Design of a 1 Tb/s Superchannel Coherent Receiver


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Abstract

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I. INTRODUCTION

In order to provide higher optical interface rates, recent research has focused on the expansion of both bandwidth and spectral efficiency (SE) [1], [2]. While some research has focused on the slicing of the received signal in the time [3], [4] or frequency [5] domains, these solutions require several parallel coherent receivers. More recently, detection of 1 Tb/s with a single coherent receiver has been demonstrated with several coherent optical carriers being used to synthesize a single-carrier dual-polarization 32-ary quadrature amplitude modulation (DP-32QAM) signal [6], with a DP-32QAM superchannel [7], and with a DP-64QAM superchannel [8].

In understanding the reason for this approach to increasing interface rates, it is useful to examine the performance of products, proposed products, and experimental records over the last several years, a scatter diagram of which is plotted as SE versus bandwidth in Fig. 1. Coherent systems operating at 100 Gb/s have been a technical and commercial success, relaxing optical plant requirements while requiring only around 3 × the optical bandwidth of 10 Gb/s intensity-modulation direct-detection (IM-DD) systems. While relatively sophisticated transceiver optics were required for 100 Gb/s systems, the increase in SE that they offered was enabled by the use of sophisticated digital signal processing (DSP). A further increase in SE within the same bandwidth has resulted in products which achieve 200 Gb/s with a single carrier. The subsequent increase to 400 Gb/s with a single transmitter and receiver has proven more technically challenging than may have initially been suspected. While real-time single carrier systems operating at 400 Gb/s have been demonstrated [9], proposed systems are currently still undergoing standardization by the Optical Internetworking Forum (OIF) [10].

In this paper, we develop our previous work [8] and provide a thorough exposition of the detailed design of receiver DSP capable of detecting a 1 Tb/s superchannel. In section II, we describe the experimental hardware used for generation and detection of a 1 Tb/s superchannel. In section VII, we then discuss the experimental performance of the various subsystems in section VI, before providing conclusions in section VII.
in order to achieve a flat optical comb with the required number of subcarriers. The subcarriers were then separated into odd and even channels by cascaded interleavers, before modulation using single polarization I/Q modulators. Two field-programmable gate arrays (FPGAs) were used to send the in-phase and quadrature components of the desired waveforms to a pair of digital-to-analog converters, operating at 20 GSa/s. The 10 Gbd, 8-level signals were generated from decorrelated to a pair of digital-to-analog converters, operating at 20 GSa/s. The electrical signals were digitized using an oscilloscope with 160 GSa/s analog-to-digital converters and 63 GHz of bandwidth, before being processed offline using Matlab.

### III. Receiver Digital Signal Processing

In our previous work [17], we noted that the limit of achievable signal-to-noise ratio (SNR) for high order modulated signals was reasonably high, but the use of blind receiver algorithms can cause significant impairments – particularly when the SNR is poor. The receiver DSP design therefore consists of two main components. The receiver was initially operated in training mode in order to estimate the equalizer taps for each of the subchannels, the SNR on each subchannel, and the centroid of each possible symbol on each of the polarization subchannels. After training, the receiver was switched to pilot-aided (PA) operation. In this mode, information from periodic pilot symbols was used in combination with channel statistics to update the adaptive equalizer and carrier phase estimate.

For all cases, the received signal was initially de-skewed and normalized on a per-quadrature basis to correct for imperfections in the receiver front-end. After this, the input signal was demultiplexed into constituent subcarriers, and each subcarrier resampled to two samples per symbol. A digital anti-aliasing filter was used before resampling, in order to prevent aliasing induced crosstalk. The filter was wide enough to avoid in-band distortion of the received signal subcarriers.

### IV. Receiver Training DSP Algorithms

For each subchannel, initial blind estimation of intradyne-frequency (IF) is performed. Coarse estimation of the timing phase is performed with a dual-polarization (DP) constant modulus algorithm (CMA) equalizer, with least-mean square (LMS) tap updating. The output symbols from this equalizer are then raised to the power of 4, and the resultant spectrum is used to determine the IF for each subcarrier.

Initial processing in training mode was performed using a blind (DP-CMA) with LMS updating, followed by Viterbi & Viterbi 4th power carrier phase estimation [18]. This enabled sufficiently accurate signal recovery to perform synchronization of the received signal with the training sequence.
A. Equalizer training

For each subchannel, a DP radius-directed equalizer (RDE) with LMS updating was used to equalize polarization rotations and filtering impairments, and to recover the timing phase. The output \( v \) of the equalizer at time \( k \), for polarizations \( x \) and \( y \) is given by

\[
\begin{align*}
  v_x(k) &= h_{xx}^H u_x + h_{xy}^H u_y, \\
  v_y(k) &= h_{yx}^H u_x + h_{yy}^H u_y,
\end{align*}
\]

where \( u_x \) and \( u_y \) are the input (column) vectors for the \( x \) and \( y \) polarizations, \( H \) denotes the Hermitian transpose, and the four FIR filter vectors are \( h_{xx}, h_{xy}, h_{yx} \) and \( h_{yy} \).

The equalizer was trained based on the radius of the symbols in the training sequence. The trained equalizer error terms were calculated with the following equations:

\[
\begin{align*}
  e_x(k) &= |T_x(k)|^2 - |v_x(k)|^2, \\
  e_y(k) &= |T_y(k)|^2 - |v_y(k)|^2,
\end{align*}
\]

where \( T_x(k) \) and \( T_y(k) \) are the training symbols at time \( k \) on the \( x \) and \( y \) polarizations, respectively. This leads to the LMS update for the filters given by:

\[
\begin{align*}
  h_{xx}' &= h_{xx} + \mu e_x(k) u_x v_x^*(k), \\
  h_{xy}' &= h_{xy} + \mu e_x(k) u_y v_y^*(k), \\
  h_{yx}' &= h_{yx} + \mu e_y(k) u_x v_y^*(k), \\
  h_{yy}' &= h_{yy} + \mu e_y(k) u_y v_y^*(k),
\end{align*}
\]

where the conjugation operator is denoted by \(^*\).

By using a trained equalizer adapted only on the radius of the received signals, we were able to attain excellent equalization of the signal with unconstrained phase. This enabled us to have an equalization structure which could adapt slowly in response to the slowly varying polarization channel, while phase tracking could be performed with a significantly higher rate of tracking.

B. Carrier phase estimation training

Carrier phase estimation (CPE) was performed using a data-aided feedforward algorithm, somewhat similar to the non-data-aided algorithm proposed in [19]. A phase estimate \( \phi \) is calculated at time \( k \) by multiplying the Hermitian transpose of an input vector \( v \) with the training symbol vector \( T \), and taking the complex argument:

\[
\phi(k) = \arg(v^H T).
\]

We note that this phase estimate does not require unwrapping, as it is already on the interval \((-\pi, \pi]\). The input signal \( v \) is then corrected for phase at instant \( k \), to produce a phase corrected output \( r \) according to:

\[
r(k) = v(k)e^{j\phi(k)}.
\]

C. Centroid calculation

After correcting for the phase noise on the training sequence, we were able to calculate the centroid of each of the 64 constellation points, and the SNR for each of the 22 polarization subchannels. For each symbol \( s \) in the set of symbols \( S \), a new symbol \( s' \) was calculated as the complex mean of the received training symbols \( r \) which correspond to transmitted training symbols \( t \) being equal to \( s \) as follows:

\[
s' = \mathbb{E}(r| t = s), \quad \forall s \in S,
\]

where \( \mathbb{E} \) denotes expectation. The new set of distorted symbols \( S' \) were subsequently used in the pilot-aided CPE, and the calculation of bit log-likelihood ratios (LLRs) [20].

V. PILOT-AIDED DSP ALGORITHMS

After training had led to a well converged equalizer, with accurately calculated IF offsets and constellation centroids, the receiver was switched to pilot-aided operation, with a 1% pilot-insertion ratio (PIR). A schematic of the pilot-aided receiver operation is shown in Fig. 5. The frequency subchannels were prepared as before, with IF correction and matched RRC filtering being performed before any pilot-aided processing.
A. Pilot-aided equalization

The equalizer taps previously calculated during training mode were used as the initial state of the pilot-aided equalizers. A pilot-aided DP-CMA (PA-DP-CMA) algorithm was used for each frequency subcarrier, with the error calculation being performed only for the pilot symbols (rather than every symbol during training mode). A schematic of this equalizer can be seen in Fig. 6. We note again that this equalizer structure is – like the conventional DP-RDE algorithm – immune to the effects of phase noise [21]. However, unlike the DP-RDE, the PA-DP-CMA algorithm is immune to the effects of noise artifacts introduced by incorrect decisions in the equalizer.

The pilot-aided equalizer was adapted according to the following equations:

\[ e_x(k) = \frac{1}{10} \sum_{i=0}^{9} (|P_x(k - 100i)|^2 - |v_x(k - 100i)|^2), \quad (11) \]

\[ e_y(k) = \frac{1}{10} \sum_{i=0}^{9} (|P_y(k - 100i)|^2 - |v_y(k - 100i)|^2), \quad (12) \]

where \( P_x(k) \) and \( P_y(k) \) are pilot symbols at time \( k \) on the \( x \) and \( y \) polarizations, respectively. This leads to the LMS update for the filters given by (4)–(7).

B. Pilot-aided carrier phase estimation

First, we describe in detail the multi-pilot-aided CPE algorithm which we have previously proposed [22] and experimentally demonstrated [23]. Then, we generalize it for joint carrier phase estimation of multiple channels when phase evolution is correlated over several wavelength subchannels.

We assume that \( N \) information symbols are transmitted in a block and that each block starts with a pilot symbol. To estimate phase of a symbol transmitted during the \( L \)th signaling interval, we use \( L_1 \) pilots preceding and \( L_2 \) pilots following the considered symbol, and without loss of generality assume \( L_1 = L_2 = L \). Therefore, phases of information symbols belonging to the same block are estimated using the same set of pilots \( P = \{ p(1), \ldots, p(L), p(L + 1), \ldots, p(2L) \} \). Note that a single pilot might belong to more than one set of pilots. Also note that phases of information symbols from different blocks are estimated with the aid of different sets of pilots. For example, phases of the symbols between pilots \( p(2) \) and \( p(3) \) in Fig. 7 are estimated using pilots \( p(1), p(2), p(3) \) and \( p(4) \).

1) Phase noise model: Assuming all signal impairments but phase and additive noise have been compensated, a sample of the received signal at discrete time \( k \), \( v(k) \), is related to
the symbol transmitted in the corresponding signaling interval, \( s(k) \), as
\[
v(k) = s(k)e^{j\theta(k)} + n(k),
\]
where \( \theta(k) \) and \( n(k) \) are, respectively, the samples of a real phase noise and complex circularly symmetric additive white Gaussian noise (AWGN). That is, \( n(k) \sim CN(0, \sigma_n^2) \), while \( \theta(k) \) is modeled as a Wiener process, i.e.,
\[
\theta(k) - \theta(k - 1) \sim \mathcal{N}(0, \sigma_\theta^2), \quad \sigma_\theta^2 = 2\pi\Delta\nu\tau_s, \tag{14}
\]
where \( \Delta\nu \) is the combined linewidth of transmitter’s and receiver’s lasers and \( \tau_s \) is the symbol period. Since the consecutive pilots \( p(\zeta) \) and \( p(\zeta + 1) \) are separated by \( N + 1 \) signaling intervals (i.e., by \( N \) information symbols), we note using (14) that
\[
\theta_p(\zeta + 1) - \theta_p(\zeta) \sim \mathcal{N}(0, (N + 1)\sigma_\theta^2), \tag{15}
\]
where \( \zeta = 1, \ldots, 2L - 1 \).

We frame the phase estimation problem by means of the statistical inference with the goal to compute/approximate the probability distribution of unknown phase \( \theta(k) \), conditioned on the transmitted and received signals at pilot locations. That is, the proposed algorithm approximates \( \Pr(\theta(k)|v(k), s_p(\zeta), v_p(\zeta), \zeta = 1, \ldots, 2L, k = 1, \ldots, N) \), which is carried out through the steps outlined in Fig. 8.

2) Inference of Pilot Phases: Initially, the algorithm approximates the posterior distribution \( \Pr(\theta_p(\zeta)|s_p(\zeta), v_p(\zeta)) \) of an unknown phase of pilot location \( p(\zeta) \), given the corresponding transmitted pilot symbol \( s_p(\zeta) \) and received signal \( v_p(\zeta) \). This posterior can be, in principle, evaluated using the Bayes’ rule and model (13). However, this approach does not yield a closed form expression for the posterior distribution and we thus approximate it. Using the Laplace approximation [24], the pilot symbol phases are approximated (after few steps of derivations which are omitted here) as
\[
\theta_p(\zeta)|s_p(\zeta), v_p(\zeta) \sim \mathcal{N}(\mu_p(\zeta), \sigma_p^2(\zeta)), \tag{16}
\]
where
\[
\mu_p(\zeta) = \arg\{v_p(\zeta)s_p^*(\zeta)\}, \tag{17}
\]
and
\[
\sigma_p^2(\zeta) = \frac{\sigma_n^2}{2|\sigma_p(\zeta)V_p(\zeta)|}. \tag{18}
\]
Note that the above computations are performed for each pilot in parallel.

After this initial step, we evaluated the posterior \( \Pr(\theta_p(k)|s_p(\zeta), v_p(\zeta), \zeta = 1, \ldots, 2L) \) of the pilot \( p(k) \)’s (\( k = 1, \ldots, 2L \)) phase, conditioned on the knowledge of the transmitted symbols and received signals corresponding to all pilots from the set \( P \). In doing so, we use the Kalman filtering framework. Towards that end, we need to specify the underlying linear dynamical model and observation model.

The linear dynamical model is simply the Wiener phase noise model in (14). On the other hand, the observation model is constructed as
\[
\psi_p(\zeta) = \theta_p(\zeta) + n_p(\zeta), \tag{19}
\]
where
\[
\psi_p(\zeta) = \mu_p(\zeta), \tag{20}
\]
and
\[
n_p(\zeta) \sim \mathcal{N}(0, \sigma_n^2), \tag{21}
\]
where \( \mu_p(\zeta) \) and \( \sigma_n^2(\zeta) \) are as evaluated in (17) and (18). Intuitively, \( \psi_p(\zeta) \) is a noisy “observation” of an unknown phase, where \( n_p(\zeta) \) is the observation noise.

Applying the Kalman smoother with linear dynamical (14) and observation model (19) yields
\[
\theta_p(\zeta)|s_p(1), v_p(1), \ldots, s_p(2L), v_p(2L) \sim \mathcal{N}(\mu_p(\zeta), \sigma_p^2(\zeta)), \tag{22}
\]
where mean \( \mu_p(\zeta) \) and variance \( \sigma_p^2(\zeta) \) are evaluated using the forward and backward pass through the model.

In fact, 22 is the only step in our method which requires sequential processing. To speed up this processing step, we can reduce the number of pilots in the set \( P \). In fact, our study shows that for 64-QAM and for relevant phase noise regimes, increasing the number of pilots \( 2L \) beyond 4 provides only negligible performance gains. Also, this step requires a backward pass which stops at pilot \( p(L + 1) \), which saves us from doing \( L \) steps in the backward pass (refer to (24)).

Alternatively, the processing in this step could also be done in parallel if the computational resources allow for performing inversion of a matrix of size \( 2L \) on each pilot. This is also a reasonable approach since \( 2L = 4 \) already brings us to the edge of possible performance improvements for the systems of our interest.

3) Estimation of Information Symbol Phases: In this stage, initial estimates of the information symbol phases are obtained by interpolating between pilots symbol phases, estimated in the previous stage. The initial phase estimates are then refined by means of the expectation maximization (EM) method [24].

Recalling that the information symbols are between pilots \( p(L) \) and \( p(L + 1) \) and using Wiener process model for phase noise (14), it is shown that the posterior \( \Pr(\theta(k)|s_p(\zeta), v_p(\zeta), \zeta = 1, \ldots, 2L) \) is Gaussian distributed with mean and variance dependent upon means and variances of Gaussian posteriors corresponding to the pilots \( p(L) \) and \( p(L + 1) \).

More precisely, it can be shown that
\[
\theta(k)|s_p(1), v_p(1), \ldots, s_p(2L), v_p(2L) \sim \mathcal{N}(\mu_k, \sigma_k^2), \tag{23}
\]
where
\[
\mu(k) = \frac{(N + 1 - k)\sigma_p^2(\tilde{p}_p) + (k\sigma_p^2 + \sigma_n^2)p(\zeta + 1)}{(N + 1)\sigma_p^2 + \sigma_n^2}}, \tag{24}
\]
where \( \tilde{p}_p(L) \) is the mean of the resulting distribution obtained from Kalman’s forward pass corresponding to pilot \( p(L) \),
while \( \nu_p(L+1) \) is the mean of the resulting distribution obtained from the Kalman’s backward pass corresponding to pilot \( p(L+1) \). As mentioned in the previous part, the backward pass ends on pilot \( p(L+1) \). Note that (24) is performed in parallel on all information symbols within a block.

The estimates of the information symbol phases in (24) are then refined by employing the EM algorithm. Note that the application of the EM algorithm is well suited after reasonably accurate phase estimates have been obtained. Namely, due to a non-convex nature of the underlying optimization function, the EM algorithm converges to a local stationary point closest to the initial point. Therefore, the EM algorithm needs to be initialized with a phase estimate that is already reasonably close to the true phase to yield better phase estimate.

A separate EM procedure refines the phase estimate of each information symbol in parallel. In the following, we present the computations involved and skip the derivation details. The EM routine on symbol \( s(k) \) is initialized with \( \hat{\theta}(0)(k) = \mu(k) \), where \( \mu(k) \) is the phase estimate obtained from (24). The q-th iteration starts with evaluating the likelihood of symbol \( s(k) \) given the received signal \( v(k) \) and phase estimate \( \hat{\theta}(q-1)(k) \), obtained from the iteration \( q-1 \). This likelihood is up to the normalization constant given by

\[
\Pr(s(k) = a|v(k); \hat{\theta}(q-1)(k)) = \frac{\exp\left(-\frac{1}{\sigma^2_a} |v(k) - ae^{j\hat{\theta}(q-1)(k)}|^2 \right)}{\Pr(v(k)|a; \hat{\theta}(q-1)(k))} \Pr(s(k) = a; \hat{\theta}(q-1)(k))
\]

(25)

where \( s(k) \) takes values from the transmitted constellation, i.e., \( a \in S \), and without loss of generality we assume that transmitted symbols are equally likely. The symbol likelihoods are then used to update the phase estimate as

\[
\hat{\theta}(q)(k) = \arg \left( \sum_{a \in S} a^* \Pr(s(k) = a|v(k); \hat{\theta}(q-1)(k)) \right).
\]

(26)

The EM algorithm is performed until a termination condition is satisfied, e.g., until a predefined number of iterations \( Q_{\max} \). To reduce the computational complexity, the number of iterations \( Q_{\max} \) can be kept to a small value. Our study shows that the algorithm converges after 2 iterations and no improvement is made by using more than 2 iterations. Additionally, the complexity burden arising from computing the symbol likelihoods for high order modulation formats (such as 64-QAM or 256-QAM) can be alleviated by taking into account only the constellation points close to the initial soft symbol estimate obtained by applying initial phase estimate (24) onto corresponding received signal \( v(k) \).

The EM procedures are performed separately on information symbols (and thus in parallel) such that the correlation structure of phase variations across symbols is not exploited. We point out that in principle it is possible to formulate the EM procedure which takes into account the statistics of phase variations. However, the phase estimates in such a procedure are not given in closed forms. More importantly, such a procedure does not admit parallel implementation and is therefore not practical.

To overcome the shortcoming of not taking into account the statistics of phase variations in the EM procedures, the proposed method filters the EM phase estimates \( \hat{\theta}(Q_{\max})(k) \) by applying a moving average filter of length \( 2L_F \). That is, the final phase estimate is computed as

\[
\hat{\theta}(k) = \frac{1}{2L_F + 1} \sum_{i=k-L_F}^{k+L_F} \hat{\theta}(Q_{\max})(i),
\]

(27)

where \( \hat{\theta}(Q_{\max}) \) is the phase estimate obtained as a result of the EM step.

The described method outputs the phase estimates of the information symbols. In addition, we can apply these phase estimates on the received symbols and output soft and/or hard estimates of the transmitted symbols.

4) Generalization to Multiple Channels: In this part, we generalize the described method for CPE of a single channel to the case where phase noise variations across multiple channels (e.g., x and y polarizations of a single wavelength channel or all x and y polarizations of channels in a superchannel) are correlated.

We denote with \( C \) the number of channels in a multi-channel system. The signal received in channel \( c \) at time \( k \) is modeled as

\[
v_c(k) = s_c(k)e^{j\theta_c(k)} + n_c(k), \quad c = 1, 2, \ldots, C,
\]

(28)

where \( s_c(k) \) is the transmitted symbol, \( \theta_c(k) \) is phase and \( n_c(k) \) is noise, all corresponding to channel \( c \) at discrete time \( k \). The noise is modeled as \( n_c(k) \sim CN(0, \sigma^2_{n(c)}) \). Note that the variance of the additive noise is not necessarily the same in different channels.

Each channel transmits a block of information symbols, preceded by a pilot symbol. The phase estimation of information symbols within a block is aided with \( L \) pilots preceding and \( L \) pilots following the block. In general, the number of pilots used on each side and in each channel can be different.

Our phase estimation method proceeds in a similar way as for a single channel case. That is, the means \( \mu_p(c, \zeta) \) and variances \( \sigma^2_p(c, \zeta) \) of approximating Gaussian posteriors of pilot symbol phases are evaluated for each pilot in each channel by using (17) and (18). The initial pilot phase estimates are processed using the Kalman filtering framework. In comparison to a single channel case, the phases of pilots across channels and polarizations appearing at the same discrete time are collected into a state vector \( \theta_{p(c, \zeta)} = [\theta_{p(1, \zeta)} \ldots \theta_{p(2C, \zeta)}] \). We assume the linear dynamical model for state vector is given by

\[
\theta_{p(c+1)} - \theta_{p(c)} \sim \mathcal{N}(0, (N+1)\sigma^2_{C})\), \quad \zeta = 1, \ldots, 2L - 1,
\]

(29)

where \( C \) is a matrix of correlation coefficients between phase noise jumps across channels and polarizations. This correlation matrix is predefined or estimated in the training mode. The observation model is similarly to a single channel case given by

\[
\psi_{p(c)} = \theta_{p(c)} + \mathbf{n}_{p(c)}, \quad \zeta = 1, \ldots, 2L,
\]

(30)

where the observed vector \( \psi_{p(c)}^T = [\mu_{p(c)}^T, \mathbf{n}_{p(c)}^T] \sim \mathcal{N}(0, \Sigma_{p(c)}) \), where \( \Sigma_{p(c)} = \text{diag}(\sigma^2_{p(1, \zeta)}, \ldots, \sigma^2_{p(2C, \zeta)}) \).
Given the linear dynamical and observation model, the proposed method processes the initial pilot phase estimates via full forward pass of Kalman filtering and backward pass of Kalman smoothing up to pilot $p(L + 1)$. The outputs of this processing stage are the mean vector $\hat{\mu}_{p(L)}$ and covariance matrix $\hat{\Sigma}_{p(L)}$ corresponding to the pilot $p(L)$, obtained from the forward pass, as well as the mean vector $\nu_{p(L+1)}$, corresponding to the pilot $p(L + 1)$, resulting from the backward pass.

Note that each step of sequential processing required in the Kalman stage performs matrix inversion, where the matrix size is equal to $2C$, i.e., all polarizations and channels. To alleviate the computational burden, one may reduce the number of pilots $2L$ aiding phase estimation. Our study with 64-QAM shows that using more than 4 pilots (2 on each side) provides no further gains.

The second stage of the proposed method first delivers initial estimates of information symbol phases, obtained from interpolating between phases corresponding to pilots $p(L)$ and $p(L + 1)$, inferred in the previous stage. Conceptually, one can interpolate between two Gaussian vectors (inferred phases across channels at locations $p(L)$ and $p(L + 1)$). However, this would necessitate computing $N$ matrix inversions (one for each information symbol in a block). To alleviate this shortcoming, we perform interpolation between phases in each channel separately. Therefore, the initial phase estimate of a symbol $k$ in channel $c$ is computed by

$$\mu(c, k) = \frac{(N + 1 - k)\sigma^2_{\nu_{p(c,L)}} + (k\sigma^2_\rho + \hat{\sigma}^2_{p(c,L)})\nu_{p(c,L+1)}}{(N + 1)\sigma^2_\rho + \hat{\sigma}^2_{p(c,L)}},$$

where $\hat{\mu}_{p(c,L)}$ and $\nu_{p(c,L+1)}$ are the $c$-th entries in respectively $\mu_{p(L)}$ and $\nu_{p(L+1)}$, while $\hat{\sigma}^2_{p(c,L)}$ is the $c$-th diagonal element of $\hat{\Sigma}_{p(L)}$.

The initial phase estimates of information symbols are then refined using the EM procedure as previously detailed. The EM procedure is applied to each information symbol in each channel in parallel. The details are the same as for a single channel case. Note that the correlations between phases in different channels are not taken into account by running separate EM procedures. Conceptually, the EM procedures can be devised so as to account for these correlations. However, this would require more complicated routines for updating phase estimates. More specifically, a vector of phase estimates across channels at some discrete time would be updated as a vector which minimizes the corresponding objective function and is not given in a closed form.

The final phase estimates are obtained by filtering the EM phase estimates with the moving average filter applied in each channel separately. The outputs from the moving average filter are the final phase estimates. They can be applied to the received signal to yield soft and/or hard estimates of the transmitted symbols.

### C. Forward Error Correction Coding

After CPE was performed, we calculated bit-wise LLRs with the modified signal set calculated in (10). As we previously noted, this method of LLR calculation allowed us to mitigate the impact of imperfect modulation [20]. We then de-interleaved the signal over all subchannels, such that each codeword contained approximately equal proportions of each of the bit-positions and subchannels. This enables the system performance to be determined by the average generalized mutual information (GMI), rather than the worst subchannel or bit position [25]. Following this, we normalized the bit LLRs such that each bit was detected as though ‘0’ was transmitted. This enabled us to test a variety of LDPC codes, by decoding the all zero codeword, which exists in all linear codes. Although we manipulated the LLR signs, no LLR values were changed, and the information content of the signal was preserved.

We used a check-concentrated irregular low-density parity-check (LDPC) (105600,82368) code [26] with rate 0.78 for the inner code. LDPC decoding was performed with 60 iterations of the sum-product algorithm, and flooding scheduling. While this is a somewhat large number of iterations for an LDPC decoder (compared with, for example, 16 iterations used in [27]), we do not consider this to be of itself a condition for high decoder complexity. Decoder complexity and latency is discussed in detail in our work presented in [28], wherein we analyze the effects of degree distribution, iteration count, and other topics which are beyond the scope of this work.

We assumed the use of an outer Bose–Chaudhuri–Hocquenghem (BCH) (30832,30592) code (rate 0.9922) [29] with minimum Hamming distance of 33. We have calculated a union (upper) bound of $10^{-15}$ on the outer decoder output bit error rate (BER) given an input BER of $5 \times 10^{-5}$. Therefore, the input BER threshold for this outer code is at or above an input BER of $5 \times 10^{-5}$. Alternatively, a BER of $5 \times 10^{-5}$ or less at the output of the LDPC decoder can be successfully decoded to $10^{-15}$ or lower when the previously described outer BCH code is used.

### VI. Results

The results presented in this section describe successful measurement of a 1 Tb/s superchannel back-to-back, and without optical noise loading.

By training all 11 of the $2 \times 2$ DP-RDE equalizers independently, we are able to achieve equalization with very low DSP penalty. We note from the taps for the central subchannel (shown in Fig. 9), that the impulse response of the channel is longer than may be expected, and 301 taps were required for good performance. We attribute this to filtering effects from the receiver photodiodes and ADCs, which are operating at extremely high frequencies (more than 50 GHz).

We note from the experimental measurement shown in Fig. 10, that the output phases are as expected – highly correlated between polarization subchannels. We also note that there are varying offsets between these subchannels which remain approximately constant. This is due to the difference in optical path lengths seen by each subchannel, including differences introduced by polarization and frequency sensitive components.

By examining the BER after the CPE has been performed, we noted a wide variation in performance from $8 \times 10^{-3}$ to
Fig. 9. Absolute value of the converged equalizer taps for the central subchannel after the training period. Note the long response time of the system, necessitating a long equalizer of 301 taps.

Fig. 10. Estimated carrier phases, from multi-channel pilot-aided estimation algorithm. Note the high degree of similarity between the estimated phases.

Fig. 11. Measured bit error rate for each polarization of the 11 frequency subchannels. Note the wide variation in performance for different frequencies.

1.4 × 10⁻³ over the different frequency subchannels (although performance between different polarizations on the same frequency was approximately equal), in Fig. 11. We speculate that this variation in performance may be due to imperfect balancing of the optical comb, in combination with the high loss in the optical comb equalizer and deinterleaver. The combination of these effects may have caused variation in the noise figure of the transmitter EDFAs over the range of frequencies in the superchannel. While it is not possible to determine the origin of a source of additive noise from post-processing alone, we may make some reasonable deductions. Due to the uneven nature of both the BER and measured subchannel SNRs, and the accurate and highly correlated recovered carrier phase, we believe that the variation in performance is unlikely to be due to analog electronic or DSP subsystems, while the variation in optical powers in the optical comb after deinterleaving and equalization seems to be a likely culprit for this distortion.

Despite this variation in the effective SNR over the different subchannels, we note that our pilot-aided CPE algorithm is sufficiently robust that the phases of all subchannels are recovered without cycle slips or significant failures in estimation. While a detailed comparison of pilot-aided and non-pilot-aided CPE algorithms is beyond the scope of this work, we would like to direct the interested reader to our previous work on this topic in [22] and [23].

The convergence of the LDPC decoder is shown in Fig. 12. We note that despite the large variation in pre-FEC BER, convergence is still possible, and the sum-product decoder has achieved an output below the threshold of the outer code in 47 iterations, while after 55 iterations, no bit errors are detected in any of the 74 codewords detected (∼7.8 million bits).

The union bound on input BER for a given output BER is shown in Fig. 13. By calculating a lower bound on the input BER for a given output BER of 10⁻¹⁵, we have determined that the threshold for this code is at or above 5 × 10⁻⁵.

VII. CONCLUSIONS

We have described in detail the design of a digital coherent receiver that is capable of detecting a 1 Tb/s superchannel. The optical transmitter and receiver used in the experiment were described in detail. Receiver training was described in
proposed for this system, with an inner rate 0.78 LDPC code and an outer BCH code which can correct an input BER of $5 \times 10^{-5}$ to an output BER of $10^{-15}$ or lower. We note that all algorithms used in this work are of moderate complexity, and suitable for parallel implementation in hardware.

Results were then given, demonstrating operation at a net data-rate of more than 1 Tb/s with a single digital coherent receiver. A Nyquist-spaced coherent superchannel, consisting of $11 \times 10$ Gbd DP-64QAM (gross bit rate of 1.32 Tb/s) was detected with an ultra-high bandwidth receiver. Pilot-aided DSP algorithms of moderate complexity and suitable for hardware implementation were used, enabling robust performance over varying subchannel SNRs with 1% pilot symbols. An inner LDPC code and an outer BCH code were used, with combined overhead of 29.2%, resulting in a net bit-rate of 1.012 Tb/s.

REFERENCES


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