Outdoor-to-Indoor Office MIMO Measurements and Analysis at 5.2 GHz

Shurjeel Wyne, Andreas Molisch, Peter Almers, Gunnar Eriksson, Johan Karedal, Fredrik Tufvesson

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Abstract

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201 Broadway, Cambridge, Massachusetts 02139
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Index Terms—Angular dispersion, channel sounding, direction-of-arrival (DOA), direction-of-departure (DOD), Kronecker model, line-of-sight (LOS) power factor, multiple-input multiple-output (MIMO), Rician K-factor, virtual channel representation (VCR), Weichselberger model.

I. INTRODUCTION

MULTIPLE-INPUT–multiple-output (MIMO) systems can result in tremendous capacity improvements over single-antenna systems [1], [2]. However, the capacity gains depend on the propagation channel in which the system operates. The most important requirement for any channel model is agreement with reality; hence, the measurement of propagation channels and the subsequent parameterization of models based on these measurements are critically important. There have been a number of double-directional outdoor-to-outdoor and indoor-to-indoor measurement results reported in the literature, e.g., [3]–[7]. However, there has been a remarkable lack of outdoor-to-indoor measurement results, although the outdoor-to-indoor scenario has important applications for voice–data transmission in third-generation cellular systems as well as wireless local area networks. The measurement campaign reported in this paper (first published in [8]), together with [9] and [10], is the first published result of outdoor-to-indoor measurements characterizing the MIMO channel.

There are two main categories of channel models for MIMO systems, both of which will be used in this paper. The double-directional channel models [3] describe the MIMO channel by parameters of the multipath components (MPCs): direction-of-departure (DOD), direction-of-arrival (DOA), delay, and complex amplitudes. A double-directional channel characterization is highly useful because it is independent of antenna configurations, describes the physical propagation alone, and serves to point out the dominant propagation mechanisms. On the other hand, analytical channel models describe the statistics of the transfer function matrix. Each entry in that matrix gives the transfer function from the ith transmit to the jth receive antenna element. Almost all of the analytical channel models, with the exception of the keyhole model [11], are based on the assumption that the entries of the transfer function matrix are zero-mean complex Gaussian, with the possible addition of a line-of-sight (LOS) component. Furthermore, many models describe the correlation matrix of those entries as a Kronecker product of the correlation matrices at the transmit and receive sides. The first assumption has, to our knowledge, generally remained unquestioned. 1 The Kronecker assumption has been

1With the exception of the rare “keyhole scenario” (see [11] and [12]).
recently more extensively discussed [7], [13]. Considering that
the measurement data from outdoor scenarios seem to indicate
good agreement with this assumption [13], the indoor data seem
to deviate more [14], and, as a consequence, a more general
model has, e.g., been developed by Weichselberger et al. [7].

In this paper, we present the results of a double-directional
MIMO channel measurement campaign for an outdoor-to-
indoor office scenario (carried out at 5.2 GHz) and evaluate
the validity of the standard assumptions of analytical channel
models (the first results were published in [15]). Our main
contributions are the following.

• We analyze the DOD and DOA and discuss the dominant
  propagation mechanisms.
• We give the distributions of root-mean-square (RMS) di-
  rectional spreads and delay spreads.
• We present a statistical analysis of the measured fading and
  compare it with popular models.
• We investigate the validity of the “LOS-plus-Gaussian-
  remainder” assumption and show that it does not hold for
  all measurement locations in our campaign.
• We explain this result by investigating in detail the differ-
  ence between “LOS power factor” and “Rician $K$-factor.”
• We analyze the validity of the Kronecker model and
  present detailed results on the coupling between DOAs
  and DODs.

This paper is organized as follows. Section II describes the
measurement setup and scenario and the procedure for data
evaluation. In Section III, the physical propagation processes
are described. Furthermore, Section IV contains an analy-
thesis of the dispersion in angular and delay domains, and
Section V compares three analytical channel models. Finally, in
Section VI, we summarize the results.

II. MEASUREMENT SETUP AND EVALUATION

A. Equipment and Scenario

For the measurements, we used the RUSK ATM [16] channel
sounder to measure the transfer function between transmit
(Tx) and receive (Rx) antenna elements. This sounder uses
the multiplexing principle (subsequently connecting the Tx,
and Rx, antenna elements to the radio frequency chains) for
obtaining MIMO transfer function matrices. The measurements
were performed at a center frequency of 5.2 GHz and a signal
bandwidth of 120 MHz using a transmit power of 33 dBm.
The Tx antenna was an eight-element dual-polarized uniform
linear array (ULA) of patch elements with element spacing
$\approx \lambda/2$ (half wavelength). We only considered the eight verti-
cally polarized elements in our analysis. The Rx antenna
was a 16-element uniform circular array (UCA) of vertically
polarized monopole elements (radius $\approx \lambda$). Both array con-
fugurations were calibrated prior to measurement so that the
array response data were available for the application of high-
resolution algorithms. The Tx signal had a period of 1.6 $\mu$s,
and the sampling time for one MIMO snapshot was 819 $\mu$s, which is
within the coherence time of the channel. At each Rx location,
13 snapshots were measured with a time spacing of 4.1 ms be-
tween successive snapshots. Our measurement results directly
give the channel transfer function matrix sampled at 193 fre-
quency subchannels. For the double-directional channel char-
acterization, we needed the parameters like delay, DOA, DOD,
and complex amplitude of the MPCs. Those were obtained
with the high-resolution SAGE algorithm [17] (see Section II-B
for details).

The test site is the E building at Lund University, Lund,
Sweden. A map of the site is shown in Fig. 1. The transmitter
was placed at three different positions on the roof of a nearby
building. For each Tx position, the receiver was placed at 53
measurement positions located in eight different rooms and
the corridor between the rooms. The measurement positions in
each room were placed on a $3 \times 3$ grid spanning an area of
approximately $6 \times 3$ m$^2$. The three positions in the north–south
direction were denoted north, middle, and south, and the three
positions in the east–west direction were denoted east, middle,
and west. The Rx position in a room was described by a pair of
letters suffixed to the room number to indicate the north–south
and east–west positions, respectively. As a sample result,
Fig. 1 shows the strongest four of the estimated MPCs for Tx
position 1 and receiver placed at 2334 NM.

B. SAGE Analysis

1) Signal Model: The data evaluation is based on the as-
sumption that the received and transmitted signals can be
described as a finite number of plane waves [18], i.e.,
\[ h_{m,n}(k,i,\alpha_l,\tau_l,\phi_{l}^{\text{Rx}},\phi_{l}^{\text{Tx}},\nu_l) = \sum_{l=1}^{L} \alpha_l e^{-j2\pi f_{\nu_l}k} G_{\text{Tx}}(n,\phi_{l}^{\text{Tx}}) G_{\text{Rx}}(m,\phi_{l}^{\text{Rx}}) e^{j2\pi \Delta f_{\nu_l} i} \] (1)

where \( L \) is the total number of extracted MPCs, and \( \alpha_l, \tau_l, \phi_{l}^{\text{Rx}}, \phi_{l}^{\text{Tx}}, \) and \( \nu_l \) are the complex amplitude, delay, DOA in azimuth, DOD in azimuth, and Doppler frequency, respectively, of the \( i \)th MPC. The impact of elevation is neglected. Furthermore, \( k, i, m, n, G_{\text{Rx}}, \) and \( G_{\text{Tx}} \) are the frequency subchannel index, snapshot index, Rx element number, Tx element number, Rx antenna pattern, and Tx antenna pattern, respectively. Based on this data model, the SAGE algorithm can, using an iterative method, provide a maximum-likelihood estimate of the MPC parameters from the measured transfer functions. In our evaluations, we used 30 iterations of the algorithm.

All 13 snapshots that were taken at a given Rx position were used in data processing, with 40 MPCs being extracted from each measurement position. The path parameters, DOA, DOD, and delay were cross checked at a number of positions with the geometry of the measurement site and provided a good match. It must be stressed that the high-resolution algorithms based on the sum-of-plane-waves model cannot explain all the possible propagation processes. For example, diffuse reflections and spherical waves are not covered by the model of (1). For this reason, the total power of the MPCs extracted by SAGE does not necessarily equal the total power of the signals observed at the antenna elements. This can be compounded by the fact that for some locations, more than 40 MPCs might carry significant energy. A quantitative discussion of this is given in Section II-B2.

The estimated Doppler frequency for most MPCs was less than 1 Hz, although at a few locations, Doppler frequencies of around 2–3 Hz were measured. Since the inverse of the Doppler frequency was significantly larger than the total measurement duration of 13 snapshots, this indicates a relatively static measurement scenario.

2) Relative Extracted Power: The received power estimated by SAGE is dependent on, e.g., the environment and the number of extracted MPCs \( L \). The relative extracted power is computed as
\[ Q(L) = \frac{\|\hat{H}(L)\|_F^2}{\|\hat{H}_{\text{meas}}\|_F^2 - \sigma_n^2} \] (2)

where \( \hat{H}_{\text{meas}} \) is the measured transfer matrix, and \( \hat{H}(L) \) is the channel matrix reconstructed from the SAGE estimates of

\[ L = 40 \] MPCs inserted into the channel model of (1). The estimate of the noise power \( \sigma_n^2 \) was calculated at each measurement position as
\[ \sigma_n^2 = \frac{1}{I-1} \sum_{i=1}^{I-1} \|\mathbf{H}_i - \text{diag}(\mathbf{H}_i)\|_F^2 \] (3)

where \( \mathbf{H}_i \) is the measured channel transfer matrix for the \( i \)th snapshot, and \( I \) is the total number of snapshots. This noise estimation was possible because we have an (approximately) time-invariant channel, which we confirmed from our measurements (see above). The cumulative distribution function (CDF) of the relative extracted power is shown for all 159 locations in Fig. 2. As shown in the figure, the extracted power with a source order of 40 significantly varies over the measurement locations. In the majority of measurement locations, more than 85% of the power is captured, although at some positions, only about 60% of the power is captured.

3) Source Order Effects: For different initial estimates of the source order, we have investigated the mean square reconstruction error between the measured data and the matrix reconstructed from MPC parameters estimated by SAGE. For each initial estimate of the source order in the range from 1 to 100 MPCs, the mean square relative reconstruction error (MSRRE) was defined as
\[ \text{MSRRE} = E \left[ \frac{\|\mathbf{H}_{\text{meas}} - \hat{\mathbf{H}}_{\text{reconstruct}}\|_F^2}{\|\mathbf{H}_{\text{meas}}\|_F^2} \right] \] (4)

where \( \mathbf{H}_{\text{meas}} \) is the \( N_R \times N_T \) measured channel, and \( \hat{\mathbf{H}}_{\text{reconstruct}} \) is the matrix reconstructed by (1) from MPCs estimated by SAGE. The expectation is over different frequency subchannels in one measured time snapshot that we use as realizations of the channel. The error from (4) is plotted in Fig. 3 for a typical LOS and non-LOS (NLOS) scenario. It can be observed from Fig. 3 that as we increase the source order (collect more MPCs), the slope of the reconstruction...
error flattens out, which can be interpreted as an indication that we begin to estimate noise spikes (or that we begin to estimate wave parameters that have small correlation peaks in the M-step of the SAGE). By extracting 40 MPCs at each location, we are not in the flat part of the reconstruction error curve, which suggests that we do not estimate noise spikes as specular components. As a further check, we have also verified for each measurement that the difference in power between the strongest and weakest MPCs estimated by SAGE is within the dynamic range of our channel sounder and within the sum (in decibels) of the correlation gain provided by SAGE and the measurement SNR at the respective location to lower the probability that we estimate noise spikes. Although Fig. 3 may suggest that extracting 40 MPCs could lead to an underestimated source order, particularly for the NLOS scenarios, we believe (based on sample evaluations not presented here) that the potential difference in source order will not significantly alter the results presented in this paper. In general, a correct source order estimation is an open research topic, and, in the extreme case, a source order of a few thousand has been used [19].

III. PHYSICAL PROPAGATION PROCESSES

In Fig. 4, the 40 extracted MPCs are plotted for each of the 53 Rx positions corresponding to Tx position 1. The line lengths represent the MPC amplitudes at each measurement location, relative to the strongest MPC at the same location.

This figure allows us to make some important conclusions about the dominant propagation processes.

1) In the north rooms, propagation through walls and windows shows an almost equal efficiency, as one can see from the (relative) strength of the LOS components in the different rooms. The reason lies in the strong attenuation by the windows and walls. The (exterior) walls consist of bricks and reinforced concrete, whereas the windows are coated with a metallic film for energy conservation.3 Adicional measurements of the propagation characteristics of walls and windows showed that the attenuation of the windows is actually slightly larger than the attenuation of the walls.

2) The reflection and diffraction by the window frames are efficient propagation mechanisms. This is evident, e.g., from the DOAs in rooms 2334 and 2336. It is particularly noteworthy that the propagation via the frames of the windows results in an attenuation similar to the attenuation of the brick wall, e.g., see the delay–azimuth plots for position Tx1Rx2336NM in Fig. 5.

3) Each window is split into two glass panes by a horizontal middle section with a metal handle and locking mechanism. There are strong MPCs coming from the window direction; see, e.g., position Tx1Rx2336NM. The delay–azimuth plot in Fig. 5 shows a number of MPCs of similar strength and very similar delays (note that the DOAs are around 180°, which corresponds to the window direction).

4) For some south rooms, propagation through north rooms via doors constitutes a strong propagation mechanism. This is clearly shown, e.g., in the delay–azimuth plot for position Tx1Rx2343SM in Fig. 5.

5) There are strong reflections observed in the south rooms coming from the south. These reflections are from structures along the south walls of the rooms, e.g., metal pipes of heaters mounted on the south wall (refer to Fig. 5 for position Tx1Rx2343SM).

6) While the strengths of the MPCs are widely differing, the directions of the MPCs are more uniformly distributed. Typically, only two or three MPCs show similar DOAs, e.g., refer to Fig. 4. On the other hand, all the DODs are closely grouped together.

Similar results were observed for all three Tx positions.

IV. STATISTICAL ANALYSIS OF ANGULAR AND DELAY DISPERSION

A. Angular Dispersion

The angular dispersion is an important parameter for the characterization of a spatial channel. In this paper, we use direction spread [20] as a measure for the angular dispersion. The direction spread parameter does not suffer from the ambiguity related to the choice of the origin of the coordinate system. The RMS direction spread is calculated as

\[ \sigma_{\text{ang}} = \sqrt{\sum_{l=1}^{L} e^{i\phi_l} - \mu_{\text{ang}}|^2 P_{\text{ang}}(\phi_l) \} } \]  

where

\[ \mu_{\text{ang}} = \sum_{l=1}^{L} e^{i\phi_l} P_{\text{ang}}(\phi_l). \]

3In most countries with a cold climate, such metal-coated windows are typically used in residential and office buildings.

4In [20], “direction” is given by the unity vector in the spherical coordinate system. The direction spread is a dimensionless quantity.
Fig. 4. DOAs at all the receiver positions for transmit position 1. North corresponds to 180° DOA.

Fig. 5. Joint delay–azimuth plot for two Rx positions. The marker diameter is scaled according to the relative power (in decibels) of each MPC, and the MPC powers are normalized with the power of the strongest MPC extracted at the respective Rx position. The measurement position is indicated in each subplot. Note the different scaling for the delay axis.

\[ P_{\text{ang}}(\phi_l) \] is the angular power spectrum normalized as \[ \sum L P_{\text{ang}}(\phi_l) = 1 \]. Figs. 6 and 7 present the CDF of the DOA and DOD spreads for different Tx and Rx locations. The differences between the north and south rooms are evident, particularly at the Rx side. In the corridor, the spread is close to that of the south offices.

The mean direction spreads are presented in Table I. We can immediately see that the angular dispersion at the Rx is markedly higher than for the Tx. This result is intuitive, as the Tx is located outdoors and radiates only toward the Rx, whereas the Rx sees MPCs that can come through the windows and walls or are reflected from walls all around the Rx. Furthermore, it is evident that the transmit position does not affect the mean value of the DOA spread, and there is no large difference in mean spread for the north rooms, corridor, and the south rooms. However, there are large differences in the DOD spread for the different transmit positions. The coupling between the DOAs and DODs will be discussed in Section V-C.

B. Delay Dispersion

The RMS delay spread roughly characterizes the multipath propagation in the delay domain and is conventionally defined as [21]

\[ \sigma_\tau = \sqrt{\frac{\tau^2 - \langle \tau \rangle^2}{\tau_2}} \]  

where the mean excess delay \( \tau \) and the noncentral second moment of the average power delay profile \( \tau^2 \) are defined as [21]

\[ \tau = \frac{\sum_L P_{\text{del}}(\tau_l) \tau_l}{\sum_L P_{\text{del}}(\tau_l)} \quad \text{and} \quad \tau^2 = \frac{\sum_L P_{\text{del}}(\tau_l) \tau_l^2}{\sum_L P_{\text{del}}(\tau_l)} \]
where $P_{\text{del}}(\tau_l)$ is the delay power spectrum, and $\tau_l$ is the delay of the $l$th MPC. Fig. 8 presents the CDF for the RMS delay spread in the north and south rooms. The delay spread has been evaluated using the MPCs as extracted from the SAGE algorithm. This has the drawback that diffuse contributions are not reflected in the obtained delay spreads (which, therefore, tend to be somewhat low). On the other hand, delay spread values that are directly extracted from the measured power delay profiles show too many high values, as noise contributions at large delays have a disproportionate influence. The usual technique of thresholding the average power delay profile (for noise reduction) cannot be applied in our case, since, in some cases, the measurement SNRs are too low for this purpose.\(^5\)

\(^5\)Note that the low SNR problem is mitigated when evaluating the delay spread based on the MPCs. The SAGE algorithm estimates the MPC parameters, including delays by maximizing a correlation function. Due to a large correlation gain accumulated over a typical number of space, time, and frequency samples employed in measurements, the wave parameters can be reliably estimated from a noisy environment. The correlation gain from our measurement parameters ($16 \times 8$ MIMO, 193 frequency subchannels, and 13 time snapshots) is in excess of 50 dB.
Therefore, the delay spread values obtained from the MPC parameters were deemed more reliable.

For the measured outdoor-to-indoor scenario, a cluster analysis of the MPCs has also been performed in the delay–DOA–DOD parameter space. The results are reported in [22].

V. STATISTICAL ANALYSIS

A. LOS Scenario—Fading Statistics

It is widely assumed that in LOS scenarios, the channel coefficients have a nonzero-mean complex Gaussian distribution; this results in a Rician distribution of the amplitudes. The measured channel matrix can be modeled as the weighted residue component drawn from a zero-mean complex Gaussian distribution [23], i.e.,

\[ \mathbf{H}_{\text{model}}(m) = \sqrt{\kappa} \mathbf{H}_{\text{LOS}}^{(n)} + \sqrt{1 - \kappa} \mathbf{H}_{\text{res}}^{(n)}(m) \]

\[ = \sqrt{\kappa} \mathbf{H}_{\text{LOS}}^{(n)} + \sqrt{1 - \kappa} \cdot \text{un-vec} \{ \mathbf{R}^{1/2} \mathbf{G} \} \]

where \( \mathbf{H}_{\text{LOS}} \) is the LOS contribution, \( \mathbf{H}_{\text{res}}(m) \) is the residue in the \( m \)th realization of the channel model, and the superscript \( (n) \) represents the fact that the matrices are normalized as \( E[\| \mathbf{H}_{\text{LOS}}^{(n)} \|^2] = N_{R}N_{T} \). The scalar \( \kappa = (K_{\text{LOS}}/(K_{\text{LOS}} + 1)) \), where \( K_{\text{LOS}} \) is the LOS power factor defined as \( K_{\text{LOS}} \) = (power in LOS component/power in all other components) (see Section V-B). The full channel correlation matrix \( \mathbf{R} \) is estimated as

\[ \mathbf{R} = \frac{1}{M} \sum_{m=1}^{M} \text{vec} \{ \mathbf{H}_{\text{res}}^{(n)}(m) \} \text{vec} \{ \mathbf{H}_{\text{res}}^{(n)}(m) \}^H. \]

In this paper, a measured scenario is treated as an LOS scenario if the strongest estimated MPC has a DOA and DOD that correspond to the hypothetical line connecting the Tx antenna to the Rx antenna. Note that due to this definition of the LOS, a specific antenna element need not have an LOS, although the array is defined to be in an LOS scenario. We have analyzed the validity of the modeling approach in (9) for our LOS scenarios and found that it is not well fulfilled for all our measured data. For example, the data in Fig. 9 have been taken from an LOS scenario; the top figure shows that the magnitudes of the measured channel coefficients do not exhibit a Rician distribution, although after subtracting the estimated LOS contribution, the residue component has a Rayleigh distribution. The CDF is based on the data from a single measurement location, such that both spatial realizations and the 193 frequency subchannels constitute the statistical ensemble. In an attempt to fit various theoretical distributions to the amplitude of the LOS data, we found that the generalized Gamma distribution [24], [25] best represented our measurements. The CDF of the distribution can be expressed as the incomplete Gamma function [26]

\[ \text{Prob}_{\text{GG}}(r < r_0) = P \left( \alpha, \left( \frac{r_0}{\beta} \right)^c \right) \]

where \( P(\cdot) \) is the incomplete Gamma function, and \( \alpha, \beta, \) and \( c \) are the distribution parameters with \( \beta = \sqrt{E[r^2]/(\Gamma(c+1))} \), and \( \Gamma(\cdot) \) is the Gamma function [27]. For all the LOS scenarios that were analyzed, the theoretical CDF of (12) provided a good fit to the measured data with \( \alpha \) in the range 1.2–3.5 and \( c \) in the range 0.7–1.6. For the residue channel as well as NLOS scenarios, the parameter values \( c = 2 \) and \( \alpha = 1 \), which correspond to a Rayleigh fading statistic [25], provide a good match to the measured data distribution.

The generalized Gamma distribution has been used in [28] to represent a composite fading distribution. We investigated possible reasons why the fading distribution in our LOS scenarios deviated from the “standard” model and found that some Rx elements experienced shadow fading, i.e., the mean received power at the Rx elements considerably varied over the array. The shadow fading was a consequence of the absorber\(^6\) that was part of the array construction; see Fig. 10(a).

Fig. 10(b), together with Fig. 11, illustrates how the absorber attenuates the LOS contribution received at the back elements of the array. Therefore, the fading distribution of the channel coefficients becomes a function of which Rx elements are considered for the ensemble. We conjecture that a similar effect would be found with a circular array of patch antennas. Thus, as an important consequence of our investigation, we find that the “standard” model of (9) is applicable for some specific receiver configurations, and the definition of, e.g., a Rice factor based on the model is meaningful. However, the model is not universally applicable, i.e., in LOS scenarios, the small-scale fading statistics may not necessarily be Rician. In our case, it is shadowing due to the array configuration that causes a composite fading distribution over a small-scale area, the Rx array, and the generalized Gamma distribution rather than the Rician is in good agreement with the measured LOS data.

B. LOS Power Factor and Rician K-Factor

We make a distinction between the conventional Rician K-factor \( K_{\text{Rice}} \), and what we term the LOS power factor \( K_{\text{LOS}} \). We define the latter as

\[ K_{\text{LOS}} = \frac{E[\| \mathbf{H}_{\text{LOS}} \|^2]}{E[\| \mathbf{H}_{\text{res}} \|^2]}. \]

\(^6\)The absorber suppresses the back-lobe of the elements. This indicates a lower probability of locking into false and local minima in the iterative estimation procedure; and, hence, a better performance of the high-resolution algorithm.
It is essentially the ratio between the power in the estimated LOS component and the power in all the other components. The LOS estimate $\hat{H}_{\text{LOS}}$ can be extracted from a high-resolution algorithm such as SAGE by inserting channel parameters of the LOS path into the signal model assumed by the algorithm. Note that matrices with unnormalized power are used in calculating $K_{\text{LOS}}$.

It should be stressed that $K_{\text{LOS}}$ is different from $K_{\text{Rice}}$. The LOS power factor physically relates to the LOS component, which is strong but is not necessarily the only strong component present in the measured scenario. Still, it can be uniquely identified in a MIMO scenario by its DOA and DOD (they have to agree with the angles that correspond to the “direct line” between the Tx and Rx antennas). On the other hand, $K_{\text{Rice}}$ is a characteristic parameter of the Rician amplitude distribution. It is conventionally related to the narrowband amplitude distribution; even when it is used to describe the amplitude characteristics of the first delay bin, it does not have a strict correspondence to the LOS component. The Rician $K$-factors can be extracted, e.g., with the method-of-moments, as suggested by Greenstein et al. [29]. Table II compares the estimated values of $K_{\text{Rice}}$ and $K_{\text{LOS}}$ in some of our measured...
Fig. 10. (a) Rx array is a 16-element vertically polarized UCA; the absorber is shown in the middle. (b) Orientation of UCA elements with respect to angle measure 0° to 180° in either direction of rotation. The element numbers (1–16) are indicated along the circumference of the UCA, and the arcs relate the Rx elements to the corresponding CDFs in Fig. 11.

Fig. 11. Measured channel. Effect of selecting Rx elements on the fading distribution of the channel coefficients. Position Tx2Rx2337ME.

TABLE II

<table>
<thead>
<tr>
<th>Position</th>
<th>Rx elements</th>
<th>$K_{\text{LOS}}$</th>
<th>$K_{\text{Rice}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tx1 Rx234MM</td>
<td>8-11</td>
<td>2.5</td>
<td>4.3</td>
</tr>
<tr>
<td>Tx1 Rx2334SM</td>
<td>8-11</td>
<td>1.6</td>
<td>2.4</td>
</tr>
<tr>
<td>Tx1 Rx2337NM</td>
<td>7-10</td>
<td>1.9</td>
<td>2.6</td>
</tr>
<tr>
<td>Tx2 Rx2337ME</td>
<td>9-12</td>
<td>2.8</td>
<td>3.0</td>
</tr>
<tr>
<td>Tx2 Rx2336NM</td>
<td>7-10</td>
<td>2.2</td>
<td>2.1</td>
</tr>
</tbody>
</table>

Fig. 12. Joint DOA–DOD plot for Rx position Tx1Rx2345SM. The marker diameter is scaled according to the power of each MPC relative to the power of the strongest component [decibel scale].

A fair comparison between the two parameters requires that the fading distribution in question is Rician, as it would only then be meaningful to talk of a Rician $K$-factor. To avoid the absorber effect discussed in Section V-A, we selected a subset of four consecutive Rx elements at each measurement location (column 2 in Table II). The selected elements for each measurement position form an arc, which contains the DOA of the respective LOS MPC. The results shown in Table II indicate a general trend that the LOS power factor is different from $K_{\text{Rice}}$. Furthermore, we propose to use $K_{\text{LOS}}$ rather than $K_{\text{Rice}}$ in modeling LOS scenarios, as in (9). The relative performance of the two metrics in modeling an LOS scenario is discussed further in Section V-C3 (see Fig. 14).

C. Interconnection Between DOAs and DODs

As a third topic of our investigation, we analyze the coupling between the DOAs and DODs. In Fig. 12, the joint DOA–DOD spectrum is shown for one Rx position corresponding to Tx position 1. The plot shows that the joint DOA–DOD spectrum is not separable into the marginal angular spectra. To quantify this effect, we investigate three analytical channel models that make different assumptions about the coupling between DOAs and DODs. All three models share the common
assumption that the channel matrix has zero-mean complex Gaussian entries. For analyzing the LOS scenarios, we consider only a subset of the full LOS channel matrix, i.e., those rows in the matrix that correspond to Rx elements that receive the LOS component free from the absorber effect. The analysis in Sections V-A and B guarantees that the subset channel has Rician fading. We then model this subset channel according to (9), where only $H_{\text{res}}$ is modeled by the zero-mean Gaussian models. For NLOS scenarios, no such limitation exists, and we can test the model validity for larger channel matrices.

1) Kronecker Model: The Kronecker model [6], [13] approximates the full channel correlation matrix $R$ by the Kronecker product of the transmit and receive antenna correlation matrices $R_{\text{Tx}}$ and $R_{\text{Rx}}$, respectively. Equivalently, the MIMO channel matrix is modeled as

$$H_{\text{Kron}} = \frac{1}{\sqrt{\text{tr}\{R_{\text{Rx}}\}}} R_{\text{Rx}}^{1/2} G R_{\text{Tx}}^{1/2}. \quad (14)$$

The Kronecker model assumes that the DOA spectrum, and hence, the structure of the Rx correlation matrix does not change for different DODs.\(^7\) In the context of Fig. 12, the Kronecker assumption, when fulfilled, would imply a rectangular structure, i.e., if one groups the estimated DODs into narrow angular bins, where each bin results in a set of DOAs and path powers according to (1), the Kronecker assumption is considered fulfilled if the DOA power spectrum for each of the DOD bins is similar. We have analyzed the validity of the Kronecker model for both LOS and NLOS scenarios. Fig. 13 shows the modeled ergodic capacity plotted against the measured one for a number of measurement locations. In the top figure (a $2 \times 8$ LOS setup), the Kronecker model deviates only very little from the measured results. This nice fit is due to the small rank of the channel matrix [30]. The bottom half of Fig. 13 is a $16 \times 8$ NLOS setup. This setup shows large deviations between the modeled and measured capacity due to the Kronecker assumption about the joint DOA–DOD spectrum. In [7], it is suggested that the Kronecker model, in general, underestimates the channel capacity. This is validated for the outdoor-to-indoor scenario by our results.

Note that the LOS locations considered in Fig. 13 have a measured SNR in the range of 14–20 dB. When computing the ergodic capacity at those locations, the evaluation SNR in the capacity formula was always set to 10 dB below the corresponding measured value. In a previous work [12] that analyzes the impact of measurement noise on capacity, it was established that even for a “keyhole” MIMO channel (in which the capacity is very sensitive to measurement noise), the capacity calculations are correct as long as the measurement SNR is 10 dB better than the evaluation SNR. Thus, our reported results are not influenced by measurement noise. For the NLOS scenarios considered in Fig. 13, the measurement SNR was in a considerably lower range of 1–13 dB. However, we mitigated the measurement noise at each location by coherently averaging the channel matrices over the available 13 time snapshots; this improves the measurement SNR by a factor exceeding 10 dB. For capacity evaluation, we always use the noise-suppressed channel matrices and set the evaluation SNR in the capacity formula to the unprocessed value of the measured SNR so that we have a 10-dB difference between measured and evaluation SNR. Therefore, our NLOS capacity results also represent the true channel capacity.

2) VCR: The virtual channel representation (VCR) was introduced in [31] for a ULA at each link end and allows an arbitrary coupling between predetermined directions at the Tx and

\(^7\)However, the total power in the spectrum, which is a scale factor for the correlation matrix, is allowed to change.
Rx sides. The model uses discrete Fourier transform matrices $A_{Rx}$ and $A_{Tx}$ at respective link ends such that the measured channel and the virtual channel are unitarily equivalent. The realizations of the channel model can be generated as

$$H_{VCR} = A_{Rx}(\hat{\Omega} \odot G)A_{Tx}^T$$

(15)

where the columns of $A_{Rx}$ and $A_{Tx}$ are based on the array response (steering) vectors computed at fixed virtual directions, and the matrix $\hat{\Omega}$ is the element-wise square root of the power coupling matrix $\Omega$. The entry $\Omega_{ij}$ gives the average power coupled between the $i$th receive and $j$th transmit direction. This beamforming approach thus incorporates the antenna array effects. However, since the directions are predetermined, and scatterers within the spatial resolution of the array will not be resolved, it is possible that the true spatial characteristics of the channel will not be accurately rendered for some scenarios.

In our measurement setup, the Rx array was not a ULA but rather a UCA with an absorber in the center. We thus use a generalization of (15) that combines the standard virtual channel model at the Tx side with a “canonical” representation, based on the channel statistics, at the Rx side, i.e.,

$$H_{VCR} = \hat{U}_{Rx}(\hat{\Omega} \odot G)\hat{A}_{Tx}^T$$

where $\hat{U}_{Rx}$ is an estimate of the receive eigenvector matrix obtained by the eigenvalue decomposition of $R_{Rx}$. In Fig. 13, the ergodic capacities computed from this model are also shown. For the $16 \times 8$ NLOS setup, the capacity from this model tends to slightly overestimate the measured values.

3) Weichselberger Model: Like the Kronecker model, the Weichselberger model [7] represents the measured channel in the eigenvector domain, although, unlike the Kronecker model, it strives to jointly model channel correlations at both link ends. This is achieved by defining a power coupling matrix between the eigenvectors of the two link ends. The Weichselberger model assumes that the eigenvector matrix at the Rx is independent of the spatial Tx weight vector, i.e., DOD, that is considered. However, the corresponding eigenvalues of the spatial correlation matrix at Rx can differ for different DODs. The same argument applies to the reverse link. The physical interpretation of the modeling assumptions can be found in [7], wherein the channel is modeled as

$$\hat{H}_{\text{weichsel}} = \hat{U}_{Rx}(\hat{\Omega} \odot G)\hat{U}_{Tx}^T$$

(16)

where $\hat{U}_{Rx}$ and $\hat{U}_{Tx}$ are estimates of the receive and transmit eigenvector matrices obtained by the eigenvalue decomposition of $R_{R}$ and $R_{T}$, respectively. The elements of the power coupling matrix $\hat{\Omega}_{ij}$ now give the average power coupled between the $i$th receive and $j$th transmit eigenvector; the matrix is estimated as

$$\hat{\Omega} = \frac{1}{M} \sum_{m=1}^{M} [K \odot K^H]$$

(17)

where $K = (\hat{U}_{Rx}^H H(m) \hat{U}_{Tx})$, and $H(m)$ is the $m$th channel realization. It should be noted that the Kronecker model is a special case of the Weichselberger model. In Fig. 13, the ergodic capacity computed from the Weichselberger model is shown for the same measurement locations as for the previous cases. Compared to the Kronecker model, the Weichselberger model provides a better fit to the measured data. This result is expected from Fig. 12, where the joint spectrum is not separable into the marginal spectra. The Weichselberger model fits the measured data better than the VCR case as well. This can be explained because in the former case, the channel statistics determine the unitary matrices at both link ends. Our results, which were obtained for the outdoor-to-indoor scenario, are consistent with the observations in [7], which separately considered the pure indoor and outdoor cases. As a follow-up to Section V-B, we use the Weichselberger model and the ergodic capacity as a metric to compare the performance of $K_{\text{Rice}}$ and $K_{\text{LOS}}$ in modeling an LOS scenario according to (9). The plots are shown in Fig. 14 for a $2 \times 8$ LOS setup. Although the restriction to use a small rank LOS channel will result in a convergence of performance of the two metrics, from the figure, the $K_{\text{LOS}}$ metric appears to perform better.

VI. CONCLUSION

In this paper, we have presented the results of a double-directional measurement campaign for an outdoor-to-indoor office scenario. Our characterization of the outdoor-to-indoor scenario indicates that the angular dispersion at the outdoor link end is rather small; the mean direction spread is in the range of 0.09–0.24. At the indoor link end, MPCs of significant energy arrive from all directions; therefore, the angular dispersion is much larger, we observed mean direction spreads in the range of 0.69–0.82. The delay spread was measured to be in the range of 5–25 ns. By considering 40 MPCs at each measured position, more than 85% of the received power could be accounted for in 60% of the 159 measurement locations.

Our statistical analysis shows that the widely used assumption in MIMO channel modeling, i.e., that the channel can be represented as a sum of a weighted LOS component plus a zero-mean complex Gaussian distribution, may not adequately
represent the measured data. In general, the small-scale fading in an LOS scenario may not be Rician. We observed a composite fading distribution caused by our antenna configuration and found the generalized Gamma distribution to be a useful tool for verifying this. Furthermore, we have highlighted the difference between the LOS power factor and the Rician $K$-factor and support this assertion with the measured data from a Rician fading channel. We show that the DOA–DOD decoupling assumptions; this holds true even for the NLOS scenarios. Compared to the VCR model, the Weichselberger model provides a better fit to the measured capacity for both the LOS and NLOS scenarios.

Our results can serve as a basis for understanding the outdoor-to-indoor MIMO channels and have served as an input to the COST 273 MIMO channel model [32].

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