Quantum Transfer Learning for Wi-Fi Sensing

Koike-Akino, Toshiaki; Pu, Wang; Wang, Ye

TR2022-044 May 20, 2022

Abstract

Beyond data communications, commercial-off-theshelf Wi-Fi devices can be used to monitor human activities, track device locomotion, and sense the ambient environment. In particular, spatial beam attributes that are inherently available in the 60-GHz IEEE 802.11ad/ay standards have shown to be effective in terms of overhead and channel measurement granularity for these indoor sensing tasks. In this paper, we investigate transfer learning to mitigate domain shift in human monitoring tasks when Wi-Fi settings and environments change over time. As a proof-of-concept study, we consider quantum neural networks (QNN) as well as classical deep neural networks (DNN) for the future quantum-ready society. The effectiveness of both DNN and QNN is validated by an in-house experiment for human pose recognition, achieving greater than 90% accuracy with a limited data size.

IEEE International Conference on Communications (ICC) 2022

© 2022 IEEE. Personal use of this material is permitted. Permission from IEEE must be obtained for all other uses, in any current or future media, including reprinting/republishing this material for advertising or promotional purposes, creating new collective works, for resale or redistribution to servers or lists, or reuse of any copyrighted component of this work in other works.

Mitsubishi Electric Research Laboratories, Inc. 201 Broadway, Cambridge, Massachusetts 02139

Quantum Transfer Learning for Wi-Fi Sensing

Toshiaki Koike-Akino, Pu Wang, Ye Wang

Mitsubishi Electric Research Laboratories (MERL), Cambridge, MA 02139, USA

Email: {koike, pwang, yewang}@merl.com

Abstract—Beyond data communications, commercial-off-theshelf Wi-Fi devices can be used to monitor human activities, track device locomotion, and sense the ambient environment. In particular, spatial beam attributes that are inherently available in the 60-GHz IEEE 802.11ad/ay standards have shown to be effective in terms of overhead and channel measurement granularity for these indoor sensing tasks. In this paper, we investigate transfer learning to mitigate domain shift in human monitoring tasks when Wi-Fi settings and environments change over time. As a proof-of-concept study, we consider quantum neural networks (QNN) as well as classical deep neural networks (DNN) for the future quantum-ready society. The effectiveness of both DNN and QNN is validated by an in-house experiment for human pose recognition, achieving greater than 90% accuracy with a limited data size.

Index Terms—Integrated sensing and communication (ISAC), Wi-Fi sensing, human monitoring, quantum machine learning.

I. INTRODUCTION

Wi-Fi-based human activity monitoring has received much attention over the past decade due to the decreasing cost and less privacy concerns compared with camera-based approaches. Modern deep neural networks (DNNs) have made commercial Wi-Fi-band signals useful for human sensing tasks such as user identification, gesture recognition, devicefree localization, fall detection, emotion sensing, and skeleton tracking [1]–[24]. Nonetheless, Wi-Fi sensing is susceptible to time-varying fading, shadowing, path loss, hardware impairments (such as carrier frequency offset, symbol timing offset, and sampling frequency offset), interference, and noise. Accordingly, DNNs designed at a training session may not be reliable enough at a time of testing.

In this paper, we investigate transfer learning (TL) or domain adaptation (DA) [25] to be robust against such timevarying domain shifts for Wi-Fi sensing. We experimentally validate the benefit of TL for DNNs to accurately recognize human's pose using commercial-off-the-shelf (COTS) Wi-Fi devices. Besides standard DNNs, we introduce a new framework of quantum neural networks (QNNs) which leverage a quantum processing unit (QPU) as an alternative solution for an envisioned future era of quantum supremacy [26, 27]. While quantum machine learning (QML) is considered as a potential driver in the sixth generation (6G) applications [28], there are few research yet to tackle practical problems. To the best of our knowledge, this is the very first paper studying QML for Wi-Fi sensing. We specifically exploit a similar technique of quantum transfer learning (QTL) framework [29].

Quantum computers have the potential to realize computationally efficient signal processing compared to traditional digital computers by exploiting quantum mechanism, e.g., superposition and entanglement, in terms of not only execution time but also energy consumption. In the past few years, several companies including IBM, Google, and Honeywell have manufactured commercial quantum computers. For instance, IBM has released 127-qubit QPUs available to the public via a cloud service. Some groups reported to have achieved quantum supremacy for specific problems [26, 27]. It may be no longer far future when noisy intermediate-scale quantum (NISQ) computers [30] will be widely used for various real applications. Although quantum-ready algorithms for wireless communication systems have been investigated [31]-[34], most existing works assume fault-tolerant QPUs, which may be beyond the capability of near-term NISQ devices. Recently, hybrid quantum-classical algorithms based on the variational principle were proposed to achieve high robustness against quantum errors [35]-[38]. Hence, such modern variational quantum algorithms have not been studied for communications problem until very recently [39, 40].

We use variational quantum circuit (VQC) [41] to build QNN [42] as a state-of-the-art QML approach [43]–[48]. The contributions of this paper are three-fold as described below:

- This paper is the very first one to introduce QML for Wi-Fi sensing.
- We verify its feasibility for the human pose recognition application with COTS Wi-Fi devices.
- The TL framework is validated to improve the robustness against domain shifts across Wi-Fi scanning sessions.

II. WI-FI SENSING FOR HUMAN MONITORING

For Wi-Fi sensing, we collect beam scanning measurements associated with a class of human gestures as a fingerprinting data to learn DNN and QNN models.

A. Human Pose Recognition Experiments

Fig. 1 (a) shows our experimental configuration using one Wi-Fi station in front of a subject and another station behind the subject. Both stations are placed on a stand of a height of 1.2 meters with a distance of approximately 2 meters. As shown in Fig. 1 (b), the subject is asked to perform a total of 8 poses including distinct gestures like 'sit', 'stand with left arm lifted', etc. For each pose, we recorded 7 independent data sessions with different time durations and with sufficient time separation between consecutive two sessions. We use the measurements in the first four data sessions as the training data (referred to as 'source domain') and those in the last three sessions as the test data ('target domain').



(a) Wi-Fi pose recognition empowered by QML



(b) Pose snapshots

Fig. 1. Wi-Fi sensing tasks and experiment settings.

TABLE I NUMBER OF BEAM SNR SAMPLES FOR EACH POSE

	~ ~ .	
Pose	Source Domain	Target Domain
0	434	151
1	499	149
2	325	173
3	347	129
4	238	88
5	314	96
6	272	119
7	432	135
Total	42,915	1,040

The total number of measurement samples is 42,915 and 1,040 in the source domain and target domain datasets, respectively. The pose-wise distribution is listed in Table I. We further divide the dataset in each domain into two subsets: i) labeled for training an ML model and ii) unlabeled for evaluating prediction accuracy of the ML model. For simplicity, no data augmentation was used.

B. COTS Wi-Fi Testbed: mmWave Beam SNR

As super-grained mmWave channel state information is not accessible from COTS devices without additional overhead, we use *mid-grained* Wi-Fi measurements in the beam angle domain—beam signal-to-noise ratios (SNRs)—generated from the beam training (a.k.a. beam alignment) phase. For each probing beampattern (a.k.a. beam sectors), beam SNR is collected by 802.11ad devices as a measure of beam quality. Such beam training is periodically carried out and the beam sectors



Fig. 2. Mid-grained beam SNR measurements at mmWave frequency bands, i.e., 60 GHz in 802.11ad standards.

are adapted to environmental changes. Fig. 2 shows beam SNRs at pre-specified beampatterns used at the transmitting side. Access to raw mmWave beam SNR measurements from COTS devices is obtained via an open-source software [49].

We use 802.11ad-compliant TP-Link Talon AD7200 routers to collect beam SNRs at 60 GHz. This router supports a single stream communication using analog beamforming over a 32-element planar array. From one beam training, one Wi-Fi station can collect 36 beam SNRs across discrete transmitting beampatterns. The measured beam SNRs are sent to a workstation via Ethernet cables to train DNN or QNN (e.g., through the IBM quantum cloud service). The experimental system is deployed in a standard indoor room setting. Further details of the experiments can be found in our previous work [24]

The key challenge of Wi-Fi sensing is that Wi-Fi measurements or the ambient environment may change over measurement sessions and these changes will degrade the efficiency of machine learning models due to the domain shifts. We investigate a TL framework to tackle the domain shift issues, focusing on QTL [29] as described in the next section.

III. QUANTUM TRANSFER LEARNING (QTL)

A. Quantum Machine Learning (QML)

Variational quantum algorithms [35]–[38] are key enabling techniques for NISQ QPUs [30]. We previously demonstrated that they are useful for some communications problems in [39, 40] by using real QPU computing at the IBM cloud service. Variational quantum computing has been further integrated to machine learning, e.g., QNN [42], quanvolutional network [43], quantum autoencoder (QAE) [44], quantum graph neural network (QGNN) [48], and quantum generative adversarial network (QGAN) [46, 47].

Fig. 3 shows a yearly trend of QML in the number of articles hit in Google scholar with keywords of 'quantum



Fig. 3. Number of articles hit in Google scholar: articles on "quantum machine learning" has exponentially increased at an annual growth rate of 2 folds.

machine learning' vs 'deep neural network'. It is found that the number of QML articles has been exponentially increasing over the last decade with a growth rate of 2 folds every year. Interestingly, this is just behind the growth of DNN articles by six years. It may potentially suggest that QML will be widely used in numerous research communities in a couple of years, considering the fact that applications of DNN are presently seen nearly everywhere.

It was proved that QNN holds the universal approximation property [50], which shows the close relation between the number of qubits in QNN and the number of DNN layers, and also the number of quantum layers of QNN and the number of hidden nodes in DNNs. Accordingly, increasing the number of qubits may enjoy state-of-the-art DNN performance. More importantly, quantum circuits can be analytically differentiable with a parameter-shift rule [51] that enables stochastic gradient optimization of VQC. Nevertheless, QNN often suffers from a vanishing gradient issue called the barren plateau [52]. To mitigate the issue, some techniques have been studied, e.g, an identity initialization strategy [53] and a simplified two-design (STD) ansatz [54] to cover nearly arbitrary unitary spectrum with shallow staggered entanglers.

B. Quantum Supremacy

Although quantum supremacy over classical computers has been reported for some specific problems [26, 27], the feasibility of realizing quantum advantages for practical problems has still been argued intensively. Nevertheless, it is highly expected that quantum computers could provide breakthroughs in a wide range of research fields. This is particularly due to the known limits of power efficiency for classical computers, especially for deep learning, where training has become extremely energy intensive [55]. For sustainable growth, a new computing modality such as quantum computers is demanded for a future eco-friendly society. Although no one can certainly foresee that QPU will supersede classical computers in future, it is of importance to explore many possibilities.

C. Quantum Neural Network (QNN) Transfer Learning

Fig. 4 depicts QNN using STD ansatz [54], which consists of Pauli-Y rotations and staggered controlled-Z entanglers in sequence. The STD ansatz is a simplified variant of a 2design whose statistical properties are identical to ensemble random unitaries with respect to the Haar measure up to the first 2 moments. For an *n*-qubit VQC, there are 2(n-1)Lvariational parameters $\{\theta\}$ over an L-layer STD ansatz. To embed 36-dimensional beam SNRs, an input linear layer is used to initialize the quantum state for rotation angles of Pauli-Y gates. The 8-class pose estimation is provided by quantum measurements in the Hamiltonian observable of Pauli-Z operations, followed by an output layer to align the dimension. The variational parameters as well as input/output layers are optimized by the adaptive momentum stochastic gradient descent to minimize the softmax cross entropy loss. The QNN model is first trained by labeled data in source domain, and then fine-tuned with few-shot labeled data from the target domain for transfer learning while input/output layers are frozen. While QNN is not necessarily better than DNN in prediction accuracy, the potential advantage of QNN lies in its computational efficiency to manipulate 2^n quantum states at once with a small number of quantum gates.

IV. PERFORMANCE EVALUATION

A. Comparison of ML Methods

We first evaluate the baseline performance in the human pose recognition task without any TL techniques: specifically, ML models are trained using only the labeled data in the source domain and tested in the target domain. Besides DNN and QNN, we compare different ML methods including support vector machine (SVM), decision tree (DT), k-nearest neighbor (kNN), Gaussian naïve Bayes (GNB), random forest (RF), bagging ensemble, and extra tree ensemble methods (10 base models). For DNN, we consider residual 4 hidden layers with 100 hidden nodes using Mish activation, where there are approximately 35k trainable parameters. For QNN, we use 10 qubits with 1-layer STD ansatz [54], dressed by input and output linear layers, where there are 18 quantum variational parameters and 610 classical trainable parameters in total. We use AdamW optimizer for a mini batch size of 100 over 100 epochs with a learning rate of 0.02 and weight decay of 10^{-4} . For simplicity, we consider no quantum noise for simulations.

Fig. 5 shows the test accuracy as a function of the number of labeled training samples in the source domain. One can notice that the performance can exceed an accuracy of 90% for DNN, QNN, and SVM when a sufficient amount of labeled data is available. It is confirmed that a small-scale QNN can achieve performance comparable to a large-scale DNN. Most conventional ML techniques are found ineffective for our pose recognition task.

B. Pose Recognition Analysis

We further discuss pose-wise detection performance in terms of confusion matrix and receiver operating characteristic (ROC) curve in Fig. 6. Here, we present performance of



Fig. 4. Variational QNN using STD ansatz, dressed with input/output linear layers for pose recognition.



Fig. 5. Test accuracy (target domain) vs. training samples (source domain).

SVM, DNN, and QNN when 104 training samples (0.03% data labeled in the source domain) are available to learn those models. From the confusion matrices, the prediction of pose class 4 was found to be the most challenging. It is particularly significant for DNN models in terms of ROC area under curve (AUC) score as shown in Fig. 6(f) for the pose class 4. Although the mean accuracy of DNN was slightly better than that of QNN, QNN outperformed DNN in the sense of macro/micro-averaging ROC-AUC performance.

C. Domain Shift Impact

Although DNN/QNN/SVM showed a reasonable prediction with an accuracy greater than 90% in Fig. 5 for a sufficient size of training data in the source domain, it does not exceed 95%. This is mainly because of the domain shift issues across measurement sessions as shown in Fig. 7, where we present the test accuracy of unlabeled source domain data when training with labeled source domain data. All ML models could achieve nearly perfect accuracy if the test data comes form the same domain. In particular, QNN was significantly better than DNN.

D. Transfer Learning

Fig. 8 shows TL performance for DNN and QNN using few-shot transfer samples from the target domain. Here, the pre-transfer model uses 129 training samples from the source domain. We present mean accuracy with 1-standard deviation zones over 5-times fine tuning. It is confirmed that TL-QNN is comparable to TL-DNN, achieving greater than 95% accuracy over 300 samples. The corresponding confusion matrix and ROC curves for TL-QNN at 104 transfer samples are shown in Fig. 6(d) and (h), respectively. We can observe that the TL can predict the pose class 4 accurately with a significant improvement in ROC-AUC.

V. CONCLUSION

This paper considered transfer learning of DNN and QNN to deal with domain shifts due to changes of Wi-Fi measurements and environments over data sessions for Wi-Fi sensing tasks. Specifically, we demonstrated the benefit of TL through realworld experiments with an in-house Wi-Fi testbed. We showed a small-scale QNN can achieve greater than 90% accuracy, comparable to a large-scale DNN, in human pose recognition. Demonstration on real quantum processors will be provided in a future work. This is a very initial proof-of-concept study for quantum-ready Wi-Fi sensing and there remain many fascinating open issues to solve in future.

ACKNOWLEDGMENT

We thank Jianyuan Yu (Virginia Tech.) for earlier data collection experiments.

REFERENCES

- F. Adib *et al.*, "Capturing the human figure through a wall," ACM Trans. Graph., vol. 34, no. 6, Oct. 2015.
- [2] C.-Y. Hsu et al., "Extracting gait velocity and stride length from surrounding radio signals," in Proceedings of the 2017 CHI Conference on Human Factors in Computing Systems, 2017, pp. 2116–2126.



Fig. 6. Confusion matrices (top row) and ROC curves (bottom row) for 8-pose recognition with 129 training samples (0.3% data labeled in the source domain). TL-QNN uses 104 transfer samples (10% data labeled in the target domain).



Fig. 7. Domain shift analysis with test accuracy (source/target domains) vs. training samples (source domain).

- [3] M. Zhao et al., "Through-wall human pose estimation using radio signals," in 2018 IEEE/CVF Conference on Computer Vision and Pattern Recognition, June 2018, pp. 7356–7365.
- [4] M. Zhao et al., "RF-based 3D skeletons," in Proceedings of the 2018 Conference of the ACM Special Interest Group on Data Communication, 2018, pp. 267–281.
- [5] P. Zhao et al., "mID: Tracking and identifying people with millimeter wave radar," in 2019 15th International Conference on Distributed Computing in Sensor Systems (DCOSS), May 2019, pp. 33–40.
- [6] A. Singh et al., "RadHAR: Human activity recognition from point clouds generated through a millimeter-wave radar," in Proceedings of the 3rd ACM Workshop on Millimeter-Wave Networks and Sensing Systems, 2019, pp. 51–56.
- [7] X. Lu et al., "Robust occupancy inference with commodity WiFi," in 2016 IEEE 12th International Conference on Wireless and Mobile



Fig. 8. Test accuracy vs. transfer samples (labeled data in target domain). Pre-transfer model uses 129 training samples (0.3%) data labeled in source domain).

Computing, Networking and Communications (WiMob), Oct 2016, pp. 1–8.

- [8] Y. Zeng et al., "WiWho: WiFi-based person identification in smart spaces," in 2016 15th ACM/IEEE International Conference on Information Processing in Sensor Networks (IPSN), April 2016, pp. 1–12.
- [9] D. Wu et al., "Device-free WiFi human sensing: From pattern-based to model-based approaches," *IEEE Communications Magazine*, vol. 55, no. 10, pp. 91–97, Oct 2017.
- [10] H. Zou et al., "WiFi-based human identification via convex tensor shapelet learning," in Proceedings of the 2018 AAAI Conference on Artificial Intelligence, 2018, pp. 1711–1718.
- [11] J. Yang *et al.*, "Device-free occupant activity sensing using WiFi-enabled IoT devices for smart homes," *IEEE Internet of Things Journal*, vol. 5, no. 5, pp. 3991–4002, Oct 2018.

- [12] Y. Gu et al., "Emosense: Data-driven emotion sensing via off-the-shelf WiFi devices," in 2018 IEEE International Conference on Communications (ICC), May 2018, pp. 1–6.
- [13] —, "Besense: Leveraging WiFi channel data and computational intelligence for behavior analysis," *IEEE Computational Intelligence Magazine*, vol. 14, no. 4, pp. 31–41, Nov 2019.
- [14] Z. Wang et al., "A survey on human behavior recognition using channel state information," *IEEE Access*, vol. 7, pp. 155 986–156 024, 2019.
- [15] F. Wang et al., "Person-in-WiFi: Fine-grained person perception using WiFi," in Proceedings of (ICCV) International Conference on Computer Vision, July 2019.
- [16] F. Wang *et al.*, "Joint activity recognition and indoor localization with WiFi fingerprints," *IEEE Access*, vol. 7, pp. 80058–80068, 2019.
- [17] Y. Ma et al., "WiFi sensing with channel state information: A survey," ACM Computing Surveys (CSUR), vol. 52, no. 3, pp. 1–36, 2019.
- [18] L. Zhang et al., "WiVi: A ubiquitous violence detection system with commercial WiFi devices," *IEEE Access*, vol. 8, pp. 6662–6672, 2020.
- [19] W. Jiang et al., "Towards 3D human pose construction using WiFi," in Proceedings of the 26th Annual International Conference on Mobile Computing and Networking, 2020, pp. 1–14.
- [20] M. Pajovic *et al.*, "Fingerprinting-based indoor localization with commercial MMWave WiFi–Part I: RSS and beam indices," in 2019 IEEE Global Communications Conference (GLOBECOM), Dec. 2019.
- [21] P. Wang et al., "Fingerprinting-based indoor localization with commercial MMWave WiFi–Part II: Spatial beam SNRs," in 2019 IEEE Global Communications Conference (GLOBECOM), Dec 2019.
- [22] T. Koike-Akino *et al.*, "Fingerprinting-based indoor localization with commercial MMWave WiFi: A deep learning approach," *IEEE Access*, vol. 8, pp. 84 879–84 892, 2020.
- [23] P. Wang et al., "Fingerprinting-based indoor localization with commercial mmwave WiFi: NLOS propagation," in 2020 IEEE Global Communications Conference (GLOBECOM), 2020, pp. 1–6.
- [24] J. Yu *et al.*, "Human pose and seat occupancy classification with commercial MMWave WiFi," in 2020 IEEE Globecom Workshops, 2020, pp. 1–6.
- [25] M. Wang and W. Deng, "Deep visual domain adaptation: A survey," *Neurocomputing*, vol. 312, pp. 135–153, 2018.
- [26] F. Arute *et al.*, "Quantum supremacy using a programmable superconducting processor," *Nature*, vol. 574, no. 7779, pp. 505–510, 2019.
- [27] H.-S. Zhong et al., "Quantum computational advantage using photons," Science, vol. 370, no. 6523, pp. 1460–1463, 2020.
- [28] S. J. Nawaz *et al.*, "Quantum machine learning for 6G communication networks: State-of-the-art and vision for the future," *IEEE Access*, vol. 7, pp. 46 317–46 350, 2019.
- [29] A. Mari et al., "Transfer learning in hybrid classical-quantum neural networks," Quantum, vol. 4, p. 340, 2020.
- [30] K. Bharti et al., "Noisy intermediate-scale quantum (NISQ) algorithms," arXiv preprint arXiv:2101.08448, 2021.
- [31] Z. Babar et al., "EXIT-chart-aided near-capacity quantum turbo code design," *IEEE Transactions on Vehicular Technology*, vol. 64, no. 3, pp. 866–875, 2014.
- [32] P. Botsinis *et al.*, "Iterative quantum-assisted multi-user detection for multi-carrier interleave division multiple access systems," *IEEE Transactions on Communications*, vol. 63, no. 10, pp. 3713–3727, 2015.
- [33] —, "Joint quantum-assisted channel estimation and data detection," *IEEE Access*, vol. 4, pp. 7658–7681, 2016.
- [34] ——, "Quantum search algorithms for wireless communications," *IEEE Communications Surveys & Tutorials*, vol. 21, no. 2, pp. 1209–1242, 2018.
- [35] E. Farhi et al., "A quantum approximate optimization algorithm," arXiv preprint arXiv:1411.4028, 2014.
- [36] E. Farhi and A. W. Harrow, "Quantum supremacy through the quantum approximate optimization algorithm," *arXiv preprint arXiv:1602.07674*, 2016.
- [37] E. Anschuetz et al., "Variational quantum factoring," in International Workshop on Quantum Technology and Optimization Problems. Springer, 2019, pp. 74–85.
- [38] A. Kandala *et al.*, "Hardware-efficient variational quantum eigensolver for small molecules and quantum magnets," *Nature*, vol. 549, no. 7671, pp. 242–246, 2017.
- [39] T. Matsumine *et al.*, "Channel decoding with quantum approximate optimization algorithm," in 2019 IEEE International Symposium on Information Theory (ISIT). IEEE, 2019, pp. 2574–2578.

- [40] T. Koike-Akino et al., "Variational quantum demodulation for coherent optical multi-dimensional QAM," in 2020 Optical Fiber Communications Conference and Exhibition (OFC). OSA, 2020, pp. 1–3.
- [41] M. Schuld *et al.*, "Circuit-centric quantum classifiers," *Physical Review A*, vol. 101, no. 3, p. 032308, 2020.
- [42] E. Farhi and H. Neven, "Classification with quantum neural networks on near term processors," arXiv preprint arXiv:1802.06002, 2018.
- [43] M. Henderson *et al.*, "Quanvolutional neural networks: powering image recognition with quantum circuits," *Quantum Machine Intelligence*, vol. 2, no. 1, pp. 1–9, 2020.
- [44] J. Romero *et al.*, "Quantum autoencoders for efficient compression of quantum data," *Quantum Science and Technology*, vol. 2, no. 4, p. 045001, 2017.
- [45] P. Rebentrost et al., "Quantum support vector machine for big data classification," *Physical review letters*, vol. 113, no. 13, p. 130503, 2014.
- [46] S. Lloyd and C. Weedbrook, "Quantum generative adversarial learning," *Physical review letters*, vol. 121, no. 4, p. 040502, 2018.
- [47] P.-L. Dallaire-Demers and N. Killoran, "Quantum generative adversarial networks," *Physical Review A*, vol. 98, no. 1, p. 012324, 2018.
- [48] G. Verdon et al., "Quantum graph neural networks," arXiv preprint arXiv:1909.12264, 2019.
- [49] D. Steinmetzer et al., "Talon tools: The framework for practical IEEE 802.11ad research," in Available: https://seemoo.de/talon-tools/, 2018.
- [50] A. Pérez-Salinas et al., "Data re-uploading for a universal quantum classifier," Quantum, vol. 4, p. 226, 2020.
- [51] M. Schuld *et al.*, "Evaluating analytic gradients on quantum hardware," *Physical Review A*, vol. 99, no. 3, p. 032331, 2019.
- [52] J. R. McClean *et al.*, "Barren plateaus in quantum neural network training landscapes," *Nature communications*, vol. 9, no. 1, pp. 1–6, 2018.
- [53] E. Grant *et al.*, "An initialization strategy for addressing barren plateaus in parametrized quantum circuits," *Quantum*, vol. 3, p. 214, 2019.
- [54] M. Cerezo *et al.*, "Cost function dependent barren plateaus in shallow parametrized quantum circuits," *Nature communications*, vol. 12, no. 1, pp. 1–12, 2021.
- [55] E. Strubell et al., "Energy and policy considerations for deep learning in NLP," arXiv preprint arXiv:1906.02243, 2019.