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LatentLLM: Activation-Aware Transform to Multi-Head Latent Attention

Toshiaki Koike-Akino, Xiangyu Chen, Jing Liu, Ye Wang,
Pu (Perry) Wang, Matthew Brand

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MITSUBISHI ELECTRIC RESEARCH LABORATORIES (MERL)

Cambridge, Massachusetts, USA

<http://www.merl.com>

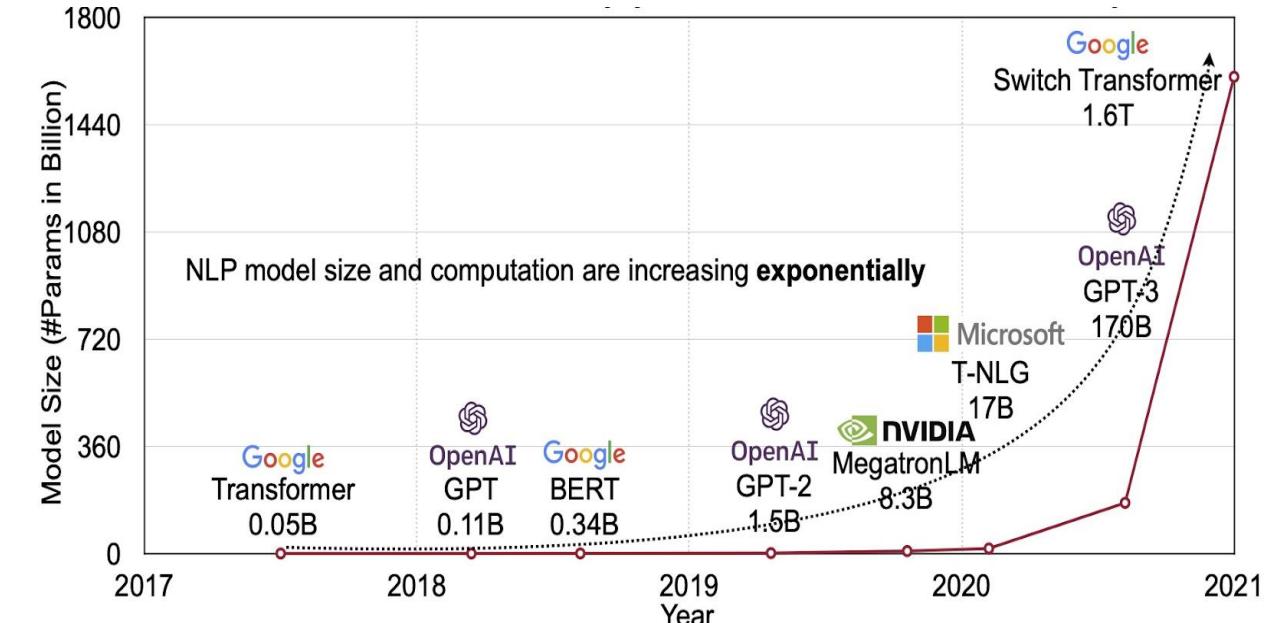
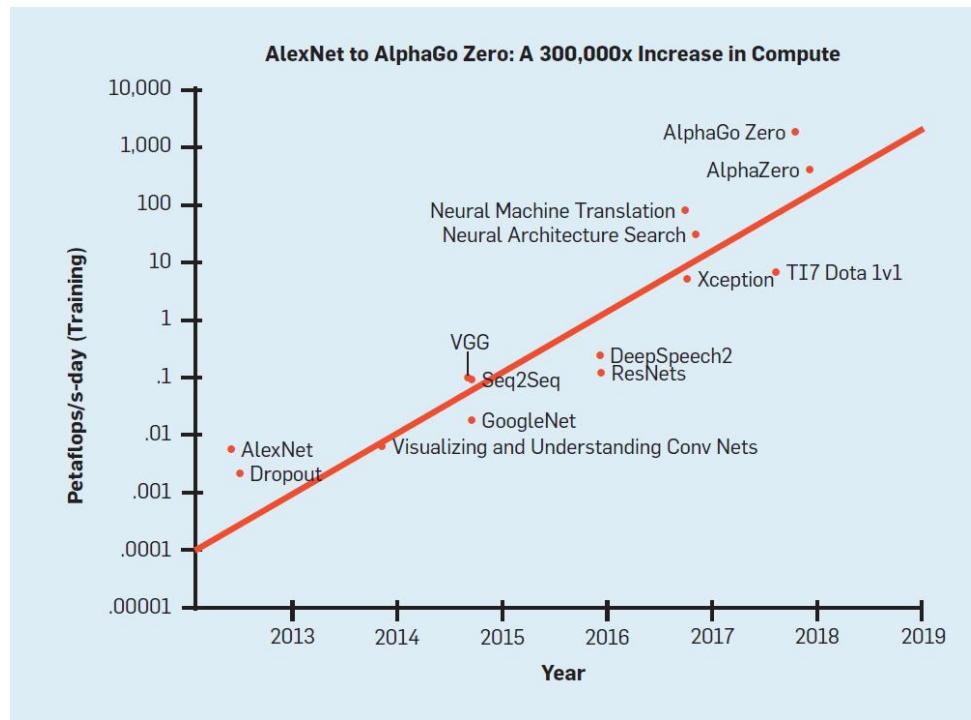
Agenda

- Green AI overview
- Model compression: **LatentLLM**
 - Preconditioning matrix
 - Junction matrix
 - Attention-aware joint tensor decomposition
- Benchmark experiments
- Summary



Social Challenge: Red AI

- R. Schwartz et al., “Green AI” 2020.
 - Training compute has increased exponentially: **10-fold annually**.
- Strubell et al. “Energy and policy considerations for deep learning in NLP” 2019.
 - Training a single NLP model requires **5-fold higher** carbon emission of *single car lifetime*.



The computation used to train deep learning models has increased 300,000x in six years: nearly 10x annually

Language model increases exponentially over years

Power Demand by AI Explosion

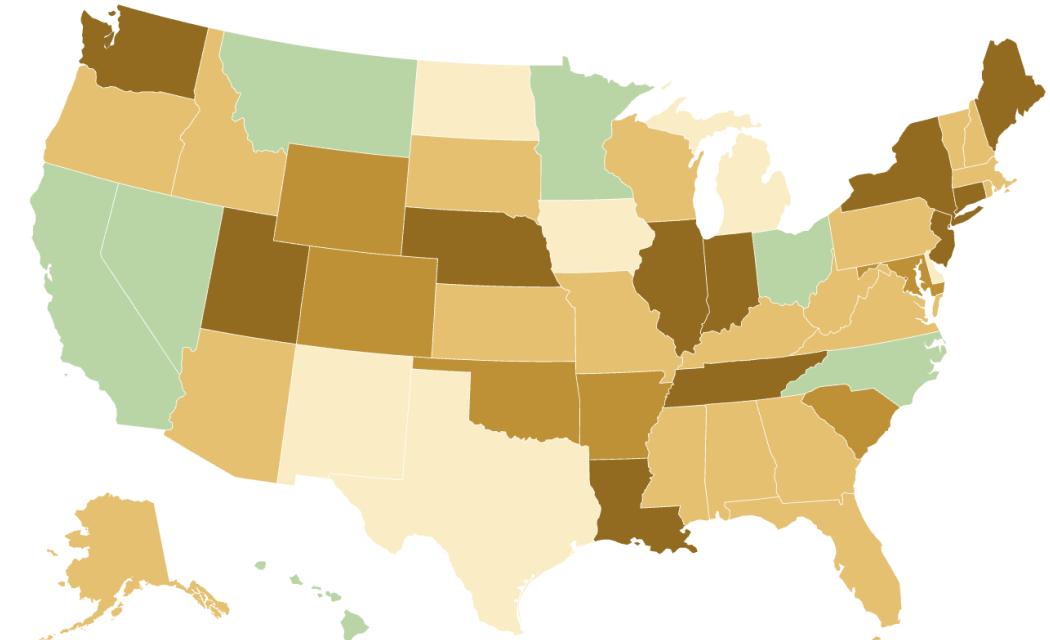
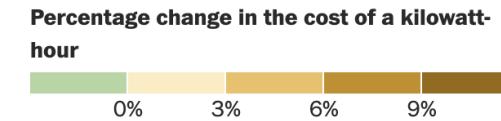
- High demand in electric power at data center driven by AI explosion, increasing bill
 - Electricity capacity prices jumped 833% in one regional auction
 - Some households saw \$27/month increases
 - All traced directly to data center electricity demand

The Washington Post
Democracy Dies in Darkness

The AI explosion means millions are paying more for electricity

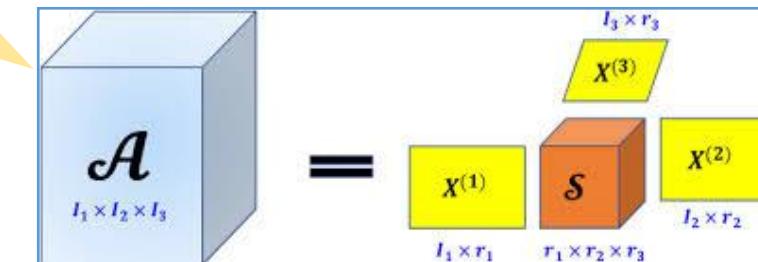
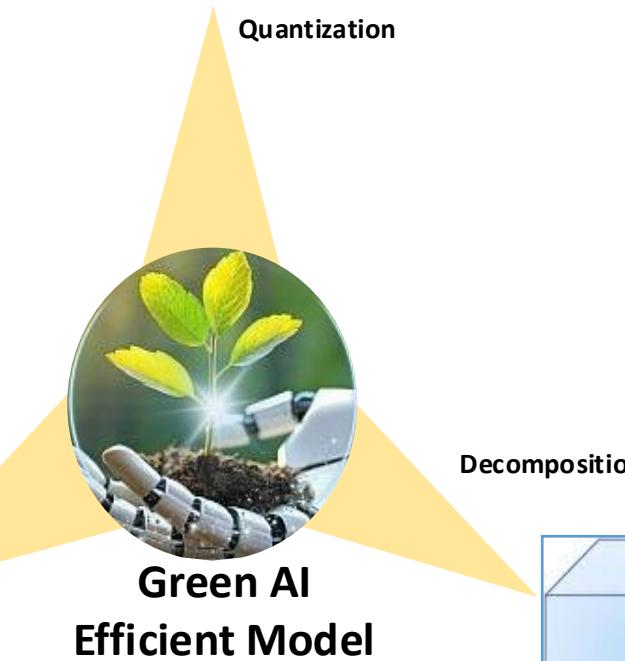
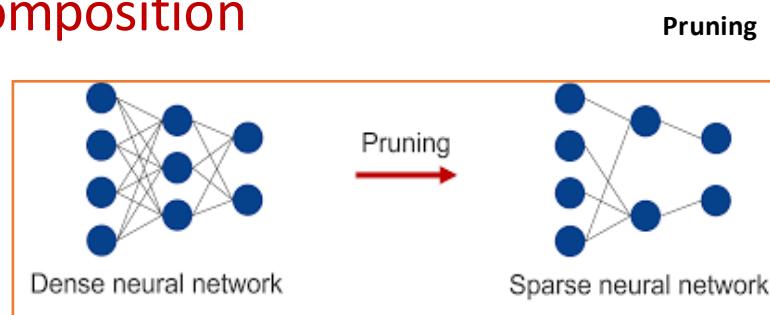
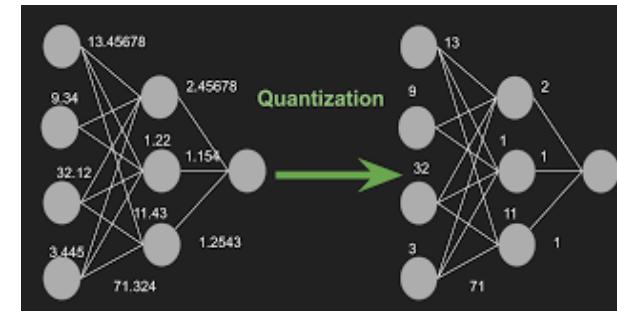
The data centers required for Big Tech are driving up electricity demand – and prices.

July 27, 2025



Green AI Technologies

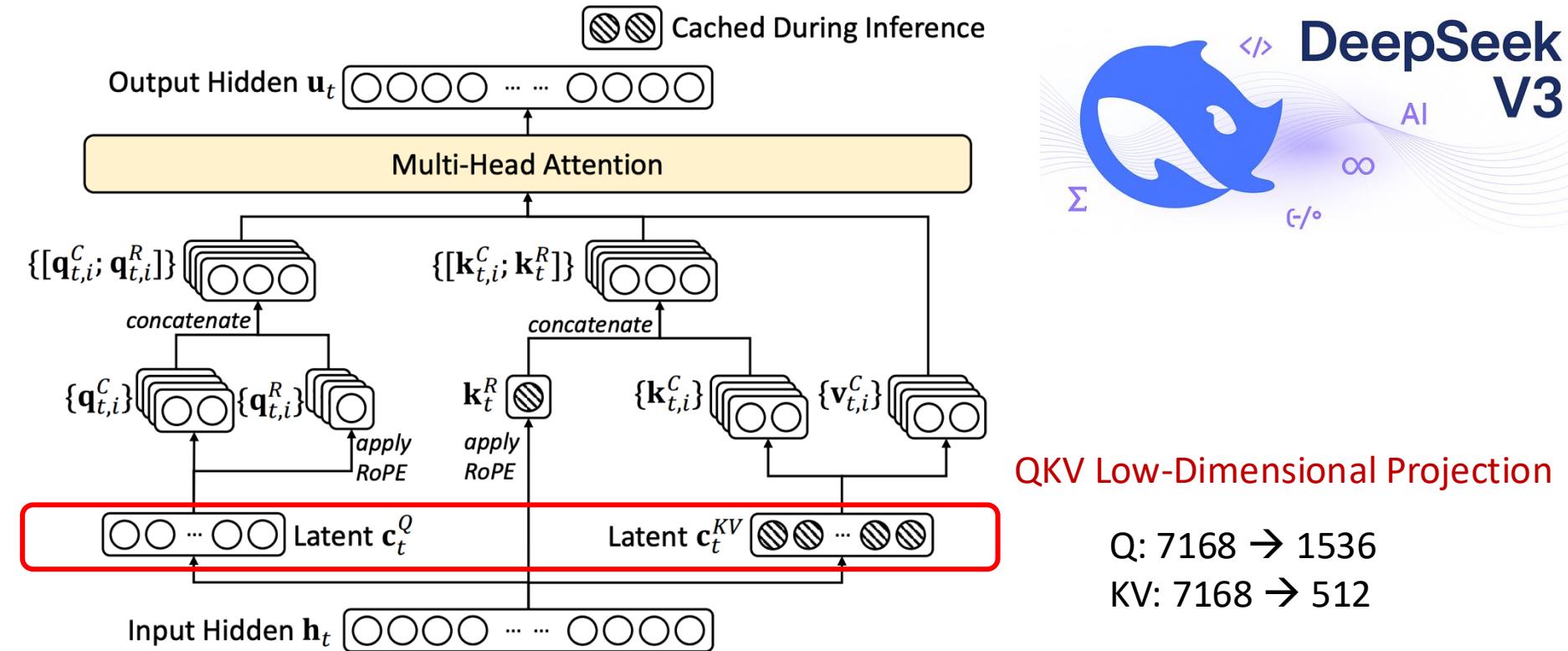
- ***Data*** efficiency:
 - Data distillation
 - Dimension reduction
 - Curriculum learning
- ***Training*** efficiency:
 - Few-shot learning
 - Parameter-efficient fine-tuning (PEFT)
- ***Model*** efficiency:
 - Quantization
 - Pruning
 - **Decomposition**



LatentLLM

- We developed a solution to globally compress multi-head attention (MHA) into multi-head latent attention (MLA)
- MLA was introduced in **DeepSeek-V3** to improve efficiency: KV cache
- **How to convert any LLMs into DeepSeek-like LLMs efficiently?**
 - 1) Preconditioner; 2) Junction; 3) Joint tensor decomposition

MLA in DeepSeek-V3



1. Activation-Aware Rank Reduction

- How to compress pre-trained LLMs without fine-tuning?
- Adaptive SVD (ASVD) [Yuan24] compresses weights in a locally optimal manner
 - Activation statistics is compensated by preconditioning matrix
 - Calibration tokens are used to compute activation statistics (similar to AWQ/GPTQ)

Plain SVD:

$$\mathcal{L}_0 = \|W - \hat{W}\|^2 = \|W - BA\|^2$$

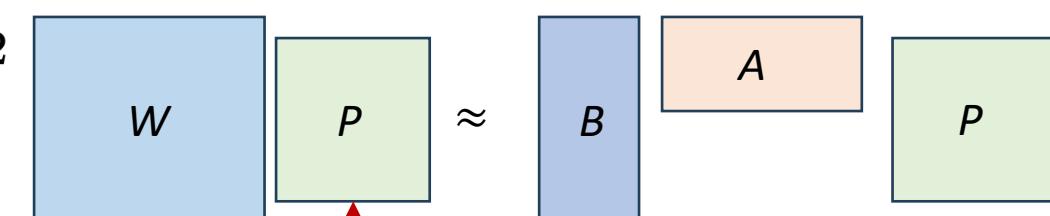
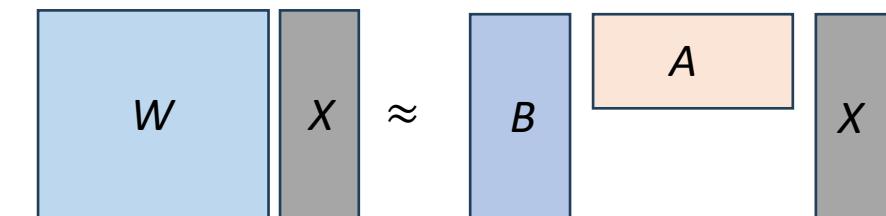
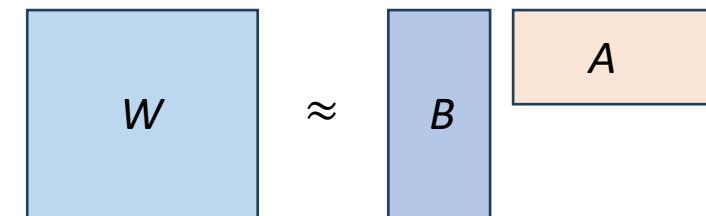


ASVD:

$$\begin{aligned} \mathcal{L}_1 &= \mathbb{E}_X \|WX - \hat{W}X\|^2 = \mathbb{E}_X \|WX - BAX\|^2 \\ &= \text{tr}[(W - BA)\mathbb{E}_X[XX^\top](W - BA)^\top] \\ &= \|(W - BA)C^{\frac{1}{2}}\|^2 = \|WC^{\frac{1}{2}} - BAC^{\frac{1}{2}}\|^2 \end{aligned}$$

$$BAP = \text{svd}_r[W P]$$

Preconditioner



Preconditioner

- Various preconditioners are introduced for model pruning, quantization, etc.
 - Original ASVD used diagonal L1-norm
 - We theoretically derived that root-covariance is optimal

Preconditioner P	Expression	Reference
Identity	I	Plain SVD
Diagonal Hessian	$\text{diag}[(\mathbf{X}\mathbf{X}^\top + \lambda I)^{-1}]^{\frac{1}{2}}$	OBS; GPTQ; SparseGPT
Diagonal ℓ_1 -norm	$\text{diag}\left[\sum_j \mathbf{X}_{1,j} , \dots, \sum_j \mathbf{X}_{d,j} \right]^\alpha / n^\alpha$	ASVD; AWQ
Diagonal ℓ_2 -norm	$\text{diag}[\mathbf{X}\mathbf{X}^\top]^{\frac{1}{2}}$	Wanda
Covariance	$\mathbf{X}\mathbf{X}^\top + \lambda I$	CorDA
Root-Covariance	$(\mathbf{X}\mathbf{X}^\top + \lambda I)^{\frac{1}{2}}$	LatentLLM (Ours)

Table: Variants of pre-conditioning matrices P for activation-aware distillation.

2. Junction Matrix

- There is no unique decomposition to minimize the error
 - Any arbitrary full-rank junction matrix has no impact in performance
 - There are infinite choices to map SVD towards B and A

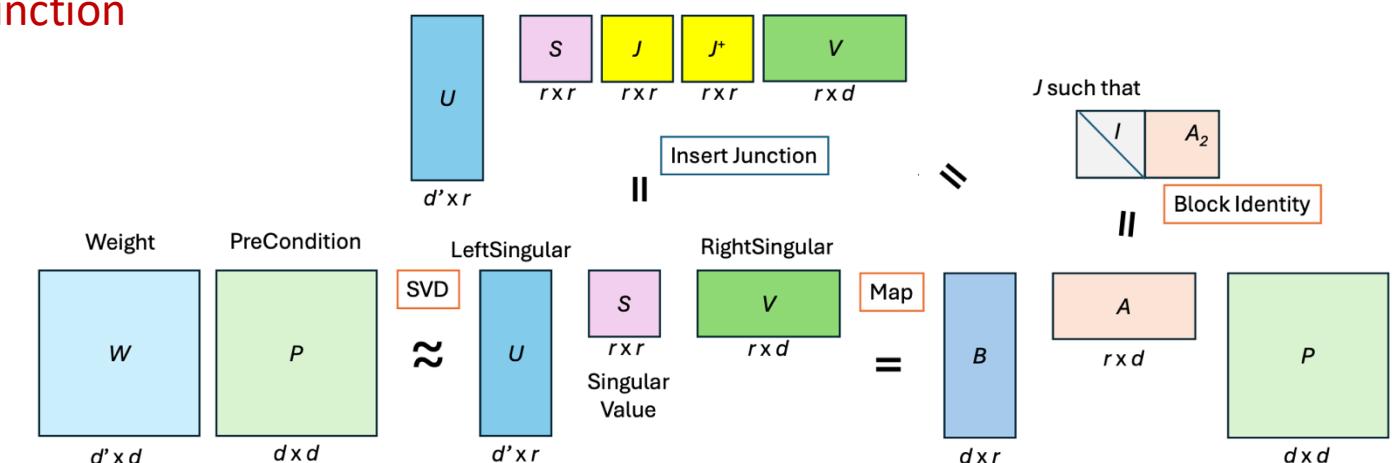
$$USV = \text{svd}_r[WP] \quad \Rightarrow \quad BAP = \text{svd}_r[WP]$$

General solution:

$$B = USJ, \quad A = J^+VP^+,$$

Junction

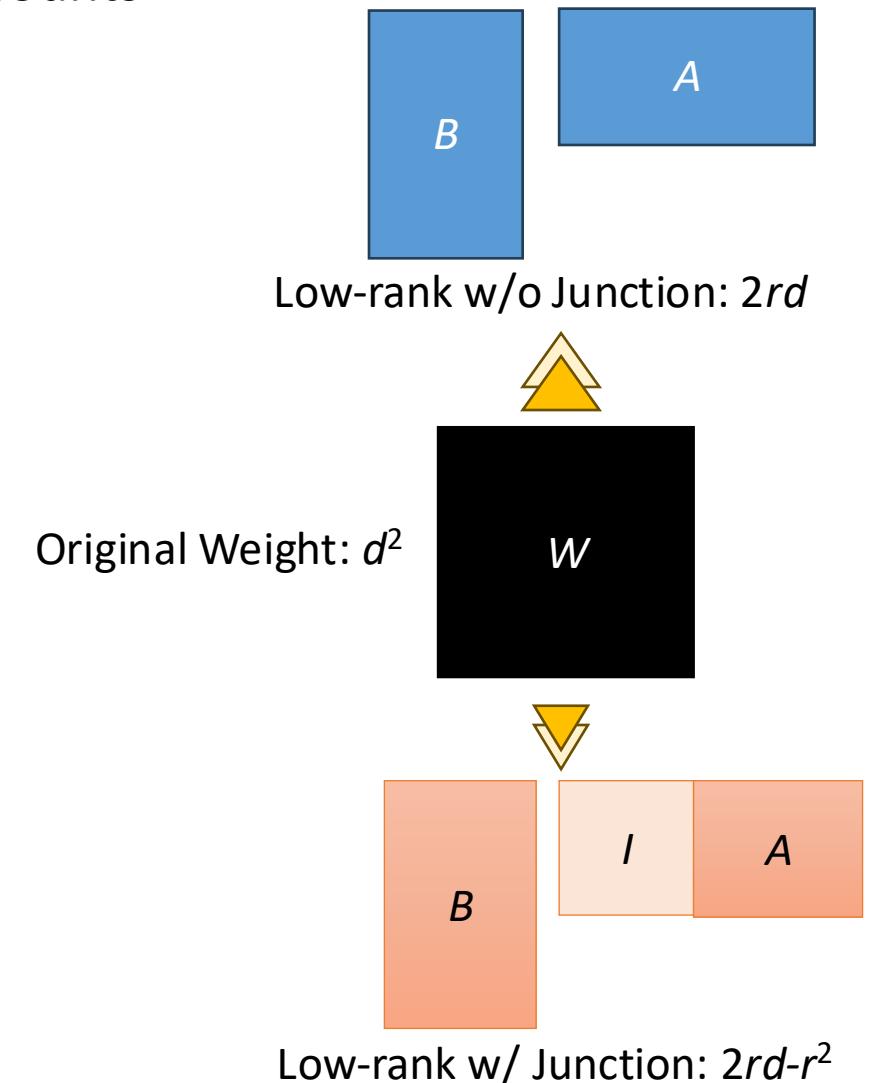
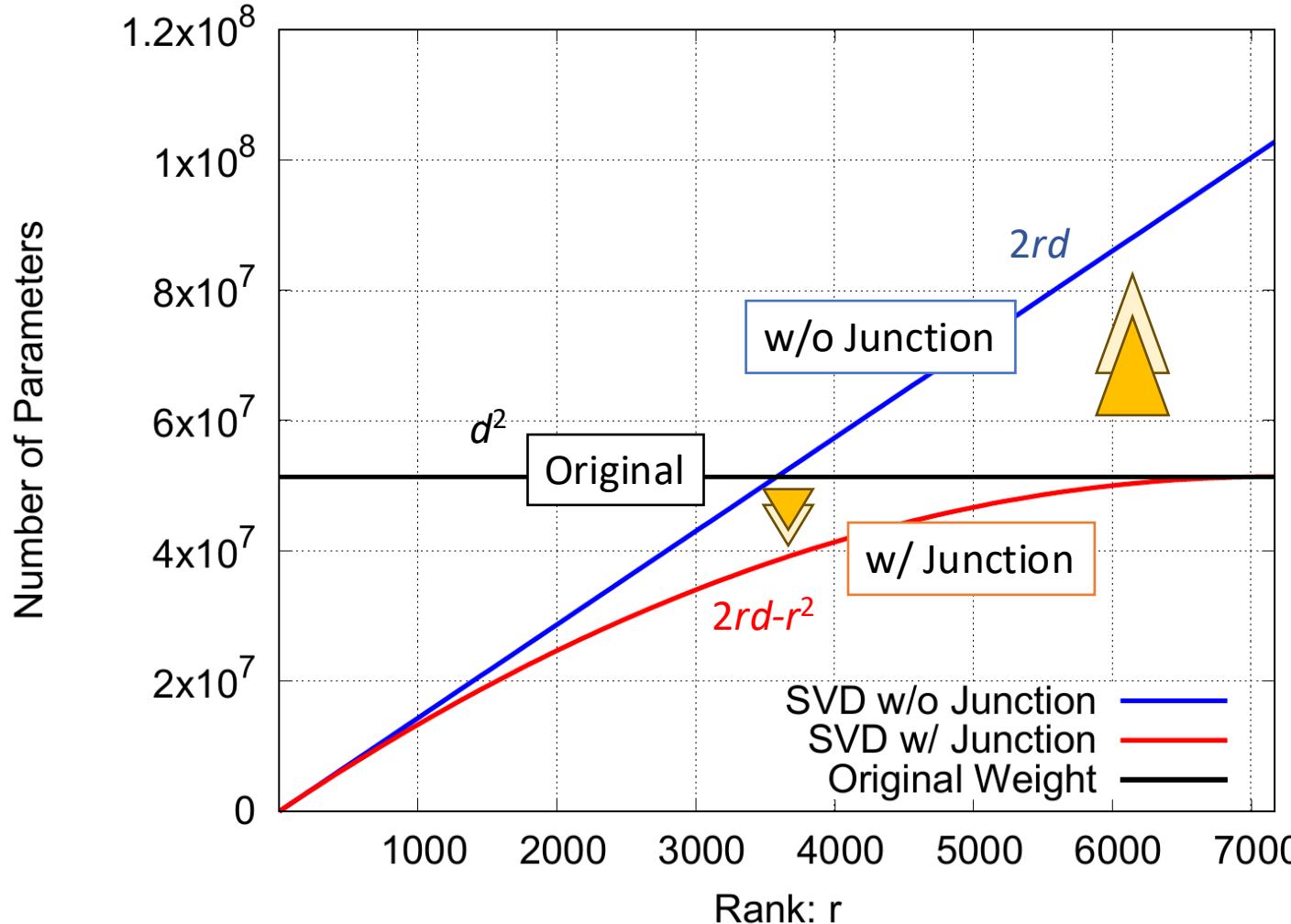
- Left singular: $J = I$;
- Right singular: $J = S^+$;
- Symmetry singular: $J = [S^{\frac{1}{2}}]^+$.
- Left block identity: $J = [US]_{:r}^+$
- Right block identity: $J = [V]_{:r}$



Total FLOPs/memory can be reduced

Junction Matrix Impact

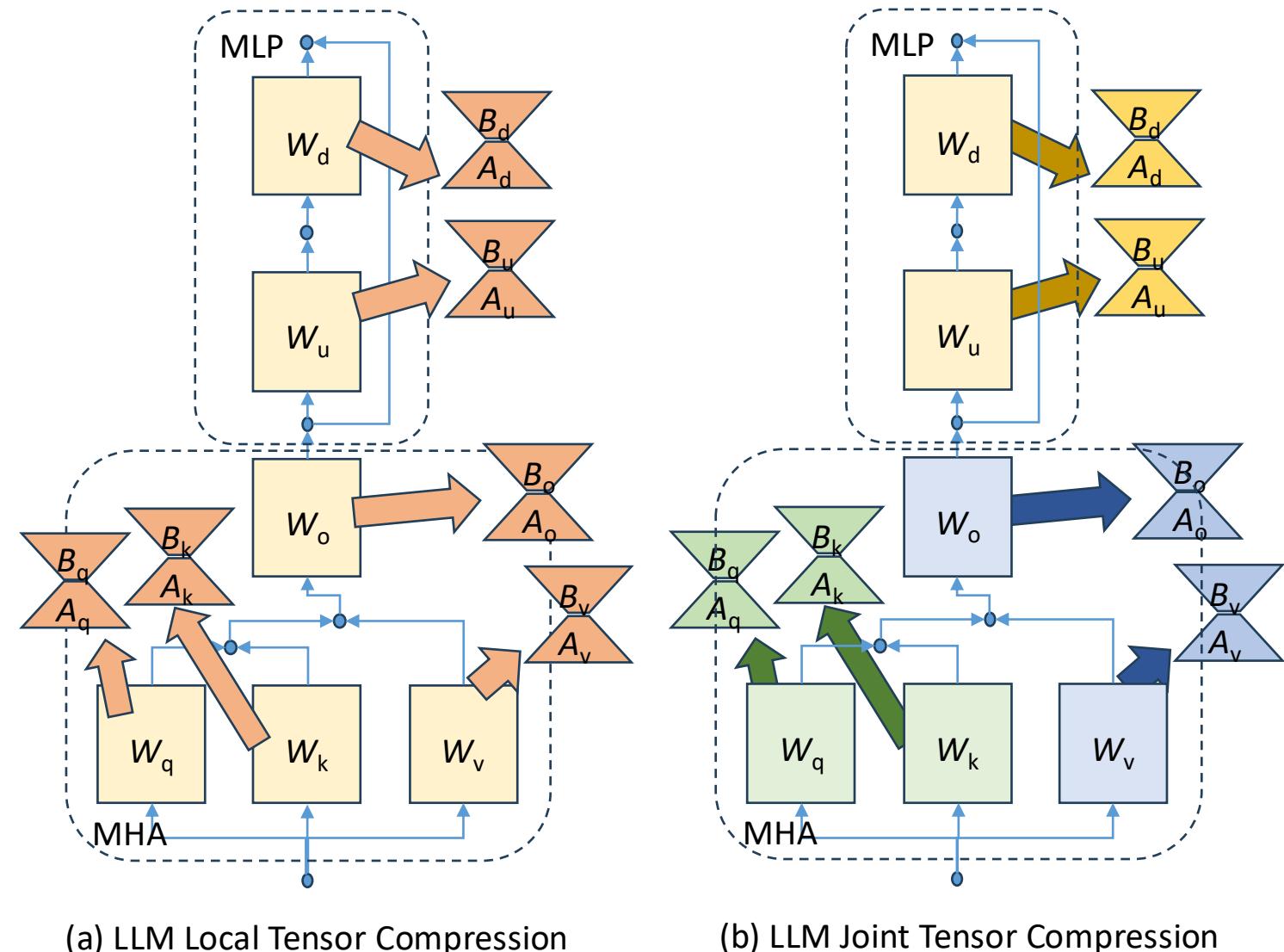
- SVD with block-identity junction can reduce the total number of parameters
 - SVD without junction can exceed the original parameter counts



3. Attention-Aware Joint Rank Reduction

- We propose to compress multiple weights jointly

- Joint QK compression
- Joint VO compression
- Joint UD compression



(a) LLM Local Tensor Compression

(b) LLM Joint Tensor Compression

Joint QK Compression: High-Order Tensor Decomposition

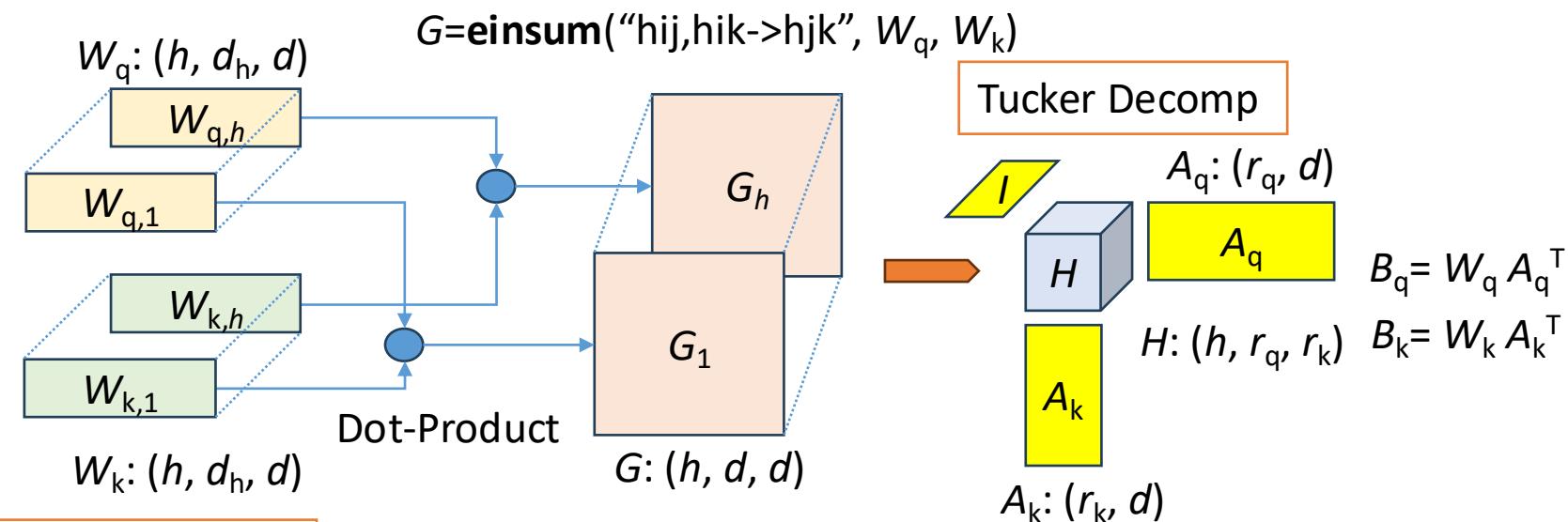
- Attention map error minimization:

$$\begin{aligned}
 \mathcal{L}_2 &= \sum_{i=1}^h \|M_i - \hat{M}_i\|^2 \\
 &= \sum_{i=1}^h \left\| \underbrace{C^{\frac{1}{2}} W_{q,i}^\top W_{k,i} C^{\frac{1}{2}}}_{G_i \in \mathbb{R}^{d \times d}} - \underbrace{C^{\frac{1}{2}} A_q^\top}_{A_q'^\top} \underbrace{B_{q,i}^\top B_{k,i}}_{H_i \in \mathbb{R}^{r_q \times r_k}} \underbrace{A_k C^{\frac{1}{2}}}_{A_k'} \right\|^2 \\
 &= \sum_{i=1}^h \|G_i - A_q'^\top H_i A_k'\|^2.
 \end{aligned} \tag{14}$$



Solution:
HO-SVD
(Tucker Decomposition)

$$\begin{aligned}
 M_i &= X^\top W_{q,i}^\top W_{k,i} X, \\
 \hat{M}_i &= X^\top A_q^\top B_{q,i}^\top B_{k,i} A_k X,
 \end{aligned}$$



Joint VO compression has similar solution

Joint UD Compression: Decoupled Loss Minimization

- We use decoupled loss minimization trick, similar to SparseLLM

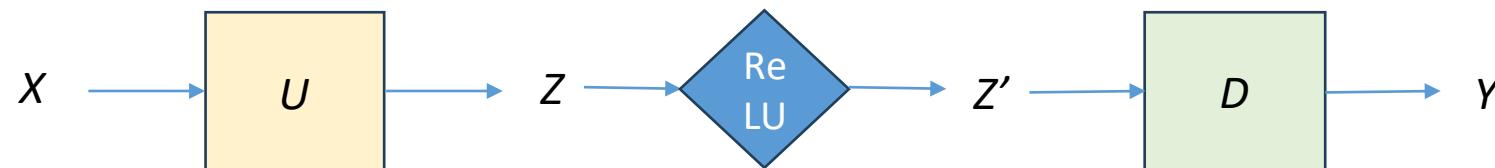
$$\mathcal{L} = \|W_d Z' - \hat{W}_d \sigma(\hat{W}_u X)\|^2$$

➤ $\mathcal{L}_4 = \alpha \|W_u X - Z\|^2 + \beta \|Z' - \sigma(Z)\|^2 + \gamma \|W_d Z' - Y\|^2,$

$Z_- = W_u X,$
 $Z_+ = \frac{1}{\alpha + \beta}(\alpha Z_- + \beta Z'),$

$Z' = (\gamma W_d^\top W_d + \beta I)^+ (\beta \sigma(Z) + \gamma W_d^\top Y)$

$$\begin{aligned} Z &= W_u X, \\ Z' &= \sigma(Z), \\ Y &= W_d Z', \end{aligned}$$

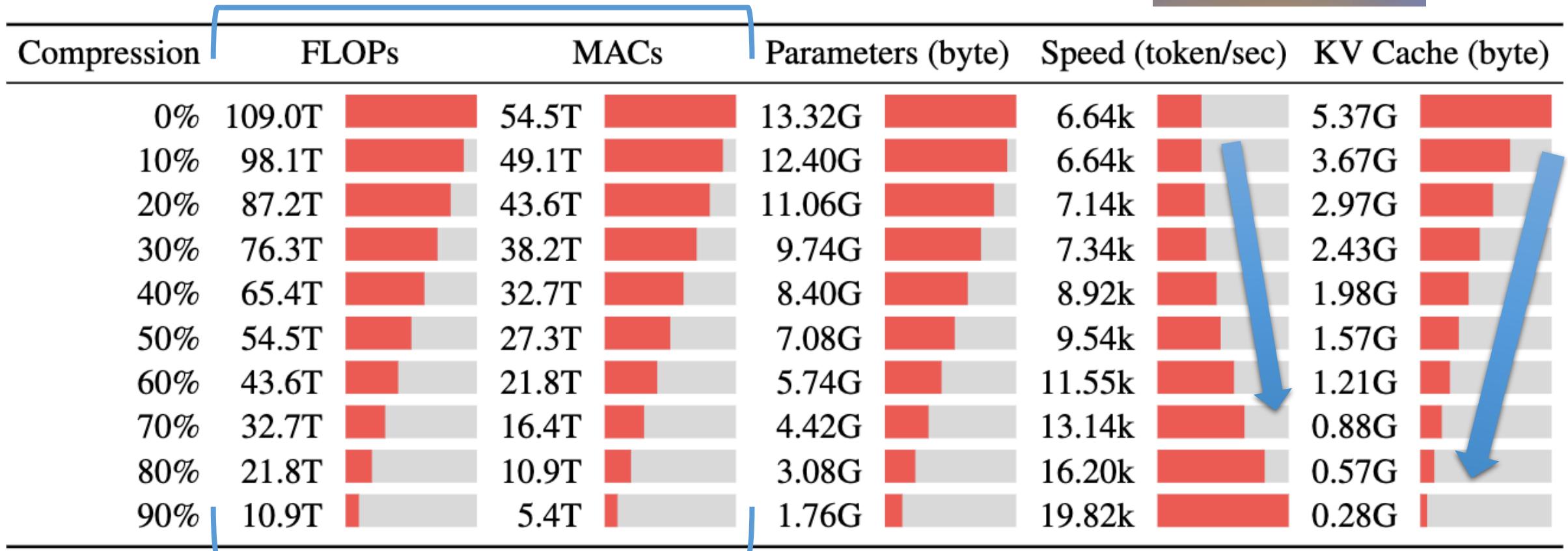


Alternating optimization of auxiliary values Z/Z' and weight rank reduction

Experiments: Complexity/Memory/Throughput Analysis

- FLOPs/MACs can decrease almost linearly
- Throughput improves almost quadratically
- KV cache reduces significantly

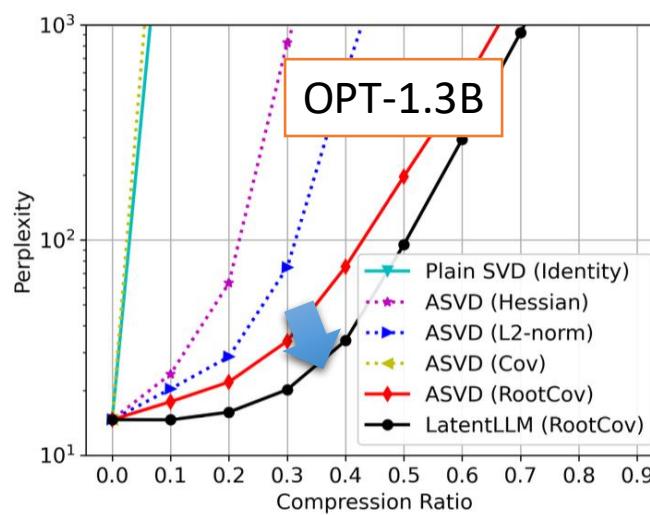
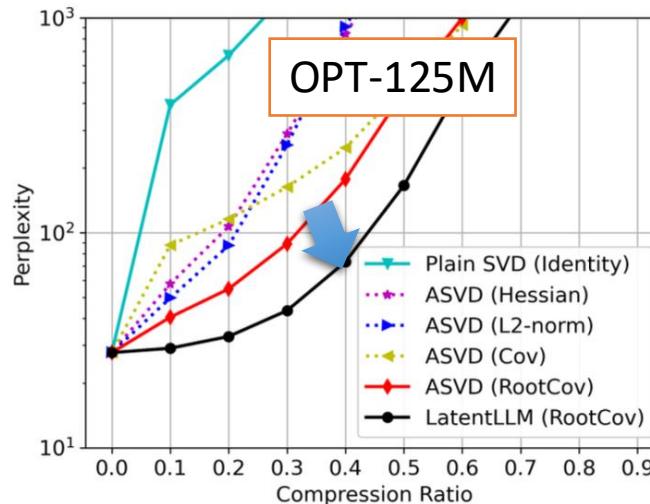
facebook
/opt-6.7b



LLM model: OPT-6.7B. 4-batch, 1024 tokens, `torch.compile("max-autotune")` on NVIDIA A40 GPU

Experiments: LLM Benchmark

- Wikitext-2 perplexity over LLM model sizes and variants



Compression	OPT-6.7B (Perplexity: 10.9)				
	10%	20%	30%	40%	50%
Plain SVD (Identity)	14839.0	67517.7	123286.4	27304.0	12780.0
ASVD (Hessian)	14.3	17.3	26.0	73.3	940.1
ASVD (ℓ_2 -norm)	12.6	14.6	18.7	30.6	146.4
ASVD (Cov)	9111.6	9842.6	11848.0	8514.7	8926.9
ASVD (RootCov)	11.8	13.5	17.0	27.2	56.71
LatentLLM (RootCov)	*10.7	11.5	13.5	18.0	33.3
Qwen3-8B (Perplexity: 9.2)					
Plain SVD (Identity)	2.4e5	9.0e6	2.8e7	5.3e7	4.3e8
ASVD (Hessian)	33.6	90.8	1250.8	5324.6	15933.7
ASVD (ℓ_2 -norm)	18.8	26.0	40.6	98.6	382.0
ASVD (Cov)	1.3e5	1.2e5	8.3e4	6.1e4	39455.9
ASVD (RootCov)	16.7	26.0	49.3	119.2	303.3
LatentLLM (RootCov)	11.8	14.2	22.4	53.9	166.3

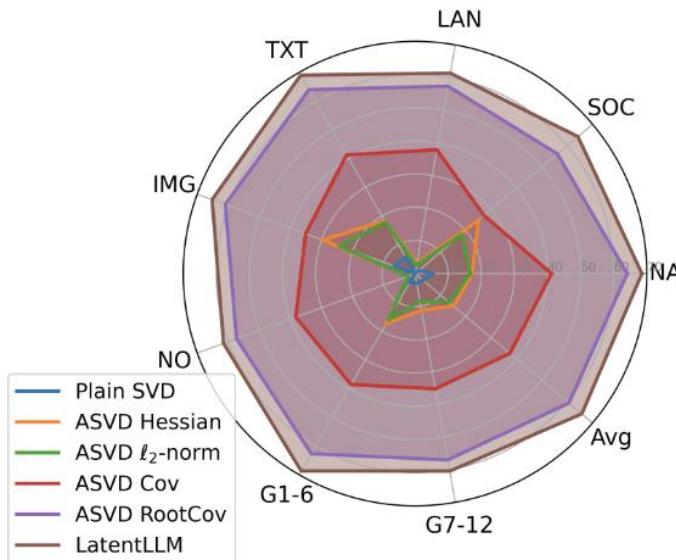
Experiments: VLM Benchmark (ScienceQA)

- LLaVA-7B model for visual reasoning benchmark: ScienceQA

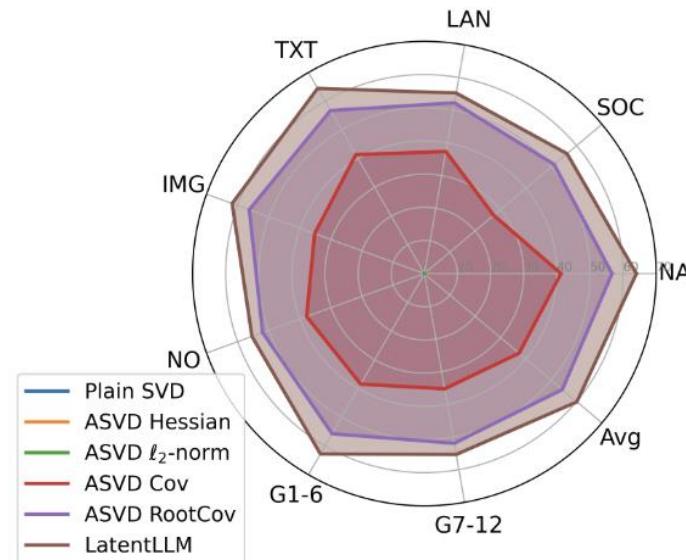
Compression	10%	20%	30%	40%	50%
Plain SVD (Identity)	3.18	0.09	0.07	0.00	0.00
ASVD (Hessian)	15.21	2.62	0.00	0.17	0.00
ASVD (ℓ_2 -norm)	13.37	0.40	0.05	0.07	0.00
ASVD (Cov)	37.42	37.42	37.33	37.02	36.95
ASVD (RootCov)	60.67	57.53	54.37	52.23	49.30
LatentLLM (RootCov)	65.76	63.85	60.13	54.59	52.25

Biology Genes to traits Classification Adaptations Traits and heredity Ecosystems Classification Scientific names Hereditiy Ecological interactions Cells Plants Animals Plant reproduction	Physics Materials Magnets Velocity and forces Force and motion Particle motion and energy Heat and thermal energy States of matter Kinetic and potential energy Mixture	Geography State capitals Geography Maps Oceania: geography Physical Geography The Americas: geography Oceans and continents Cities States	History Colonial America English colonies in North America The American Revolution	Economics Basic economic principles Supply and demand Banking and finance	Civics Social skills Government The Constitution
			World History Greece Ancient Mesopotamia World religions American history Medieval Asia	Global Studies Society and environment	
			Chemistry Solutions Physical and chemical change Atoms and molecules Chemical reactions	Writing Strategies Supporting arguments Sentences, fragments, and run-ons Word usage and nuance Creative techniques	Vocabulary Categories Shades of meaning Comprehension strategies Context clues
			Earth Science Weather and climate Rocks and minerals Astronomy Fossils Earth events Plate tectonics	Engineering Designing experiments Engineering practices	Verbs Verb tense
			Units and Measurement Weather and climate	Phonology Rhyming	Capitalization Formatting
				Figurative Language Literary devices	Punctuation Fragments
					Grammar Sentences and fragments Phrases and clauses
					Reference Research skills

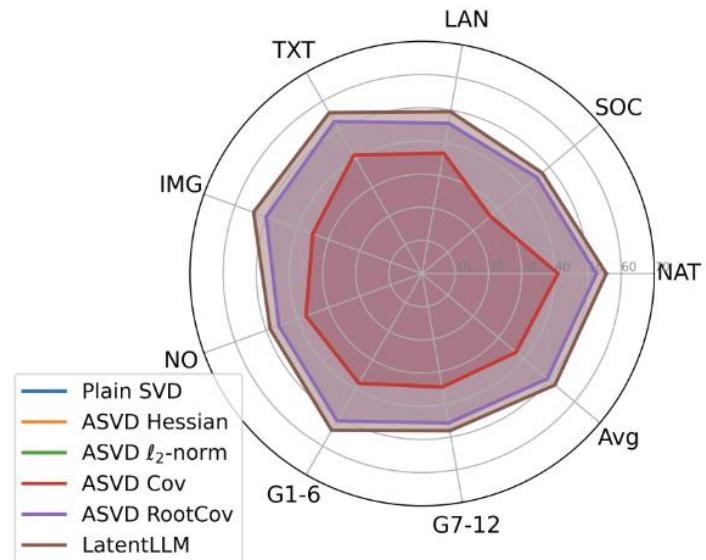
QA for Natural, Social, & Language Science



(a) 10% Compression



(b) 30% Compression



(c) 50% Compression

Experiments: VLM Benchmark (TextVQA)

- LLaVA-7B/Qwen2.5-VL-7B/3B models for visual reasoning benchmark: **TextVQA**

LLaVA

Qwen2.5-VL



Compression	10%	20%	30%	40%	50%
LLaVA-7B: Uncompressed Acc 61.32					
Plain SVD (identity)	2.36	0.48	0.35	0.34	0.36
ASVD (Hessian)	23.88	9.60	1.24	0.21	0.31
ASVD (ℓ_2 -norm)	24.41	9.53	2.77	0.82	0.75
ASVD (Cov)	0.38	0.36	0.40	0.33	0.35
ASVD (RootCov)	52.51	49.91	45.53	38.47	27.36
LatentLLM (RootCov)	60.06	57.65	52.63	46.90	35.94
Qwen2.5-VL-7B: Uncompressed Acc 82.11					
Plain SVD (identity)	0.02	0.47	0.32	0.05	0.11
ASVD (Hessian)	58.76	7.03	0.23	0.45	0.41
ASVD (ℓ_2 -norm)	77.84	73.92	57.13	18.79	0.41
ASVD (Cov)	0.41	0.41	0.41	0.41	0.41
ASVD (RootCov)	79.46	74.76	66.31	51.80	34.91
LatentLLM (RootCov)	80.85	79.30	73.90	62.11	42.53
Qwen2.5-VL-3B: Uncompressed Acc 78.17					
Plain SVD (identity)	0.01	0.08	0.09	0.09	0.01
ASVD (Hessian)	0.14	0.31	0.31	0.31	0.34
ASVD (ℓ_2 -norm)	44.23	0.14	0.00	0.41	0.37
ASVD (Cov)	0.41	0.41	0.41	0.41	0.41
ASVD (RootCov)	73.78	67.30	54.20	33.93	13.99
LatentLLM (RootCov)	76.44	74.29	64.28	45.80	19.67



What does it say near the star on the tail of the plane?

Ground Truth Prediction

jet

nothing

ASVD without RootCov:
Nearly 0% Acc

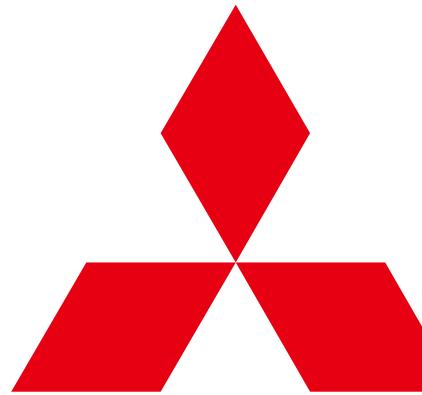
LatentLLM:
Best performance consistently

Table: Accuracy in percent (↑) on **TextVQA** dataset for compressed LLaVA-7B and Qwen2.5-VL-7B/3B.

Summary

- We introduced a new compression method **LatentLLM** for green AI
 - We discussed various preconditioning matrices, validating the optimality of root-covariance
 - We proposed to use junction matrix, improving the efficiency with block identity form
 - We derived a mathematically optimal joint tensor decomposition method, minimizing attention loss
 - LatentLLM can convert MHA to MLA like DeepSeek, without the need of re-training
 - We showed significant KV cache reduction and throughput improvement
 - We validated the superiority of LatentLLM over state-of-the-art rank reduction methods for various LLM/VLM models and benchmarks
- We plan:
 - to integrate pruning and quantization
 - to incorporate with fine-tuning
 - to apply to edge AI platforms
- Please contact us (koike@merl.com) for more discussions





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Changes for the Better