div><div></div></div> | 16.4T | <div><div></div></div> | 4.42G             | <div><div></div></div> | 13.14k            | <div><div></div></div> | 0.88G | <div><div></div></div> |
| 80%         | 21.8T  | <div><div></div></div> | 10.9T | <div><div></div></div> | 3.08G             | <div><div></div></div> | 16.20k            | <div><div></div></div> | 0.57G | <div><div></div></div> |
| 90%         | 10.9T  | <div><div></div></div> | 5.4T  | <div><div></div></div> | 1.76G             | <div><div></div></div> | 19.82k            | <div><div></div></div> | 0.28G | <div><div></div></div> |

LLM model: OPT-6.7B. 4-batch, 1024 tokens, torch.compile("max-autotune") on NVIDIA A40 GPU



# Experiments: LLM Benchmark

- Wikitext-2 perplexity over LLM model sizes and variants



facebook  
/opt-6.7b

Qwen3

OPT-6.7B (Perplexity: 10.9)

| Compression                | 10%          | 20%         | 30%         | 40%         | 50%         |
|----------------------------|--------------|-------------|-------------|-------------|-------------|
| Plain SVD (Identity)       | 14839.0      | 67517.7     | 123286.4    | 27304.0     | 12780.0     |
| ASVD (Hessian)             | 14.3         | 17.3        | 26.0        | 73.3        | 940.1       |
| ASVD ( $\ell_2$ -norm)     | 12.6         | 14.6        | 18.7        | 30.6        | 146.4       |
| ASVD (Cov)                 | 9111.6       | 9842.6      | 11848.0     | 8514.7      | 8926.9      |
| ASVD (RootCov)             | 11.8         | 13.5        | 17.0        | 27.2        | 56.71       |
| <b>LatentLLM (RootCov)</b> | <b>*10.7</b> | <b>11.5</b> | <b>13.5</b> | <b>18.0</b> | <b>33.3</b> |

Qwen3-8B (Perplexity: 9.2)

|                            |             |             |             |             |              |
|----------------------------|-------------|-------------|-------------|-------------|--------------|
| Plain SVD (Identity)       | 2.4e5       | 9.0e6       | 2.8e7       | 5.3e7       | 4.3e8        |
| ASVD (Hessian)             | 33.6        | 90.8        | 1250.8      | 5324.6      | 15933.7      |
| ASVD ( $\ell_2$ -norm)     | 18.8        | 26.0        | 40.6        | 98.6        | 382.0        |
| ASVD (Cov)                 | 1.3e5       | 1.2e5       | 8.3e4       | 6.1e4       | 39455.9      |
| ASVD (RootCov)             | 16.7        | 26.0        | 49.3        | 119.2       | 303.3        |
| <b>LatentLLM (RootCov)</b> | <b>11.8</b> | <b>14.2</b> | <b>22.4</b> | <b>53.9</b> | <b>166.3</b> |

# Experiments: VLM Benchmark (ScienceQA)

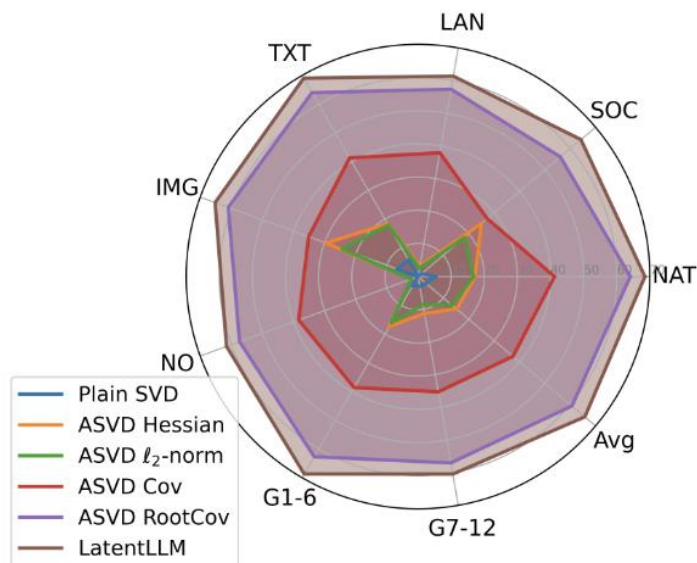
- LLaVA-7B model for visual reasoning benchmark: ScienceQA

LLaVA

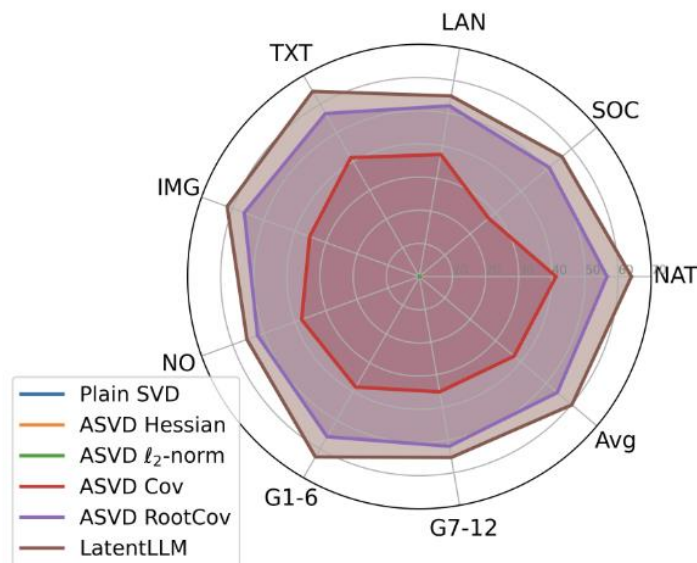
| Compression            | 10%          | 20%          | 30%          | 40%          | 50%          |
|------------------------|--------------|--------------|--------------|--------------|--------------|
| Plain SVD (Identity)   | 3.18         | 0.09         | 0.07         | 0.00         | 0.00         |
| ASVD (Hessian)         | 15.21        | 2.62         | 0.00         | 0.17         | 0.00         |
| ASVD ( $\ell_2$ -norm) | 13.37        | 0.40         | 0.05         | 0.07         | 0.00         |
| ASVD (Cov)             | 37.42        | 37.42        | 37.33        | 37.02        | 36.95        |
| ASVD (RootCov)         | 60.67        | 57.53        | 54.37        | 52.23        | 49.30        |
| LatentLLM (RootCov)    | <b>65.76</b> | <b>63.85</b> | <b>60.13</b> | <b>54.59</b> | <b>52.25</b> |

|  |   |  |   |   |
|--|---|--|---|---|
| <b>Biology</b><br>Genes to traits<br>Classification<br>Adaptations<br>Traits and heredity<br>Ecosystems<br>Classification<br>Scientific names<br>Heredity<br>Ecological interactions<br>Cells<br>Plants<br>Animals<br>Plant reproduction | <b>Physics</b><br>Materials<br>Magnets<br>Velocity and forces<br>Force and motion<br>Particle motion and energy<br>Heat and thermal energy<br>States of matter<br>Kinetic and potential energy<br>Mixture                                 | <b>Geography</b><br>State capitals<br>Geography<br>Maps<br>Oceania: geography<br>Physical Geography<br>The Americas: geography<br>Oceans and continents<br>Cities<br>States  | <b>History</b><br>Colonial America<br>English colonies in North America<br>The American Revolution<br><b>World History</b><br>Greece<br>Ancient Mesopotamia<br>World religions<br>American history<br>Medieval Asia     | <b>Civics</b><br>Social skills<br>Government<br>The Constitution<br><b>Economics</b><br>Basic economic principles<br>Supply and demand<br>Banking and finance<br><b>Global Studies</b><br>Society and environment |
| <b>Earth Science</b><br>Weather and climate<br>Rocks and minerals<br>Astronomy<br>Fossils<br>Earth events<br>Plate tectonics   | <b>Chemistry</b><br>Solutions<br>Physical and chemical change<br>Atoms and molecules<br>Chemical reactions<br><b>Engineering</b><br>Designing experiments<br>Engineering practices<br><b>Units and Measurement</b><br>Weather and climate | <b>Writing Strategies</b><br>Supporting arguments<br>Sentences, fragments, and run-ons<br>Word usage and nuance<br>Creative techniques<br>Audience, purpose, and tone<br>Pronouns and antecedents<br>Persuasive strategies<br>Editing and revising<br>Visual elements<br>Opinion writing | <b>Vocabulary</b><br>Categories<br>Shades of meaning<br>Comprehension strategies<br>Context clues<br><b>Grammar</b><br>Sentences and fragments<br>Phrases and clauses<br><b>Figurative Language</b><br>Literary devices | <b>Verbs</b><br>Verb tense<br><b>Capitalization</b><br>Formatting<br><b>Punctuation</b><br>Fragments<br><b>Phonology</b><br>Rhyming<br><b>Reference</b><br>Research skills  |

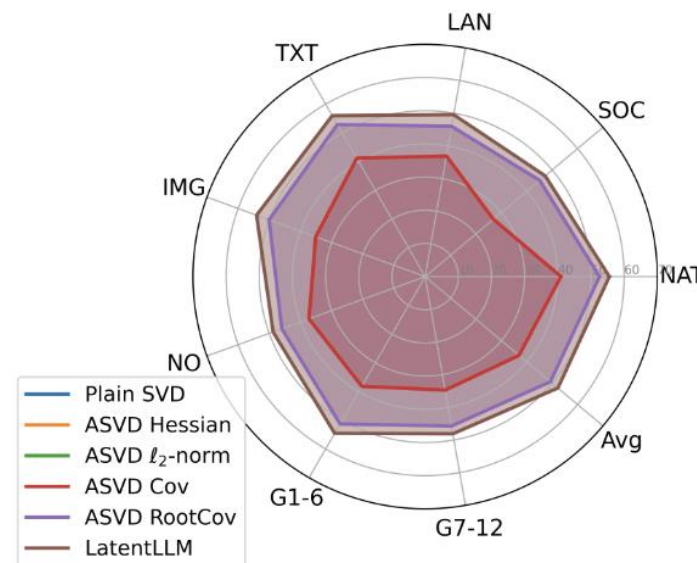
QA for Natural, Social, & Language Science



(a) 10% Compression



(b) 30% Compression



(c) 50% Compression

# Experiments: VLM Benchmark (TextVQA)

- LLaVA-7B/Qwen2.5-VL-7B/3B models for visual reasoning benchmark: TextVQA

LLaVA

LLaVA-7B: Uncompressed Acc 61.32

| Compression                | 10%          | 20%          | 30%          | 40%          | 50%          |
|----------------------------|--------------|--------------|--------------|--------------|--------------|
| Plain SVD (identity)       | 2.36         | 0.48         | 0.35         | 0.34         | 0.36         |
| ASVD (Hessian)             | 23.88        | 9.60         | 1.24         | 0.21         | 0.31         |
| ASVD ( $\ell_2$ -norm)     | 24.41        | 9.53         | 2.77         | 0.82         | 0.75         |
| ASVD (Cov)                 | 0.38         | 0.36         | 0.40         | 0.33         | 0.35         |
| ASVD (RootCov)             | 52.51        | 49.91        | 45.53        | 38.47        | 27.36        |
| <b>LatentLLM (RootCov)</b> | <b>60.06</b> | <b>57.65</b> | <b>52.63</b> | <b>46.90</b> | <b>35.94</b> |

Qwen2.5-VL-7B: Uncompressed Acc 82.11

|                            |              |              |              |              |              |
|----------------------------|--------------|--------------|--------------|--------------|--------------|
| Plain SVD (identity)       | 0.02         | 0.47         | 0.32         | 0.05         | 0.11         |
| ASVD (Hessian)             | 58.76        | 7.03         | 0.23         | 0.45         | 0.41         |
| ASVD ( $\ell_2$ -norm)     | 77.84        | 73.92        | 57.13        | 18.79        | 0.41         |
| ASVD (Cov)                 | 0.41         | 0.41         | 0.41         | 0.41         | 0.41         |
| ASVD (RootCov)             | 79.46        | 74.76        | 66.31        | 51.80        | 34.91        |
| <b>LatentLLM (RootCov)</b> | <b>80.85</b> | <b>79.30</b> | <b>73.90</b> | <b>62.11</b> | <b>42.53</b> |

Qwen2.5-VL-3B: Uncompressed Acc 78.17

|                            |              |              |              |              |              |
|----------------------------|--------------|--------------|--------------|--------------|--------------|
| Plain SVD (identity)       | 0.01         | 0.08         | 0.09         | 0.09         | 0.01         |
| ASVD (Hessian)             | 0.14         | 0.31         | 0.31         | 0.31         | 0.34         |
| ASVD ( $\ell_2$ -norm)     | 44.23        | 0.14         | 0.00         | 0.41         | 0.37         |
| ASVD (Cov)                 | 0.41         | 0.41         | 0.41         | 0.41         | 0.41         |
| ASVD (RootCov)             | 73.78        | 67.30        | 54.20        | 33.93        | 13.99        |
| <b>LatentLLM (RootCov)</b> | <b>76.44</b> | <b>74.29</b> | <b>64.28</b> | <b>45.80</b> | <b>19.67</b> |

ASVD without RootCov:  
Nearly 0% Acc

LatentLLM:  
Best performance consistently



What does it say near the star on the tail of the plane?

Ground Truth

jet

Prediction

nothing

Table: Accuracy in percent ( $\uparrow$ ) on TextVQA dataset for compressed LLaVA-7B and Qwen2.5-VL-7B/3B.



# Summary

- We introduced a new compression method **LatentLLM** for green AI
  - We discussed various preconditioning matrices, validating the optimality of root-covariance
  - We proposed to use junction matrix, improving the efficiency with block identity form
  - We derived a mathematically optimal joint tensor decomposition method, minimizing attention loss
  - LatentLLM can convert MHA to MLA like DeepSeek, without the need of re-training
  - We showed significant KV cache reduction and throughput improvement
  - We validated the superiority of LatentLLM over state-of-the-art rank reduction methods for various LLM/VLM models and benchmarks
- We plan:
  - to integrate pruning and quantization
  - to incorporate with fine-tuning
  - to apply to edge AI platforms
- Please contact us ([koike@merl.com](mailto:koike@merl.com)) for more discussions



