A Qualitative Approach to Classifying Gaze Direction

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An explicit quantitative approach to this problem requires **(a)** *a priori information about the interior geometry of the car and the calibration of the camera, and* **(b)** *accurate computation of the subject's location and gaze direction. This paper describes a more qualitative approach. The subject is observed over an extended period of time, and a "pose-space histogram" is used to record the frequency with which particular head poses occur. For observation of a car driver, peaks will appear in the histogram according to the frequently viewed directions of straight-ahead, toward the dashboard, and the mirrors. Each peak is labelled, and the focus of attention of the driver in all subsequent images is then classified by use of the histogram.*

1 Introduction

This paper addresses the classification of the focus of attention of a vehicle driver. This is an important component in the development of automatic safety mechanisms [2, 6] e.g. to alert a driver who is looking to one side while other sensors are indicating a potential collision in front of the vehicle.

An explicit quantitative approach would involve *(a)* modelling the interior geometry of the car and obtaining the calibration of the camera, and storing this as *a priori* information, and *(b)* making an accurate computation of the driver's location and gaze direction. Generating a 3D ray for the driver's gaze direction in the car coordinate frame then determines what the driver is looking at.

There are problems with this kind of approach. Firstly, although the geometry of the car's interior will usually be known from the manufacturer's design data, the intrinsic parameters of the camera and extrinsic parameters relative to the car coordinate frame need to be calibrated. That extrinsic calibration might change over time due to vibration. Furthermore, the location of the driver's head and gaze direction must be computed in the car coordinate frame at run-time.

To avoid these difficulties, we adopt a qualitative approach. The driver is observed over an extended period. For each acquired image, the driver's head pose is computed and used to update a "pose-space histogram". Peaks in the histogram indicate those head poses which occur most frequently, and can be expected to occur for the driver looking straight-ahead, towards the dashboard, towards the rear-view and side mirrors, and out of the side window. It is straightforward to label the frequently occurring head poses from a qualitative description of the relative location of windscreen, mirrors etc. The focus of attention of the driver in all subsequent images can then be classified by measuring head pose and checking whether it is close to a labelled peak in the pose-space. [1]

Head pose alone does not of course determine gaze direction. But for our application, the head pose is often a good indicator of the driver's focus of attention. For instance, looking at the side or rear-view mirrors requires the adoption of a particular head pose. We discuss situations where head pose alone is insufficient for the application, plus extension of the work to handle eye direction in Section 6.

The algorithms used are appropriate for the Artificial Retina camera [3], a low-cost (a few tens of dollars) image detector which has programmable on-chip processing. We have a version with a 32x32 detector array, and so employed algorithms which are able to give useful results at coarse image resolutions.

The next section is an overview of our approach. Section 3 describes the measurement of the driver's head pose, Section 4 describes the construction of a pose-space histogram which encodes the head pose over time, and Section 5 contains experimental results.

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[1] We use the term "qualitative" for this approach to indicate that there is no computation of absolute angles of the head pose; however, we will make accurate and repeatable measurements related to the head pose.

2 Overview

The head is modelled with an ellipsoid [1, 5]. An ellipsoid is a crude model but is sufficient in the context of the overall system since our aim is not to make accurate quantitative measurements, but to identify frequently adopted head poses, and to classify these poses based on a qualitative description of their relative orientations.

Figure 1 is a diagrammatic overview of the four components to the processing - **(a)** initialise an ellipsoid coincident with the driver's head (Section 3.1), **(b)** use the ellipsoid to generate an array of synthetic views for a range of head motion (Section 3.2); this is done offline as part of the initialisation process, **(c)** search for the synthetic view which best matches a target image of the driver (Section 3.3), **(d)** accumulate head pose information over time in order to classify the driver's focus of attention (Section 4).

3 Processing Head Pose

3.1 Initialisation

Initialisation involves setting up a 3D coordinate frame containing a camera and ellipsoid, such that they are consistent with a fronto-parallel "reference" image of the subject. See Figure 1a. This process requires some assumptions about approximate camera intrinsic/extrinsic parameters and typical human head sizes as described below, but note that there is no requirement for exact camera calibration or other information here.

A quadric surface can be described by a 4x4 symmetric matrix $\mathtt{Q}$.

$$\mathbf{X}^\top \mathtt{Q} \mathbf{X} = 0 \qquad (1)$$

where $\mathbf{X} = (X, Y, Z, 1)^\top$ are homogeneous coordinates for a 3D point. For an ellipsoid in canonical position, matrix $\mathtt{Q}$ is diagonal with diagonal elements $\left[a^{-2}, b^{-2}, c^{-2}, -1 \right]$, where the axis lengths of the ellipsoid along the $x-$, $y-$ and $z-$axes are $2a$, $2b$, $2c$ respectively. Assume the x-axis is the horizontal axis through the ears, the $y-$axis is aligned with the vertical direction through the head, and a horizontal cross-section through the head is a circle (the ellipsoid is prolate) so that $a = c$.

The initialisation process is manual. We start with reasonable estimates of camera intrinsic and extrinsic parameters, and ellipsoid parameters, for the particular setup which is used to generate the reference image.[2] Based on these assumed parameters, the el-

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[2] For the initial estimate of the camera intrinsics, the focal length (in pixels) is obtained by taking coarse estimates of the subject's distance and head size, and using a similar triangles
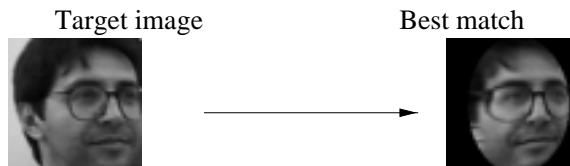
(a) Initialise ellipsoid

Reference image

(b) Generate synthetic views offline

(c) Matching

Target image   Best match
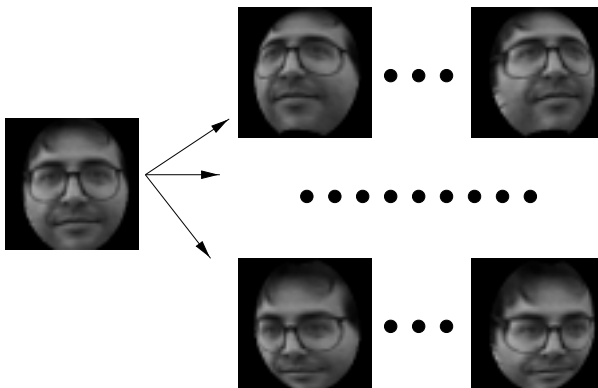
(d) Record head pose over time

looking left   looking right

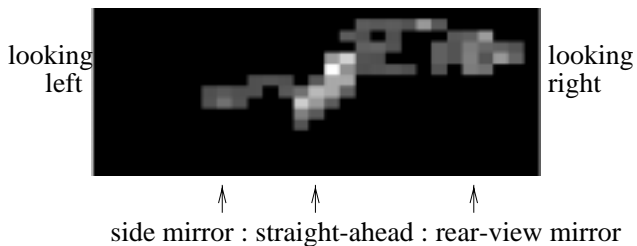side mirror : straight-ahead : rear-view mirror

Figure 1: *(a)* a 3D ellipsoid is initialised to coincide with a reference image of the subject's head, *(b)* the reference image provides the basis for generating a series of synthetic views consistent with rotations of the head, *(c)* a target image of the subject is matched against the synthetic views, *(d)* information about head pose is accumulated over time in a pose-space histogram.

lipsoid is projected onto the image plane, and any discrepancy between the projected location and the actual outline of the driver's head is manually corrected by adjusting the extrinsics and the ratio b/a.

3.2 Generating a Synthetic View

Once the ellipsoid model has been initialised, we can generate a synthetic view of the face consistent with a specified rotation and translation of the head.

For mathematical convenience, we develop the description by an equivalent scenario in which the head is assumed fixed, and the camera is moving relative to it. Generating a synthetic view involves the following conceptual steps - *(a)* the texture from the reference image is backprojected onto the ellipsoid, *(b)* a new location and orientation of the camera is specified, and the texture is reprojected to the image plane of the new camera to generate the required synthetic view. In practice, the image texture is mapped directly from the reference image to the synthetic image.

(a) Backprojection of texture:

Assume that for the reference image, the ellipsoid is in the canonical position and the camera has rotation R and translation $\mathbf{T}=(t_x, t_y, t_z)$ in the world coordinate frame. The perspective projection equation is

$$\mathbf{x} = P\mathbf{X} \qquad (2)$$

where $\mathbf{x} = (x, y, 1)^\top$ are homogeneous coordinates for an image point. For homogeneous quantities '=' indicates equality up to a non-zero scale factor.

In a Euclidean coordinate frame, P can be decomposed as

$$P = C[R| - R\mathbf{T}] \qquad (3)$$

where C is the camera matrix [4].

An image pixel $\mathbf{x}$ backprojects to a ray in the world coordinate frame described by

$$\mathbf{X} = \begin{pmatrix} \mathbf{T} \\ 1 \end{pmatrix} + \lambda \begin{pmatrix} D \\ 0 \end{pmatrix} \qquad (4)$$

where

$$\mathbf{D} = (d_x, d_y, d_z) = R^{-1}C^{-1}\mathbf{x} \qquad (5)$$

Substituting into equation (1) gives a quadratic in λ,

$$a\lambda^2 + b\lambda + c = 0 \qquad (6)$$

where

$$a = d_x^2 Q_{1,1} + d_y^2 Q_{2,2} + d_z^2 Q_{3,3}$$

$$b = 2(d_x t_x Q_{1,1} + d_y t_y Q_{2,2} + d_z t_z Q_{3,3})$$

$$c = t_x^2 Q_{1,1} + t_y^2 Q_{2,2} + t_z^2 Q_{3,3} + Q_{4,4}$$

and $Q_{m,n}$ is the (m, n)th element of Q.

The roots of equation (6) give the intersection points of the ray with the ellipsoid (zero, one or two intersection points). For our problem, the ellipsoid is always in front of the camera. When the number of roots is two, their values are positive and the smaller value of λ corresponds to the intersection of the ray with the front (visible) side of the ellipsoid.

(b) Reprojection of texture:

Assume we want to generate a synthetic image consistent with a transformation R_h, $\mathbf{T_h}$ of the driver's head. The pixel location $\mathbf{x_r}$ in the reference image which corresponds to a pixel $\mathbf{x_s}$ in the synthetic image is determined by -

1. Transform the location of the original (reference image) camera by a rotation and translation R_h^{-1}, $-\mathbf{T_h}$ in the world coordinate frame. Construct the matrix P' for the transformed camera using equation (3).

2. Backproject a ray from pixel $\mathbf{x_s}$ in the transformed camera, and find its intersection point $\mathbf{X_s}$ with the front side of the ellipsoid using equation (6). If there is no intersection point, discontinue. If the intersection point is not on the front (visible) side of the ellipsoid relative to the *reference* image, discontinue.

3. Project $\mathbf{X_s}$ onto the reference image - the projected image point is $\mathbf{x_r}$.

4. The pixel intensity at $\mathbf{x_s}$ in the synthetic image is then given by the intensity at $\mathbf{x_r}$ in the reference image. Note that $\mathbf{x_r}$ specifies a sub-pixel location in the reference image. To obtain a good resampling, we fit a quadric to the 3x3 patch around the required location in the reference image, and interpolate to obtain the intensity at the sub-pixel coordinates.

The synthetic view generation described above is repeated for a range of rotations around the $x-$ and $y-$ axes (the horizontal axis through the ears, and the vertical axis through the head respectively) to generate an array of synthetic views. This is done offline at initialisation time. Typically we use $\pm 35°$ and $\pm 56°$ around the horizontal axis and vertical axes respectively. We have currently omitted to include cyclorotations of the head because these are relatively uncommon motions - there is in any case some resilience in

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construction. For the initial estimate of the camera extrinsics, the optical axis is assumed to intersect the origin of the ellipsoid, while the distance of the camera to the subject was typically about 1m. For the initial estimate of the ellipsoid parameters, the typical width of a human head is assumed to be $a = 25$cm, and the ratio $b/a = 1.7$.

the processing to cyclorotation. Sample images from the full set are shown in Figure 2.

Figure 2: An array of synthetic views is generated from the reference image, corresponding to head rotations around the axis through the ears and around the vertical axis. This figure shows a sample of the images - the full series is typically an 11x17 array.

3.3 Matching Against Synthetic Views

Processing a target image of the driver now involves comparing that image with each of the synthetic views to find the best match.

Consider a target image I which is being matched against a synthetic image S. The goodness of match M between the two is found by computing

$$M = \sum 1 - \cos(I_d(i,j) - S_d(i,j)) \qquad (7)$$

where $I_d(i,j), S_d(i,j)$ are the directions of the gradient of the image intensity at pixel (i,j) in the target and synthetic images respectively, and the summation is over all significant (i.e. on the ellipsoid) pixels in the synthetic view. The best-matching synthetic view is the one which minimises this score.

While translational motion of the driver's head could also be handled by searching over translations of the ellipsoid in the 3D world coordinate frame, we take a different approach. The target image is matched against a synthetic view for a range of offsets around the default position. Typically the range of offsets is $\pm$ 4 pixels in steps of 2 pixels. This is almost equivalent to searching through the space of translations in 3D space, but offers a more explicit understanding of the coverage of the search space.

3.4 Using Multiple Reference Images

The basic scheme above is extended to make use of three reference images of the subject in the following way. The fronto-parallel reference image is used to generate an array of synthetic views. The subject looks to the left, a left-facing reference image is taken, and the best-match synthetic view is computed. All the synthetic views in the array which correspond to more extreme left-turn rotations than the best-match are now regenerated, using the left-facing reference image. This is repeated on the right side. This provides better quality synthetic views for the more extreme rotations of the head.

The next section describes how the information obtained from matching in Section 3.3 is used to classify what the driver is looking at.

4   The Pose-Space Histogram

The algorithm in the previous section will not deliver accurate measurements of head orientation, because we are using an approximate head model and working at low image resolutions, but it does produce reliable measurements about relative pose and that is what we seek to capitalise on.

Corresponding to the 2D array of synthetic views (Figure 2), a 2D histogram of the same dimensions is set up. All elements in the array are initialised to zero. For each new target image of the driver, once the best-matching synthetic view is found, the corresponding element in the histogram is incremented. Over an extended period, peaks will appear in the histogram for those head poses which are being most frequently adopted.

Ideally, we would expect to find a peak corresponding to the driver looking out of the left-side window, then a peak to the right of this for viewing the left-side mirror, two vertically-aligned peaks corresponding to viewing straight-ahead and looking at the dashboard, and another peak to the right of this corresponding to viewing the rear-view mirror. The observed peaks can be labelled automatically in accordance with this. Thereafter, for any acquired image of the driver, we find its best-matching synthetic view, use that to index the corresponding location in the histogram, and then classify the target image according to the labelling of the nearest peak in the histogram. Thus, classification of the driver's focus of attention is achieved without any quantitative information about the 3D layout of the car.

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5 Results

The system runs on an SGI workstation. For the majority of the experiments, image acquisition was by a Sony Hi-8 video camera with the images subsampled to 32x32 pixels. Some of the experiments were carried out directly on images captured by the Artificial Retina. The processing speed is about 6Hz.

Since the main idea of this system is to avoid explicit measurement of the rotation angles of the head, we will not provide quantitative measurements about head pose, but will illustrate various aspects of the performance of the system.

As previously discussed, Figures 1 and 2 depict a typical reference image and a selection of synthetically generated views (shown at higher than 32x32 resolution for illustration). Synthetic views of the face were generated in the range $\pm 35°$ and $\pm 56°$ around the horizontal and vertical axes respectively, quantized at $7°$ intervals, for a total of 187 synthetic views. This initialisation process takes some tens of seconds.

Figure 3 shows tracking for a number of different subjects. For each image, the best-matching synthetic view has been found, and a 3D head model is illustrated with pose given by the pose angles which were used to generate that synthetic view. This use of the absolute angles is for illustration only, and is not part of the processing.

Figure 4 shows a typical target image together with the error surface generated by matching the target against each image in the array of synthetic views. The error surface is often well-behaved, as shown here. The horizontal elongation of the minimum probably occurs because the dominant features in the matching process are the upper hairline, the eyes, and the mouth - all horizontally aligned features so that horizontal offsets have smaller effect on the matching score in equation (7) than vertical offsets.

Figure 5 shows the result of an experiment in which the subject repeatedly views three different locations over an extended period, with a short pause (about 1s) at each location. In Figure 5a, the three locations correspond to the rear-view mirror, the side-mirror, and straight-ahead for a car driver. The pose-space histogram shows distinctive peaks for each location. In Figure 5b, the three locations correspond to the rear-view mirror, straight-ahead, and the dashboard. The pose-space histogram has a separate peak for the rear-view mirror direction, but the other two directions are not differentiable. This is as expected since the array of the synthetic views has a resolution of 7 degrees between images, which is similar to the head motion for these two directions. This is discussed further in

Figure 3: Segments of image sequences (not consecutive images) for different subjects, showing resilience to strong illumination gradients (top), specularities on spectacles (centre), and changing facial expression (bottom).

Section 6.

Figure 6 shows the pose-space histogram for a short video sequence of a driver in a car. There is a peak for the straight-ahead viewing direction, and lobes to the left and right correspond to the driver looking at the side and rear-view mirrors.

6 Analysis and Future Work

A large part of the work so far has dealt with the head tracking. In our first version of the system, the synthetic views were initialised from a single fronto-parallel reference image of the subject; we modified this to utilise three reference images of the subject (fronto-parallel, left-view, right-view) when it became clear that a lot of valuable information is present in the hairline at the sides of the face. Our matching metric (equation (7)) uses gradients of the image intensity to obtain resilience to illumination changes and illumination gradients.

The current system does not discriminate between a driver's focus of attention being straight-ahead or towards the dashboard, because of the relatively small head motion involved (in fact, of course, there may

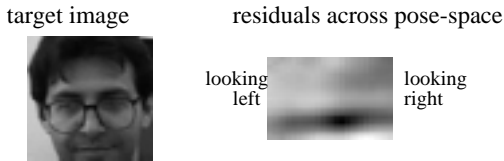target image   residuals across pose-space

Figure 4: A typical target image together with the error surface generated by matching the image against each image in the array of synthetic views. The darker areas indicate lower residuals (better matching). The error surface is well-behaved, with a clear minimum at the expected location.
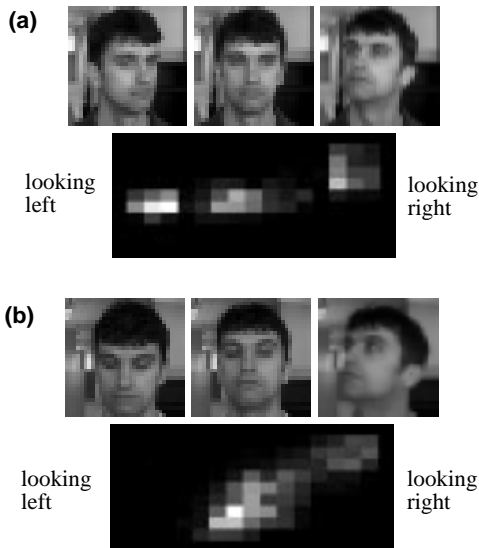

Figure 5: **(a)** The images show the three head poses adopted repeatedly over an extended sequence, together with the pose-space histogram which shows three distinct peaks for those head poses. **(b)** A similar experiment but two of the head poses (forward and forward-down) are not sufficiently far apart to register as distinct peaks in the pose-space histogram.

Figure 6: At top, three sample images from a driving sequence. At bottom, the pose-space histogram for this sequence, showing a peak for the driver looking straight-forward, and side lobes corresponding to viewing the side and rear-view mirrors.

be no head motion, just eye motion, between the two). Increasing the resolution of the array of synthetic views does not help, since the problem is due to the approximate nature of the ellipsoid model plus the low-resolution of the images being used. To deal with this in future work, we are considering replacing the ellipsoid model with a generic head model. We are also considering the computation of eye direction (which would require higher resolution imagery). For the latter, we would like to develop a scheme which does not make Euclidean measurements, to maintain the approach of the basic system.

7 Conclusion

This paper describes work in progress on a system for classifying the focus of attention of a car driver.

We introduced a representation - the pose-space histogram - for classifying the driver's focus of attention without computing Euclidean information. By avoiding explicit Euclidean measurements, we avoid the need to know *a priori* information about the car's interior geometry, the camera calibration, or the driver's exact location and gaze direction, and thereby hope to achieve a more robust system.

Within this framework, the choice of algorithms is motivated by the use of the Artificial Retina. In particular, synthetic view generation is done offline to enable fast run-time processing, and the use of a template matching approach rather than facial feature detection is appropriate to the 32x32 image resolution.

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